

**P2 PORTAL COLUMN 1.1 M DIAMETER**

**TOP**

## **Serviceability Check - Traffic Load Only**



**KATAHIRA & ENGINEERS  
INTERNATIONAL**

**Project:** Detailed Design Study of  
North Java Corridor Flyover Project

**Calculation:** Balaraja Flyover  
Serviceability Check - Traffic Load Only  
1100 mm Dia Circular RC Column - P2 Top Section

**Reference:** Project Specific Design Criteria

**Section Data**

MPa := 1000000·Pa

kN := 1000·N

Input Item		
Concrete Compressive Strength	fc	30 MPa
Structural Steel Yield Strength	fys	250 MPa
Rebar Yield Strength	fy	390 MPa
Diameter of reinforced concrete section	D	1100 mm
Thickness of CHS section	t	0 mm
Diameter of rebar - layer 1	dia1	32 mm
Diameter of rebar - layer 2	dia2	0 mm
Number bars - layer 1 (max 100)	n1	30
Number bars - layer 2 (max 100)	n2	0
Cover from face of section - layer 1	cov1	60 mm
Cover from face of section - layer 2	cov2	115 mm

**Load Data**

Ref	Pier	Load Case	P	M	Stress
			kN	kNm	Allowance
1	P21	Combination 1 - P + Traffic Load Only	3173.2	1877.2	100%
2	P21	Combination 1 - P + Traffic Load Only	3173.2	901.7	100%
3	P22	Combination 1 - P + Traffic Load Only	3177.7	1878.1	100%
4	P22	Combination 1 - P + Traffic Load Only	3177.7	900.9	100%

$$f_c := f_c \cdot \text{MPa} \quad f_{ys} := f_{ys} \cdot \text{MPa} \quad f_y := f_y \cdot \text{MPa} \quad D := D \cdot \text{mm} \quad ts := ts \cdot \text{mm}$$

$$\text{dia1} := \text{dia1} \cdot \text{mm} \quad \text{dia2} := \text{dia2} \cdot \text{mm} \quad \text{cov1} := \text{cov1} \cdot \text{mm} \quad \text{cov2} := \text{cov2} \cdot \text{mm}$$

$$P := P \cdot \text{kN} \quad M := M \cdot \text{kN} \cdot \text{m}$$

$$E_S := 200000 \cdot \text{MPa} \quad E_C := 4700 \sqrt{\frac{f_c}{\text{MPa}}} \cdot \text{MPa} \quad \text{Modular ratio} \quad \alpha := \begin{cases} \frac{E_S}{E_C} & \text{if } E_C > 0 \\ 1 & \text{otherwise} \end{cases} \quad \alpha = 7.77$$

$$E_C = 25743 \text{ MPa}$$

### Calculate Basic Allowable Stresses

Calculate rupture stress:

$$\sigma_{ct} := 0.5 \cdot \left( \frac{f_c}{\text{MPa}} \right)^{\frac{2}{3}} \cdot \text{MPa} \quad \sigma_{ct} = 4.8 \text{ MPa}$$

Calculate basic allowable stress of concrete

$$\sigma_{cc} := 1.0 \cdot f_c \quad \sigma_{cc} = 30.0 \text{ MPa}$$

Calculate basic allowable tensile stress of rebar

$$\sigma_{rs} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 170 \text{ MPa} \\ 170 \text{ MPa} & \text{otherwise} \end{cases} \quad \sigma_{rs} = 170 \text{ MPa}$$

Calculate basic allowable compressive stress of rebar

$$\sigma_{rc} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 110 \text{ MPa} \\ f_y & \text{otherwise} \end{cases} \quad \sigma_{rc} = 390 \text{ MPa}$$

Calculate basic allowable stress of structural steel

$$\sigma_{ts} := -0.6 f_{ys} \quad \sigma_{ts} = -150 \text{ MPa}$$

$$\sigma_{tc} := 1 f_{ys} \quad \sigma_{tc} = 250 \text{ MPa}$$

Limiting strain of rebar

$$\epsilon_{rs} := -\frac{\sigma_{rs}}{E_S} \quad \epsilon_{rs} = -0.000850$$

$$\epsilon_{rc} := \frac{\sigma_{rc}}{E_S} \quad \epsilon_{rc} = 0.001950$$

Limiting strain of structural steel

$$\epsilon_{ts} := \frac{\sigma_{ts}}{E_S} \quad \epsilon_{ts} = -0.000750$$

$$\epsilon_{tc} := \frac{\sigma_{tc}}{E_S} \quad \epsilon_{tc} = 0.001250$$

### Concrete Cross Section Data - generated

n := 50      Number of Points - 50 points maximum

i := 1 .. n + 1      Range from 1 to n+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	550
2	-69	-546	27	69	546
3	-137	-533	28	137	533
4	-202	-511	29	202	511
5	-265	-482	30	265	482
6	-323	-445	31	323	445
7	-377	-401	32	377	401
8	-424	-351	33	424	351
9	-464	-295	34	464	295
10	-498	-234	35	498	234
11	-523	-170	36	523	170
12	-540	-103	37	540	103
13	-549	-35	38	549	35
14	-549	35	39	549	-35
15	-540	103	40	540	-103
16	-523	170	41	523	-170
17	-498	234	42	498	-234
18	-464	295	43	464	-295
19	-424	351	44	424	-351
20	-377	401	45	377	-401
21	-323	445	46	323	-445
22	-265	482	47	265	-482
23	-202	511	48	202	-511
24	-137	533	49	137	-533
25	-69	546	50	69	-546

k := 1 .. 25      XS1 := XS1·mm    XS2 := XS2·mm      YS1 := YS1·mm    YS2 := YS2·mm

$x_k := XS1_k$        $y_k := YS1_k$        $x_{k+25} := XS2_k$        $y_{k+25} := YS2_k$        $x_{n+1} := XS1_1$        $y_{n+1} := YS1_1$

### Calculate Section Properties of Concrete Section

$$A_C := - \sum_{i=1}^n \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{2} \right] \quad A_C = 0.94783 \text{ m}^2$$

$$x_C := - \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{y_{i+1} - y_i}{8} \cdot \left[ (x_{i+1} + x_i)^2 + \frac{(x_{i+1} - x_i)^2}{3} \right] \right] \quad x_C = 0 \text{ m}$$

$$y_C := \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{x_{i+1} - x_i}{8} \cdot \left[ (y_{i+1} + y_i)^2 + \frac{(y_{i+1} - y_i)^2}{3} \right] \right] \quad y_C = 0 \text{ m}$$

$$I_x := \sum_{i=1}^n \left[ \left[ (x_{i+1} - x_i) \cdot \frac{y_{i+1} + y_i}{24} \right] \cdot \left[ (y_{i+1} + y_i)^2 + (y_{i+1} - y_i)^2 \right] \right] \quad I_x = 0.07149 \text{ m}^4$$

$$I_y := - \sum_{i=1}^n \left[ \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{24} \right] \cdot \left[ (x_{i+1} + x_i)^2 + (x_{i+1} - x_i)^2 \right] \right] \quad I_y = 0.07149 \text{ m}^4$$

$$I_{xC} := I_x - A_C \cdot x_C^2 \quad I_{xC} = 0.07149 \text{ m}^4$$

$$I_{yC} := I_y - A_C \cdot y_C^2 \quad I_{yC} = 0.07149 \text{ m}^4$$

### Steel Tube Cross Section Data - generated from input

ns := 50      Number of Points - 50 points maximum

ps := 1 .. ns + 1      Range from 1 to ns+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	-550
2	-142	-531	27	142	-531
3	-275	-476	28	275	-476
4	-389	-389	29	389	-389
5	-476	-275	30	476	-275
6	-531	-142	31	531	-142
7	-550	0	32	550	0
8	-531	142	33	531	142
9	-476	275	34	476	275
10	-389	389	35	389	389
11	-275	476	36	275	476
12	-142	531	37	142	531
13	0	550	38	0	550
14	142	531	39	-142	531
15	275	476	40	-275	476
16	389	389	41	-389	389
17	476	275	42	-476	275
18	531	142	43	-531	142
19	550	0	44	-550	0
20	531	-142	45	-531	-142
21	476	-275	46	-476	-275
22	389	-389	47	-389	-389
23	275	-476	48	-275	-476
24	142	-531	49	-142	-531
25	0	-550	50	0	-550

$$XSS1 := XSS1 \cdot \text{mm}$$

$$XSS2 := XSS2 \cdot \text{mm}$$

$$YSS1 := YSS1 \cdot \text{mm}$$

$$YSS2 := YSS2 \cdot \text{mm}$$

$$z := 1 .. 25$$

$$xs_z := XSS1_z$$

$$ys_z := YSS1_z$$

$$z := 26 .. 50$$

$$xs_z := XSS2_{z-25}$$

$$ys_z := YSS2_{z-25}$$

$$xs_{ns+1} := XSS1_1$$

$$ys_{ns+1} := YSS1_1$$



### Calculate Section Properties of Steel Tube Section

$$A_{ST} := - \sum_{ps=1}^{ns} \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{2} \right] \quad A_{ST} = 0 \text{ m}^2$$

$$x_{ST} := - \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{y_{ps+1}^{s} - y_{ps}^{s}}{8} \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + \frac{(x_{ps+1}^{s} - x_{ps}^{s})^2}{3} \right] \right] \quad x_{ST} = 0.2 \text{ m}$$

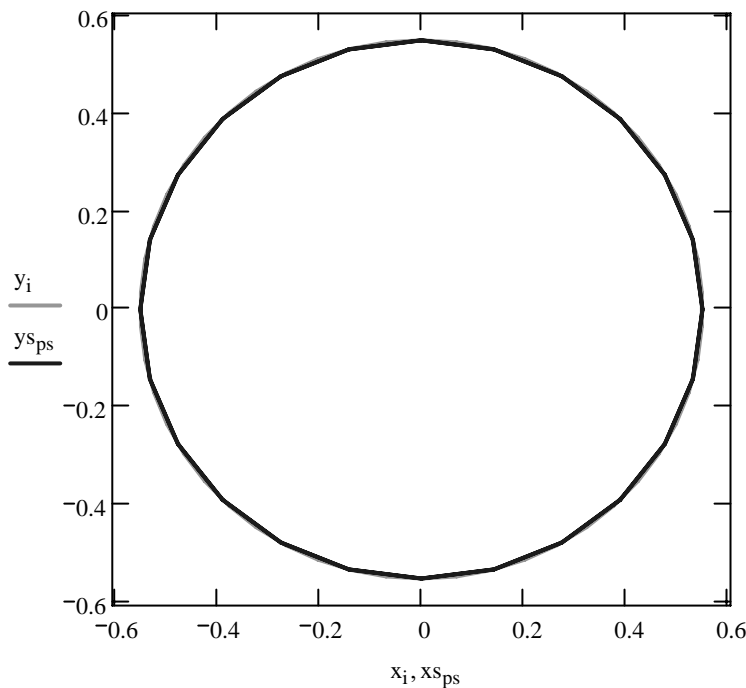
$$y_{ST} := \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{x_{ps+1}^{s} - x_{ps}^{s}}{8} \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + \frac{(y_{ps+1}^{s} - y_{ps}^{s})^2}{3} \right] \right] \quad y_{ST} = -0.011 \text{ m}$$

$$I_{xS} := \sum_{ps=1}^{ns} \left[ \left[ (x_{ps+1}^{s} - x_{ps}^{s}) \cdot \frac{y_{ps+1}^{s} + y_{ps}^{s}}{24} \right] \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + (y_{ps+1}^{s} - y_{ps}^{s})^2 \right] \right] \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := - \sum_{ps=1}^{ns} \left[ \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{24} \right] \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + (x_{ps+1}^{s} - x_{ps}^{s})^2 \right] \right] \quad I_{yS} = 0 \text{ m}^4$$

$$I_{xS} := I_{xS} - A_{ST} \cdot x_{ST}^2 \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := I_{yS} - A_{ST} \cdot y_{ST}^2 \quad I_{yS} = 0.00000 \text{ m}^4$$



**Rebar Data Layer 1 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	804	0	-474	51	0	0	0
2	804	-99	-464	52	0	0	0
3	804	-193	-433	53	0	0	0
4	804	-279	-383	54	0	0	0
5	804	-352	-317	55	0	0	0
6	804	-410	-237	56	0	0	0
7	804	-451	-146	57	0	0	0
8	804	-471	-50	58	0	0	0
9	804	-471	50	59	0	0	0
10	804	-451	146	60	0	0	0
11	804	-410	237	61	0	0	0
12	804	-352	317	62	0	0	0
13	804	-279	383	63	0	0	0
14	804	-193	433	64	0	0	0
15	804	-99	464	65	0	0	0
16	804	0	474	66	0	0	0
17	804	99	464	67	0	0	0
18	804	193	433	68	0	0	0
19	804	279	383	69	0	0	0
20	804	352	317	70	0	0	0
21	804	410	237	71	0	0	0
22	804	451	146	72	0	0	0
23	804	471	50	73	0	0	0
24	804	471	-50	74	0	0	0
25	804	451	-146	75	0	0	0
26	804	410	-237	76	0	0	0
27	804	352	-317	77	0	0	0
28	804	279	-383	78	0	0	0
29	804	193	-433	79	0	0	0
30	804	99	-464	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

**Rebar Data Layer 2 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	0	0	0	51	0	0	0
2	0	0	0	52	0	0	0
3	0	0	0	53	0	0	0
4	0	0	0	54	0	0	0
5	0	0	0	55	0	0	0
6	0	0	0	56	0	0	0
7	0	0	0	57	0	0	0
8	0	0	0	58	0	0	0
9	0	0	0	59	0	0	0
10	0	0	0	60	0	0	0
11	0	0	0	61	0	0	0
12	0	0	0	62	0	0	0
13	0	0	0	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

$$A1 := A1 \cdot \text{mm}^2 \quad A2 := A2 \cdot \text{mm}^2 \quad A3 := A3 \cdot \text{mm}^2 \quad A4 := A4 \cdot \text{mm}^2$$

$$X1 := X1 \cdot \text{mm} \quad X2 := X2 \cdot \text{mm} \quad X3 := X3 \cdot \text{mm} \quad X4 := X4 \cdot \text{mm}$$

$$Y1 := Y1 \cdot \text{mm} \quad Y2 := Y2 \cdot \text{mm} \quad Y3 := Y3 \cdot \text{mm} \quad Y4 := Y4 \cdot \text{mm}$$

$$k := 1..50$$

$$A_{\text{bar}_k} := A1_k \quad x_{\text{bar}_k} := X1_k \quad y_{\text{bar}_k} := Y1_k$$

$$A_{\text{bar}_{k+50}} := A2_k \quad x_{\text{bar}_{k+50}} := X2_k \quad y_{\text{bar}_{k+50}} := Y2_k$$

$$A_{\text{bar}_{k+100}} := A3_k \quad x_{\text{bar}_{k+100}} := X3_k \quad y_{\text{bar}_{k+100}} := Y3_k$$

$$A_{\text{bar}_{k+150}} := A4_k \quad x_{\text{bar}_{k+150}} := X4_k \quad y_{\text{bar}_{k+150}} := Y4_k$$

### Calculate Section Properties of Reinforcement

$$A_{\text{BAR}} := \sum_{j=1}^{200} A_{\text{bar}_j} \quad A_{\text{BAR}} = 24127 \text{ mm}^2$$

$$\rho := \frac{A_{\text{BAR}}}{A_C} \quad \rho = 0.0255$$

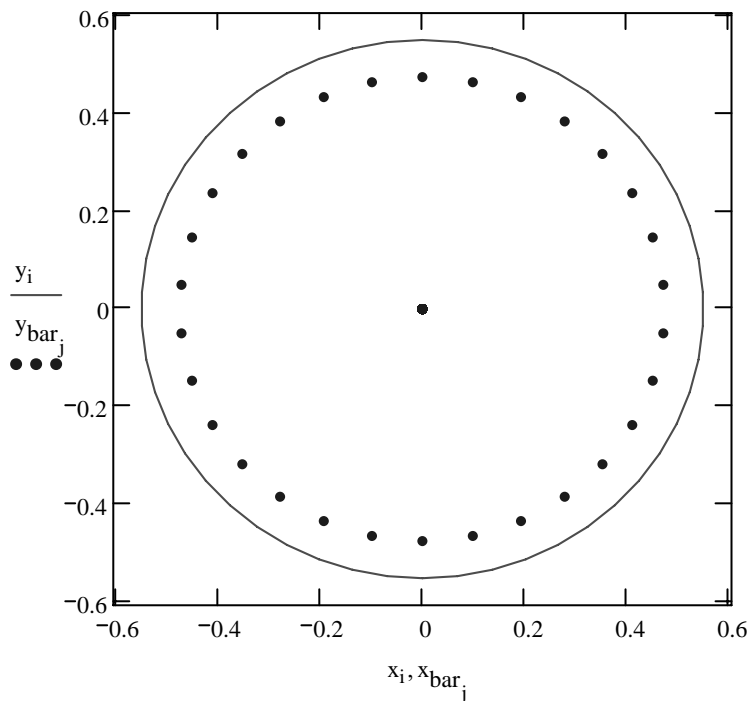
$$x_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot x_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad x_b = 0 \text{ m}$$

$$y_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot y_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad y_b = 0 \text{ m}$$

$$I_{x_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (x_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot x_b^2 \quad I_{x_b} = 0.00271 \text{ m}^4$$

$$I_{y_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (y_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot y_b^2 \quad I_{y_b} = 0.00271 \text{ m}^4$$

$j := 1 \dots 200$



**Calculate Composite Section Properties (before cracking)**

Effective area  $A_E := A_C \cdot [1 + \rho \cdot (\alpha - 1)] + A_{ST} \cdot \alpha$   $A_E = 1111154 \text{ mm}^2$

Effective centroid  $x_E := \frac{A_C \cdot [(1 - \rho) \cdot x_C + \rho \cdot x_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot x_{ST}}{A_E}$   $x_E = 0.000 \text{ m}$

$y_E := \frac{A_C \cdot [(1 - \rho) \cdot y_C + \rho \cdot y_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot y_{ST}}{A_E}$   $y_E = 0.000 \text{ m}$

Effective stiffness  $I_{EX} := I_{xC} + I_{xb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot x_C^2 + \rho \cdot x_b^2 \cdot \alpha] + (I_{xS} + A_{ST} \cdot x_{ST}^2) \cdot \alpha$   
 $I_{EX} = 0 \text{ m}^4$

$I_{EY} := I_{yC} + I_{yb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot y_C^2 + \rho \cdot y_b^2 \cdot \alpha] + (I_{yS} + A_{ST} \cdot y_{ST}^2) \cdot \alpha$   
 $I_{EY} = 0 \text{ m}^4$

Distance from extreme concrete fiber to centroid

$x_{F_{pos}} := \max(x - x_E)$   $x_{F_{neg}} := \min(x - x_E)$

$y_{F_{pos}} := \max(y - y_E)$   $y_{F_{neg}} := \min(y - y_E)$

Total depth of concrete section

$H_{CX} := x_{F_{pos}} - x_{F_{neg}}$   $H_{CX} = 1 \text{ m}$

$H_{CY} := y_{F_{pos}} - y_{F_{neg}}$   $H_{CY} = 1 \text{ m}$

Section modulus

$$Z_{Xpos} := \frac{I_{EX}}{xF_{pos}}$$

$$Z_{Xneg} := \frac{I_{EX}}{xF_{neg}}$$

$$Z_{Ypos} := \frac{I_{EY}}{yF_{pos}}$$

$$Z_{Yneg} := \frac{I_{EY}}{yF_{neg}}$$

Thickness of steel tube:

$$ts := y_1 - ys_1$$

$$ts = 0 \text{ mm}$$

**Establish Section Dimensions**

Positive case - determine coord of extreme concrete fiber

$$y_{Epos} := \max(y)$$

$$y_{Epos} = 550 \text{ mm}$$

Negative case - determine coord of extreme concrete fiber

$$y_{Eneg} := \min(y)$$

$$y_{Eneg} = -550 \text{ mm}$$

Offsets of rebar from extreme fiber

$$y_{Obar} := y_{Epos} - y_{bar}$$

Determine most extreme rebar (minimum offset)

$$y_{1bar} := \min(y_{Epos} - y_{bar})$$

$$y_{1bar} = 76 \text{ mm}$$

Determine most extreme rebar (maximum offset)

$$y_{nbar} := \max(y_{Epos} - y_{bar})$$

$$y_{nbar} = 1024 \text{ mm}$$

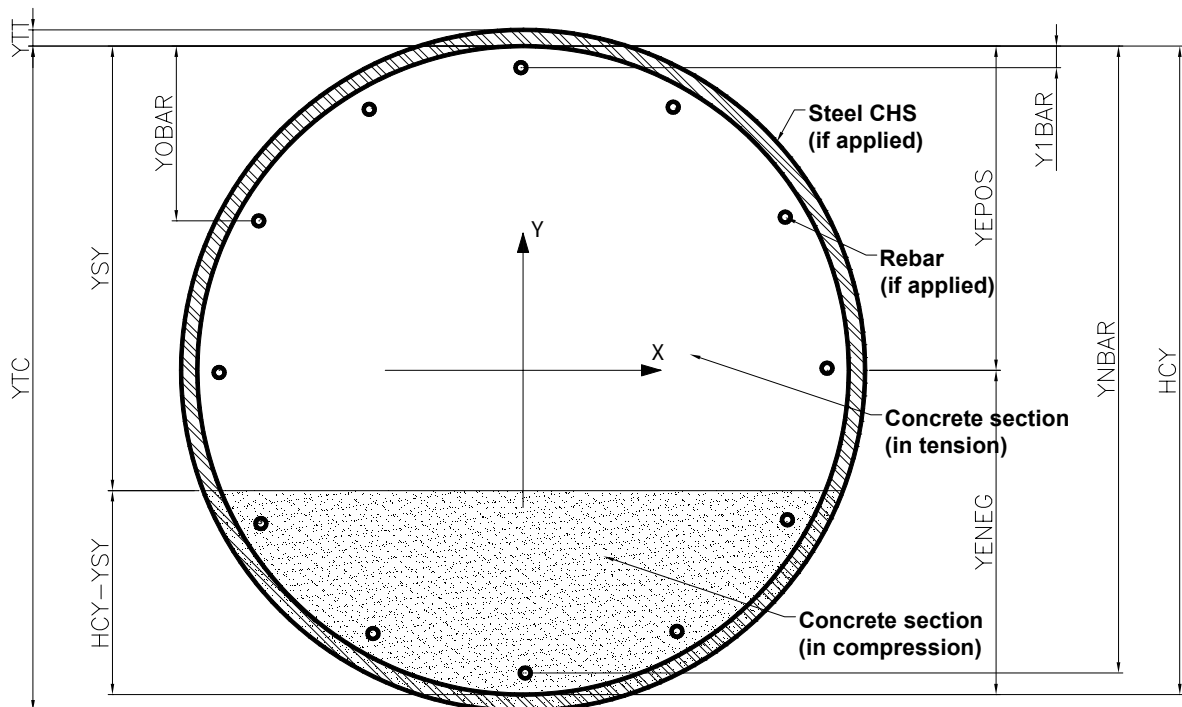
Offsets of extreme steel tube fiber from extreme concrete fiber

$$y_{tt} := ts$$

$$y_{tt} = 0 \text{ mm}$$

$$y_{tc} := H_{CY} + ts$$

$$y_{tc} = 1100 \text{ mm}$$



**ASSIGN NEUTRAL AXIS VALUES**

Number of sections to analysed                      ns := 500

q := 2 .. ns

Distance of neutral axis from extreme fiber in tension                       $y_{SY_q} := H_{CY} \cdot \frac{q}{ns + 1}$

**Calculate stresses and strains in reinforcement and concrete at extreme fibers**

Calculate strain at extreme compression fiber assuming max allowable stress in concrete:

Trial value of concrete strain

$$\epsilon_{cc} := \frac{\sigma_{cc}}{E_C} \cdot 2 \qquad \frac{\sigma_{cc}}{E_C} = 0.001165$$

Given

$$\sigma_{cc} = \epsilon_{cc} \cdot \left( 4700 \sqrt{\frac{f_c \cdot 2}{MPa}} - \frac{4700^2}{2.68} \cdot \epsilon_{cc} \right) \cdot MPa$$

$$\epsilon_{cc} := \text{Find}(\epsilon_{cc}) \qquad \epsilon_{cc} = 0.003321$$

$$\epsilon_{cc} := \begin{cases} \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \epsilon_{cc} & \text{otherwise} \end{cases} \qquad \epsilon_{cc} = 0.003321$$

Strain at other stresses taken to be linear:

$$\epsilon_{cc}(f_c, \sigma_{cd}) := \begin{cases} \frac{\sigma_{cd}}{\sigma_{tc}} \cdot \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \frac{\sigma_{cd}}{\sigma_{rc}} \cdot \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \frac{\sigma_{cd}}{\sigma_{cc}} \cdot \epsilon_{cc} & \text{otherwise} \end{cases}$$

Calculate strain in steel tube assuming max allowable stress in concrete:

In compression                       $\epsilon_{tcc_q} := \epsilon_{cc} \cdot \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}}$

In tension                               $\epsilon_{tct_q} := \epsilon_{cc} \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}}$

Calculate strain in rebar assuming max allowable stress in concrete:

$$\text{In compression} \quad \varepsilon_{rcc_q} := \varepsilon_{cc} \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

$$\text{In tension} \quad \varepsilon_{rct_q} := \varepsilon_{cc} \cdot \frac{y_{1bar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

Calculate design max stress in compression taking account of other limits:

$$\sigma_{cd}(\varepsilon_{tcc}, q) := \begin{cases} \sigma_{cd} \leftarrow \sigma_{cc} & \text{if } f_c > 0 \\ \sigma_{cd} \leftarrow \sigma_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \sigma_{cd} \leftarrow \sigma_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{tc}}{\varepsilon_{tcc}} & \text{if } (\varepsilon_{tcc} > \varepsilon_{tc}) \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rc}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}} & \text{if } \left( \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}} > \varepsilon_{rc} \right) \cdot (A_{BAR} > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{ts}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}}} & \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} < \varepsilon_{ts} \right] \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rs}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}}} & \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}} < \varepsilon_{rs} \right] \cdot (A_{BAR} > 0) \\ \sigma_{cc} & \text{otherwise} \end{cases}$$

$$\sigma_{cd_q} := \sigma_{cd}(\varepsilon_{tcc_q}, q)$$



**CALCULATE FORCES AND MOMENTS AT EACH NEUTRAL AXIS LOCATION**

Calculate force in concrete:

$$F_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from concrete about column centroid:

$$M_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] \cdot y dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in rebar assuming design max stress in concrete:

$$y_{SY_q} := \begin{cases} y_{nbar} \cdot \frac{q}{ns + 1} & \text{if } (f_c = 0) \cdot (A_{BAR} > 0) \\ y_{SY_q} & \text{otherwise} \end{cases}$$

$$\varepsilon_{S_{j,q}} := \begin{cases} \frac{y_{SY_q} - y_{Obar_j}}{y_{nbar} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{if } f_c = 0 \\ \frac{y_{SY_q} - y_{Obar_j}}{H_{CY} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{otherwise} \end{cases}$$

Calculate force in each rebar:

$$F_{S_{j,q}} := \begin{cases} \varepsilon_{S_{j,q}} \cdot E_S \cdot A_{bar_j} & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total force in reinforcement:

$$F_{R_q} := \sum_j F_{S_{j,q}}$$

Calculate moment from reinforcement about section centroid:

$$M_{R_q} := \begin{cases} \sum_j -(\varepsilon_{S_{j,q}} E_S \cdot A_{\text{bar}_j} \cdot y_{\text{bar}_j}) & \text{if } A_{\text{BAR}} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in steel tube at extreme tension fiber:

$$\varepsilon_{\text{tds}_q} := \frac{-(y_{\text{SY}_q} + y_{\text{tt}})}{H_{\text{CY}} - y_{\text{SY}_q}} \varepsilon_{\text{cc}}(f_c, \sigma_{\text{cd}_q})$$

Calculate strain in steel tube at extreme compression fiber:

$$\varepsilon_{\text{tdc}_q} := \frac{y_{\text{tc}} - y_{\text{SY}_q}}{H_{\text{CY}} - y_{\text{SY}_q}} \varepsilon_{\text{cc}}(f_c, \sigma_{\text{cd}_q})$$

Calculate tensile force in steel tube:

$$F_{\text{TS1}_q} := \int_{\left(\frac{H_{\text{CY}}}{2} - y_{\text{SY}_q}\right)}^{\frac{H_{\text{CY}}}{2} + y_{\text{tt}}} 2 \sqrt{\left(\frac{H_{\text{CY}}}{2} + y_{\text{tt}}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{\text{tds}_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{\text{CY}}}{2} - y_{\text{SY}_q} \right) \right]}{y_{\text{SY}_q} + y_{\text{tt}}} \right] dy$$

$$F_{\text{TS2}_q} := \int_{\left(\frac{H_{\text{CY}}}{2} - y_{\text{SY}_q}\right)}^{\frac{H_{\text{CY}}}{2}} 2 \sqrt{\left(\frac{H_{\text{CY}}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{\text{tds}_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{\text{CY}}}{2} - y_{\text{SY}_q} \right) \right]}{y_{\text{SY}_q} + y_{\text{tt}}} \right] dy$$

$$F_{\text{TS}} := \begin{cases} F_{\text{TS1}} - F_{\text{TS2}} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate compressive force in steel tube:

$$F_{\text{TC1}_q} := \int_{-\left(\frac{H_{\text{CY}}}{2} - y_{\text{SY}_q}\right)}^{\frac{H_{\text{CY}}}{2} + y_{\text{tt}}} 2 \sqrt{\left(\frac{H_{\text{CY}}}{2} + y_{\text{tt}}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{\text{tdc}_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{\text{CY}}}{2} - y_{\text{SY}_q} \right) \right]}{H_{\text{CY}} - y_{\text{SY}_q} + y_{\text{tt}}} \right] dy$$

$$F_{TC2_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TC} := \begin{cases} F_{TC1} - F_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from tensile force in steel tube:

$$M_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} -2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} -2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS} := \begin{cases} M_{TS1} - M_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from compressive force in steel tube:

$$M_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC2_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC} := \begin{cases} M_{TC1} - M_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total axial response from section:

$$F_T := F_C + F_R + F_{TS} + F_{TC}$$

$$F_{TC} := F_C$$

Calculate total moment response from section:

$$M_T := M_C + M_R + M_{TS} + M_{TC}$$

$$M_{TC} := M_C$$

**CALCULATE MAXIMUM ALLOWABLE AXIAL FORCE IN SECTION**

Limiting strain in axial  
compression:

$$\varepsilon_{cL} := \begin{cases} \min(\varepsilon_{cc}, \varepsilon_{tc}) & \text{if } (A_{BAR} = 0) \cdot (ts \neq 0) \cdot (f_c \neq 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}) & \text{if } (ts = 0) \cdot (A_{BAR} \neq 0) \cdot (f_c \neq 0) \\ \varepsilon_{tc} & \text{if } (A_{BAR} = 0) \cdot (f_c = 0) \\ \varepsilon_{rc} & \text{if } (ts = 0) \cdot (f_c = 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}, \varepsilon_{tc}) & \text{otherwise} \end{cases} \quad \varepsilon_{cL} = 0.001950$$

Limiting concrete stress in axial compression

$$\sigma_{cL} := \begin{cases} \sigma_{cd2} & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases} \quad \sigma_{cL} = 18.93 \text{ MPa}$$

$$P_{MAX} := \sigma_{cL} \cdot A_C (1 - \rho) + \varepsilon_{cL} \cdot E_S (A_{BAR} + A_{ST})$$

$$P_{MAX} = 26894.6 \text{ kN} \quad F_{T_1} := P_{MAX} \quad M_{T_1} := 0 \cdot \text{kN} \cdot \text{m}$$

$$P_{MAXC} := \sigma_{cL} \cdot A_C \cdot (1 - \rho)$$

$$P_{MAXC} = 17484.9 \text{ kN} \quad F_{TC_1} := P_{MAXC} \quad M_{TC_1} := 0 \cdot \text{kN} \cdot \text{m}$$

**CALCULATE MINIMUM ALLOWABLE AXIAL FORCE IN SECTION**

$$P_{MIN} := \begin{cases} \varepsilon_{rs} \cdot E_S (A_{BAR}) & \text{if } ts = 0 \\ \varepsilon_{ts} \cdot E_S (A_{ST}) & \text{if } A_{BAR} = 0 \\ \max(\varepsilon_{ts}, \varepsilon_{rs}) \cdot E_S (A_{BAR} + A_{ST}) & \text{otherwise} \end{cases}$$

$$P_{MIN} = -4101.7 \text{ kN} \quad F_{T_{ns+1}} := P_{MIN} \quad M_{T_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

$$\text{Limit} := \begin{cases} \min(P, F_T) \cdot 0.75 & \text{if } \min(P) > 0 \\ \min(P, F_T) \cdot 1.25 & \text{otherwise} \end{cases}$$

$$P_{MINC} := 0 \text{ kN} \quad M_{TC_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

Diameter of Column  $D = 1100 \text{ mm}$

Percentage reinforcement  $\rho = 2.55 \%$

Thickness of CHS  $t_s = 0 \text{ mm}$

Characteristic strength of concrete

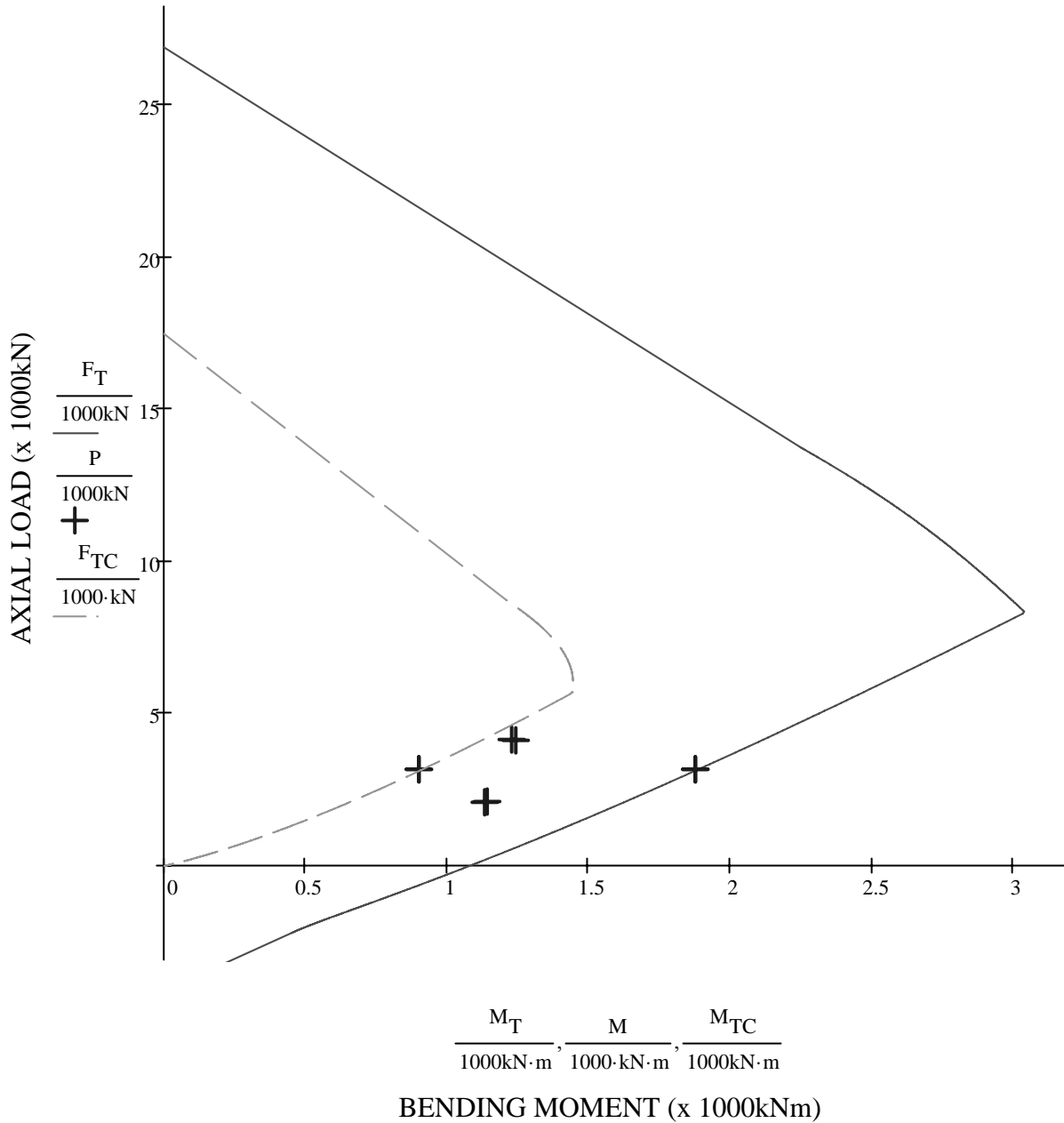
Yield Strength of Rebar

Yield Strength of CHS

$f_c = 30 \text{ MPa}$

$f_y = 390 \text{ MPa}$

$f_{ys} = 250 \text{ MPa}$



INTERACTION CURVE AT SERVICEABILITY LIMIT STATE

Equation of interaction line - upper region (between 1 and 2 calculation points)

$$m1 := \frac{M_{T_2} - M_{T_1}}{F_{T_2} - F_{T_1}} \quad c1 := F_{T_1}$$

Equation of interaction line - lower region (between ns and ns+1 calculation points)

$$m2 := \frac{M_{T_{ns}} - M_{T_{ns+1}}}{F_{T_{ns}} - F_{T_{ns+1}}} \quad c2 := F_{T_{ns+1}}$$

r := 1 .. 8

$$M_{SLS_r} := \begin{cases} 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r > F_{T_1} \\ 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r < F_{T_{ns+1}} \\ (P_r - c1) \cdot m1 & \text{if } (P_r > F_{T_2}) \cdot (P_r \leq F_{T_1}) \\ (P_r - c2) \cdot m2 & \text{if } (P_r \geq F_{T_{ns+1}}) \cdot (P_r < F_{T_{ns}}) \\ \text{otherwise} \\ \quad j \leftarrow 1 \\ \quad \text{while } F_{T_j} > P_r \\ \quad \quad j \leftarrow j + 1 \\ \quad M_{T_j} \end{cases}$$

$$\text{StressFactor}_r := \begin{cases} \text{"No Result"} & \text{if } M_{SLS_r} < 0.000000000000000001 \cdot \text{kN}\cdot\text{m} \\ \frac{M_r}{M_{SLS_r}} & \text{otherwise} \end{cases}$$

$$P = \begin{pmatrix} 3173 \\ 3173 \\ 3178 \\ 3178 \\ 2096 \\ 4131 \\ 2119 \\ 4157 \end{pmatrix} \text{ kN} \quad M = \begin{pmatrix} 1877 \\ 902 \\ 1878 \\ 901 \\ 1133 \\ 1243 \\ 1143 \\ 1229 \end{pmatrix} \text{ kN}\cdot\text{m} \quad M_{SLS} = \begin{pmatrix} 1884.6 \\ 1884.6 \\ 1884.6 \\ 1884.6 \\ 1624.7 \\ 2100.6 \\ 1624.7 \\ 2117.3 \end{pmatrix} \text{ kN}\cdot\text{m} \quad \text{StressFactor} = \begin{pmatrix} 0.996 \\ 0.478 \\ 0.997 \\ 0.478 \\ 0.698 \\ 0.592 \\ 0.703 \\ 0.580 \end{pmatrix}$$

**RESULTS SUMMARY**  
**SERVICEABILITY LIMIT STATE ANALYSIS OF CIRCULAR BEAM COLUMN**

Diameter of Column		1100	mm				
Percentage of rebar		2.55	%				
Load Case Ref	Pier	Applied Service Axial Load kN	Applied Service Bending Moment kNm	Service Limit State Bending Moment kNm	Allowable Stress Factor	Applied Stress Factor	Serviceability Limit State Design Result
1	P21	3173	1877	1884.6	100%	100%	OK
2	P21	3173	902	1884.6	100%	48%	OK
3	P22	3178	1878	1884.6	100%	100%	OK
4	P22	3178	901	1884.6	100%	48%	OK



## **Serviceability Check - Full Live Load**



**KATAHIRA & ENGINEERS  
INTERNATIONAL**

**Project:** Detailed Design Study of  
North Java Corridor Flyover Project

**Calculation:** Balaraja Flyover  
Serviceability Check - Full Live Load  
1100 mm Dia Circular RC Column - P2 Top Section

**Reference:** Project Specific Design Criteria

**Section Data**

MPa := 1000000·Pa

kN := 1000·N

Input Item		
Concrete Compressive Strength	fc	30 MPa
Structural Steel Yield Strength	fys	250 MPa
Rebar Yield Strength	fy	390 MPa
Diameter of reinforced concrete section	D	1100 mm
Thickness of CHS section	t	0 mm
Diameter of rebar - layer 1	dia1	32 mm
Diameter of rebar - layer 2	dia2	0 mm
Number bars - layer 1 (max 100)	n1	30
Number bars - layer 2 (max 100)	n2	0
Cover from face of section - layer 1	cov1	60 mm
Cover from face of section - layer 2	cov2	115 mm

**Load Data**

Ref	Pier	Load Case	P	M	Stress
			kN	kNm	Allowance
1	P21	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+CRSH	3173.2	2269.3	140%
2	P21	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+CRSH	3173.2	1293.4	140%
3	P22	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+CRSH	3177.7	2270.8	140%
4	P22	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+CRSH	3177.7	1293.1	140%

$$f_c := f_c \cdot \text{MPa} \quad f_{ys} := f_{ys} \cdot \text{MPa} \quad f_y := f_y \cdot \text{MPa} \quad D := D \cdot \text{mm} \quad ts := ts \cdot \text{mm}$$

$$\text{dia1} := \text{dia1} \cdot \text{mm} \quad \text{dia2} := \text{dia2} \cdot \text{mm} \quad \text{cov1} := \text{cov1} \cdot \text{mm} \quad \text{cov2} := \text{cov2} \cdot \text{mm}$$

$$P := P \cdot \text{kN} \quad M := M \cdot \text{kN} \cdot \text{m}$$

$$E_S := 200000 \cdot \text{MPa} \quad E_C := 4700 \sqrt{\frac{f_c}{\text{MPa}}} \cdot \text{MPa} \quad \text{Modular ratio} \quad \alpha := \begin{cases} \frac{E_S}{E_C} & \text{if } E_C > 0 \\ 1 & \text{otherwise} \end{cases} \quad \alpha = 7.77$$

$$E_C = 25743 \text{ MPa}$$

### Calculate Basic Allowable Stresses

Calculate rupture stress:

$$\sigma_{ct} := 0.5 \cdot \left( \frac{f_c}{\text{MPa}} \right)^{\frac{2}{3}} \cdot \text{MPa} \quad \sigma_{ct} = 4.8 \text{ MPa}$$

Calculate basic allowable stress of concrete

$$\sigma_{cc} := 1.0 \cdot f_c \quad \sigma_{cc} = 30.0 \text{ MPa}$$

Calculate basic allowable tensile stress of rebar

$$\sigma_{rs} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 170 \text{ MPa} \\ 170 \text{ MPa} & \text{otherwise} \end{cases} \quad \sigma_{rs} = 170 \text{ MPa}$$

Calculate basic allowable compressive stress of rebar

$$\sigma_{rc} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 110 \text{ MPa} \\ f_y & \text{otherwise} \end{cases} \quad \sigma_{rc} = 390 \text{ MPa}$$

Calculate basic allowable stress of structural steel

$$\sigma_{ts} := -0.6 f_{ys} \quad \sigma_{ts} = -150 \text{ MPa}$$

$$\sigma_{tc} := 1 f_{ys} \quad \sigma_{tc} = 250 \text{ MPa}$$

Limiting strain of rebar

$$\epsilon_{rs} := -\frac{\sigma_{rs}}{E_S} \quad \epsilon_{rs} = -0.000850$$

$$\epsilon_{rc} := \frac{\sigma_{rc}}{E_S} \quad \epsilon_{rc} = 0.001950$$

Limiting strain of structural steel

$$\epsilon_{ts} := \frac{\sigma_{ts}}{E_S} \quad \epsilon_{ts} = -0.000750$$

$$\epsilon_{tc} := \frac{\sigma_{tc}}{E_S} \quad \epsilon_{tc} = 0.001250$$

### Concrete Cross Section Data - generated

n := 50      Number of Points - 50 points maximum

i := 1 .. n + 1      Range from 1 to n+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	550
2	-69	-546	27	69	546
3	-137	-533	28	137	533
4	-202	-511	29	202	511
5	-265	-482	30	265	482
6	-323	-445	31	323	445
7	-377	-401	32	377	401
8	-424	-351	33	424	351
9	-464	-295	34	464	295
10	-498	-234	35	498	234
11	-523	-170	36	523	170
12	-540	-103	37	540	103
13	-549	-35	38	549	35
14	-549	35	39	549	-35
15	-540	103	40	540	-103
16	-523	170	41	523	-170
17	-498	234	42	498	-234
18	-464	295	43	464	-295
19	-424	351	44	424	-351
20	-377	401	45	377	-401
21	-323	445	46	323	-445
22	-265	482	47	265	-482
23	-202	511	48	202	-511
24	-137	533	49	137	-533
25	-69	546	50	69	-546

k := 1 .. 25      XS1 := XS1·mm    XS2 := XS2·mm    YS1 := YS1·mm    YS2 := YS2·mm

$x_k := XS1_k$        $y_k := YS1_k$        $x_{k+25} := XS2_k$        $y_{k+25} := YS2_k$        $x_{n+1} := XS1_1$        $y_{n+1} := YS1_1$

### Calculate Section Properties of Concrete Section

$$A_C := - \sum_{i=1}^n \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{2} \right] \quad A_C = 0.94783 \text{ m}^2$$

$$x_C := - \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{y_{i+1} - y_i}{8} \cdot \left[ (x_{i+1} + x_i)^2 + \frac{(x_{i+1} - x_i)^2}{3} \right] \right] \quad x_C = 0 \text{ m}$$

$$y_C := \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{x_{i+1} - x_i}{8} \cdot \left[ (y_{i+1} + y_i)^2 + \frac{(y_{i+1} - y_i)^2}{3} \right] \right] \quad y_C = 0 \text{ m}$$

$$I_x := \sum_{i=1}^n \left[ \left[ (x_{i+1} - x_i) \cdot \frac{y_{i+1} + y_i}{24} \right] \cdot \left[ (y_{i+1} + y_i)^2 + (y_{i+1} - y_i)^2 \right] \right] \quad I_x = 0.07149 \text{ m}^4$$

$$I_y := - \sum_{i=1}^n \left[ \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{24} \right] \cdot \left[ (x_{i+1} + x_i)^2 + (x_{i+1} - x_i)^2 \right] \right] \quad I_y = 0.07149 \text{ m}^4$$

$$I_{xC} := I_x - A_C \cdot x_C^2 \quad I_{xC} = 0.07149 \text{ m}^4$$

$$I_{yC} := I_y - A_C \cdot y_C^2 \quad I_{yC} = 0.07149 \text{ m}^4$$

### Steel Tube Cross Section Data - generated from input

ns := 50      Number of Points - 50 points maximum

ps := 1 .. ns + 1      Range from 1 to ns+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	-550
2	-142	-531	27	142	-531
3	-275	-476	28	275	-476
4	-389	-389	29	389	-389
5	-476	-275	30	476	-275
6	-531	-142	31	531	-142
7	-550	0	32	550	0
8	-531	142	33	531	142
9	-476	275	34	476	275
10	-389	389	35	389	389
11	-275	476	36	275	476
12	-142	531	37	142	531
13	0	550	38	0	550
14	142	531	39	-142	531
15	275	476	40	-275	476
16	389	389	41	-389	389
17	476	275	42	-476	275
18	531	142	43	-531	142
19	550	0	44	-550	0
20	531	-142	45	-531	-142
21	476	-275	46	-476	-275
22	389	-389	47	-389	-389
23	275	-476	48	-275	-476
24	142	-531	49	-142	-531
25	0	-550	50	0	-550

$$XSS1 := XSS1 \cdot \text{mm}$$

$$XSS2 := XSS2 \cdot \text{mm}$$

$$YSS1 := YSS1 \cdot \text{mm}$$

$$YSS2 := YSS2 \cdot \text{mm}$$

$$z := 1 .. 25$$

$$xs_z := XSS1_z$$

$$ys_z := YSS1_z$$

$$z := 26 .. 50$$

$$xs_z := XSS2_{z-25}$$

$$ys_z := YSS2_{z-25}$$

$$xs_{ns+1} := XSS1_1$$

$$ys_{ns+1} := YSS1_1$$

**Calculate Section Properties of Steel Tube Section**

$$A_{ST} := - \sum_{ps=1}^{ns} \left[ (y_{ps+1}^s - y_{ps}^s) \cdot \frac{x_{ps+1}^s + x_{ps}^s}{2} \right] \quad A_{ST} = 0 \text{ m}^2$$

$$x_{ST} := - \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{y_{ps+1}^s - y_{ps}^s}{8} \cdot \left[ (x_{ps+1}^s + x_{ps}^s)^2 + \frac{(x_{ps+1}^s - x_{ps}^s)^2}{3} \right] \right] \quad x_{ST} = 0.2 \text{ m}$$

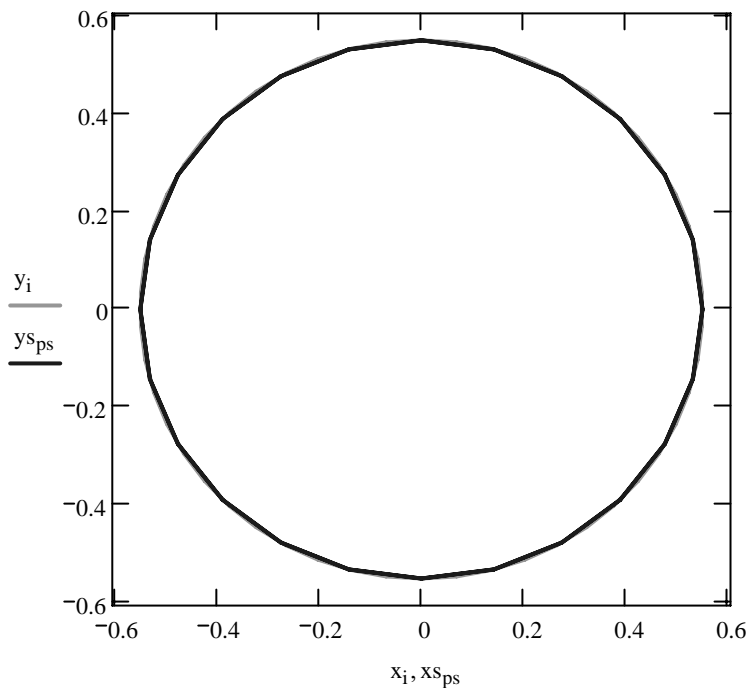
$$y_{ST} := \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{x_{ps+1}^s - x_{ps}^s}{8} \cdot \left[ (y_{ps+1}^s + y_{ps}^s)^2 + \frac{(y_{ps+1}^s - y_{ps}^s)^2}{3} \right] \right] \quad y_{ST} = -0.011 \text{ m}$$

$$I_{xS} := \sum_{ps=1}^{ns} \left[ \left[ (x_{ps+1}^s - x_{ps}^s) \cdot \frac{y_{ps+1}^s + y_{ps}^s}{24} \right] \cdot \left[ (y_{ps+1}^s + y_{ps}^s)^2 + (y_{ps+1}^s - y_{ps}^s)^2 \right] \right] \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := - \sum_{ps=1}^{ns} \left[ \left[ (y_{ps+1}^s - y_{ps}^s) \cdot \frac{x_{ps+1}^s + x_{ps}^s}{24} \right] \cdot \left[ (x_{ps+1}^s + x_{ps}^s)^2 + (x_{ps+1}^s - x_{ps}^s)^2 \right] \right] \quad I_{yS} = 0 \text{ m}^4$$

$$I_{xS} := I_{xS} - A_{ST} \cdot x_{ST}^2 \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := I_{yS} - A_{ST} \cdot y_{ST}^2 \quad I_{yS} = 0.00000 \text{ m}^4$$



**Rebar Data Layer 1 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	804	0	-474	51	0	0	0
2	804	-99	-464	52	0	0	0
3	804	-193	-433	53	0	0	0
4	804	-279	-383	54	0	0	0
5	804	-352	-317	55	0	0	0
6	804	-410	-237	56	0	0	0
7	804	-451	-146	57	0	0	0
8	804	-471	-50	58	0	0	0
9	804	-471	50	59	0	0	0
10	804	-451	146	60	0	0	0
11	804	-410	237	61	0	0	0
12	804	-352	317	62	0	0	0
13	804	-279	383	63	0	0	0
14	804	-193	433	64	0	0	0
15	804	-99	464	65	0	0	0
16	804	0	474	66	0	0	0
17	804	99	464	67	0	0	0
18	804	193	433	68	0	0	0
19	804	279	383	69	0	0	0
20	804	352	317	70	0	0	0
21	804	410	237	71	0	0	0
22	804	451	146	72	0	0	0
23	804	471	50	73	0	0	0
24	804	471	-50	74	0	0	0
25	804	451	-146	75	0	0	0
26	804	410	-237	76	0	0	0
27	804	352	-317	77	0	0	0
28	804	279	-383	78	0	0	0
29	804	193	-433	79	0	0	0
30	804	99	-464	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0



**Rebar Data Layer 2 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	0	0	0	51	0	0	0
2	0	0	0	52	0	0	0
3	0	0	0	53	0	0	0
4	0	0	0	54	0	0	0
5	0	0	0	55	0	0	0
6	0	0	0	56	0	0	0
7	0	0	0	57	0	0	0
8	0	0	0	58	0	0	0
9	0	0	0	59	0	0	0
10	0	0	0	60	0	0	0
11	0	0	0	61	0	0	0
12	0	0	0	62	0	0	0
13	0	0	0	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

$$A1 := A1 \cdot \text{mm}^2 \quad A2 := A2 \cdot \text{mm}^2 \quad A3 := A3 \cdot \text{mm}^2 \quad A4 := A4 \cdot \text{mm}^2$$

$$X1 := X1 \cdot \text{mm} \quad X2 := X2 \cdot \text{mm} \quad X3 := X3 \cdot \text{mm} \quad X4 := X4 \cdot \text{mm}$$

$$Y1 := Y1 \cdot \text{mm} \quad Y2 := Y2 \cdot \text{mm} \quad Y3 := Y3 \cdot \text{mm} \quad Y4 := Y4 \cdot \text{mm}$$

$$k := 1..50$$

$$A_{\text{bar}_k} := A1_k \quad x_{\text{bar}_k} := X1_k \quad y_{\text{bar}_k} := Y1_k$$

$$A_{\text{bar}_{k+50}} := A2_k \quad x_{\text{bar}_{k+50}} := X2_k \quad y_{\text{bar}_{k+50}} := Y2_k$$

$$A_{\text{bar}_{k+100}} := A3_k \quad x_{\text{bar}_{k+100}} := X3_k \quad y_{\text{bar}_{k+100}} := Y3_k$$

$$A_{\text{bar}_{k+150}} := A4_k \quad x_{\text{bar}_{k+150}} := X4_k \quad y_{\text{bar}_{k+150}} := Y4_k$$

### Calculate Section Properties of Reinforcement

$$A_{\text{BAR}} := \sum_{j=1}^{200} A_{\text{bar}_j} \quad A_{\text{BAR}} = 24127 \text{ mm}^2$$

$$\rho := \frac{A_{\text{BAR}}}{A_C} \quad \rho = 0.0255$$

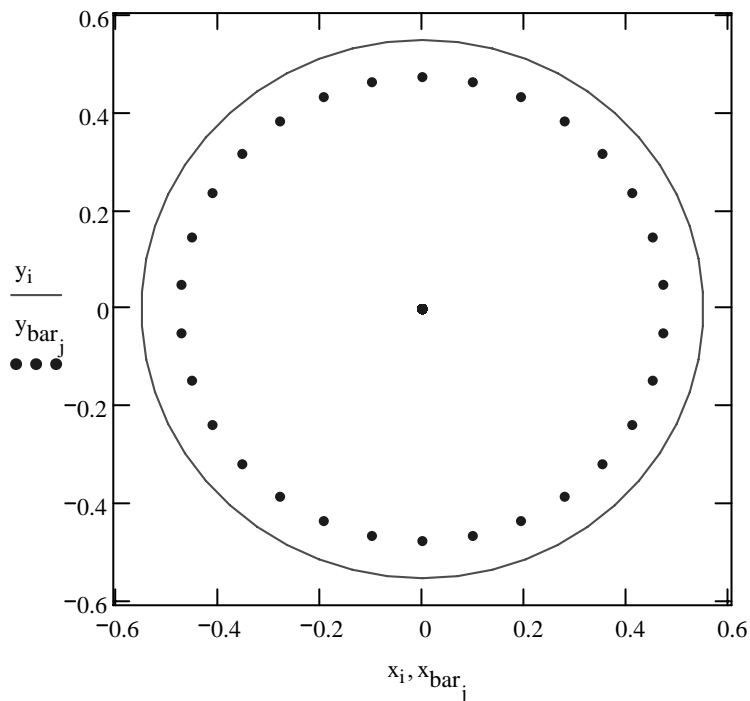
$$x_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot x_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad x_b = 0 \text{ m}$$

$$y_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot y_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad y_b = 0 \text{ m}$$

$$I_{x_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (x_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot x_b^2 \quad I_{x_b} = 0.00271 \text{ m}^4$$

$$I_{y_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (y_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot y_b^2 \quad I_{y_b} = 0.00271 \text{ m}^4$$

$j := 1 .. 200$



**Calculate Composite Section Properties (before cracking)**

Effective area  $A_E := A_C \cdot [1 + \rho \cdot (\alpha - 1)] + A_{ST} \cdot \alpha$   $A_E = 1111154 \text{ mm}^2$

Effective centroid  $x_E := \frac{A_C \cdot [(1 - \rho) \cdot x_C + \rho \cdot x_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot x_{ST}}{A_E}$   $x_E = 0.000 \text{ m}$

$y_E := \frac{A_C \cdot [(1 - \rho) \cdot y_C + \rho \cdot y_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot y_{ST}}{A_E}$   $y_E = 0.000 \text{ m}$

Effective stiffness  $I_{EX} := I_{xC} + I_{xb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot x_C^2 + \rho \cdot x_b^2 \cdot \alpha] + (I_{xS} + A_{ST} \cdot x_{ST}^2) \cdot \alpha$   
 $I_{EX} = 0 \text{ m}^4$

$I_{EY} := I_{yC} + I_{yb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot y_C^2 + \rho \cdot y_b^2 \cdot \alpha] + (I_{yS} + A_{ST} \cdot y_{ST}^2) \cdot \alpha$   
 $I_{EY} = 0 \text{ m}^4$

Distance from extreme concrete fiber to centroid

$x_{F_{pos}} := \max(x - x_E)$   $x_{F_{neg}} := \min(x - x_E)$

$y_{F_{pos}} := \max(y - y_E)$   $y_{F_{neg}} := \min(y - y_E)$

Total depth of concrete section

$H_{CX} := x_{F_{pos}} - x_{F_{neg}}$   $H_{CX} = 1 \text{ m}$

$H_{CY} := y_{F_{pos}} - y_{F_{neg}}$   $H_{CY} = 1 \text{ m}$

Section modulus

$$Z_{Xpos} := \frac{I_{EX}}{xF_{pos}}$$

$$Z_{Xneg} := \frac{I_{EX}}{xF_{neg}}$$

$$Z_{Ypos} := \frac{I_{EY}}{yF_{pos}}$$

$$Z_{Yneg} := \frac{I_{EY}}{yF_{neg}}$$

Thickness of steel tube:

$$ts := y_1 - ys_1$$

$$ts = 0 \text{ mm}$$

**Establish Section Dimensions**

Positive case - determine coord of extreme concrete fiber

$$y_{Epos} := \max(y)$$

$$y_{Epos} = 550 \text{ mm}$$

Negative case - determine coord of extreme concrete fiber

$$y_{Eneg} := \min(y)$$

$$y_{Eneg} = -550 \text{ mm}$$

Offsets of rebar from extreme fiber

$$y_{Obar} := y_{Epos} - y_{bar}$$

Determine most extreme rebar (minimum offset)

$$y_{1bar} := \min(y_{Epos} - y_{bar})$$

$$y_{1bar} = 76 \text{ mm}$$

Determine most extreme rebar (maximum offset)

$$y_{nbar} := \max(y_{Epos} - y_{bar})$$

$$y_{nbar} = 1024 \text{ mm}$$

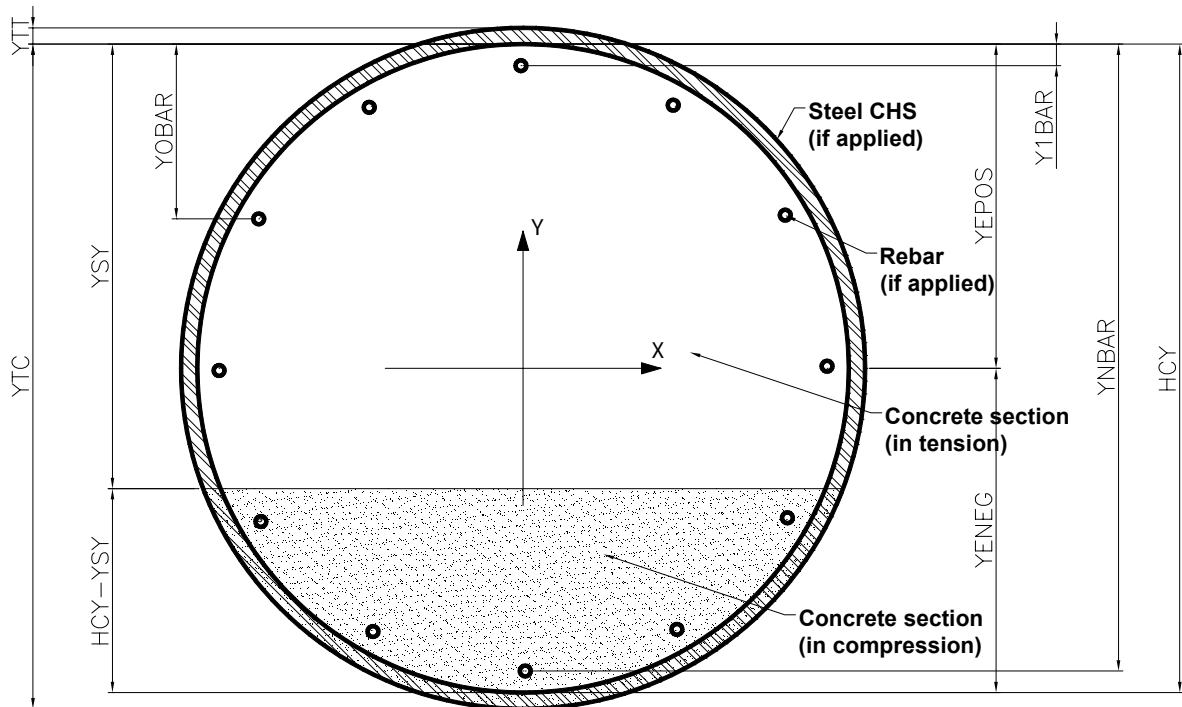
Offsets of extreme steel tube fiber from extreme concrete fiber

$$y_{tt} := ts$$

$$y_{tt} = 0 \text{ mm}$$

$$y_{tc} := H_{CY} + ts$$

$$y_{tc} = 1100 \text{ mm}$$



**ASSIGN NEUTRAL AXIS VALUES**

Number of sections to analysed                      ns := 500

q := 2 .. ns

Distance of neutral axis from extreme fiber in tension                       $y_{SY_q} := H_{CY} \cdot \frac{q}{ns + 1}$

**Calculate stresses and strains in reinforcement and concrete at extreme fibers**

Calculate strain at extreme compression fiber assuming max allowable stress in concrete:

Trial value of concrete strain

$$\epsilon_{cc} := \frac{\sigma_{cc}}{E_C} \cdot 2 \qquad \frac{\sigma_{cc}}{E_C} = 0.001165$$

Given

$$\sigma_{cc} = \epsilon_{cc} \cdot \left( 4700 \sqrt{\frac{f_c \cdot 2}{\text{MPa}}} - \frac{4700^2}{2.68} \cdot \epsilon_{cc} \right) \cdot \text{MPa}$$

$$\epsilon_{cc} := \text{Find}(\epsilon_{cc}) \qquad \epsilon_{cc} = 0.003321$$

$$\epsilon_{cc} := \begin{cases} \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \epsilon_{cc} & \text{otherwise} \end{cases} \qquad \epsilon_{cc} = 0.003321$$

Strain at other stresses taken to be linear:

$$\epsilon_{cc}(f_c, \sigma_{cd}) := \begin{cases} \frac{\sigma_{cd}}{\sigma_{tc}} \cdot \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \frac{\sigma_{cd}}{\sigma_{rc}} \cdot \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \frac{\sigma_{cd}}{\sigma_{cc}} \cdot \epsilon_{cc} & \text{otherwise} \end{cases}$$

Calculate strain in steel tube assuming max allowable stress in concrete:

$$\begin{aligned} \text{In compression} \quad \epsilon_{tcc_q} &:= \epsilon_{cc} \cdot \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \\ \text{In tension} \quad \epsilon_{tct_q} &:= \epsilon_{cc} \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \end{aligned}$$

Calculate strain in rebar assuming max allowable stress in concrete:

$$\begin{array}{l} \text{In} \\ \text{compression} \end{array} \quad \varepsilon_{rcc_q} := \varepsilon_{cc} \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

$$\begin{array}{l} \text{In} \\ \text{tension} \end{array} \quad \varepsilon_{rct_q} := \varepsilon_{cc} \cdot \frac{y_{1bar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

Calculate design max stress in compression taking account of other limits:

$$\sigma_{cd}(\varepsilon_{tcc}, q) := \left\{ \begin{array}{l} \sigma_{cd} \leftarrow \sigma_{cc} \quad \text{if } f_c > 0 \\ \sigma_{cd} \leftarrow \sigma_{tc} \quad \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \sigma_{cd} \leftarrow \sigma_{rc} \quad \text{if } (f_c = 0) \cdot (ts = 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{tc}}{\varepsilon_{tcc}} \quad \text{if } (\varepsilon_{tcc} > \varepsilon_{tc}) \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rc}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}} \quad \text{if } \left( \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}} > \varepsilon_{rc} \right) \cdot (A_{BAR} > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{ts}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}}} \quad \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} < \varepsilon_{ts} \right] \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rs}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}}} \quad \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}} < \varepsilon_{rs} \right] \cdot (A_{BAR} > 0) \\ \sigma_{cc} \quad \text{otherwise} \end{array} \right.$$

$$\sigma_{cd_q} := \sigma_{cd}(\varepsilon_{tcc_q}, q)$$

**CALCULATE FORCES AND MOMENTS AT EACH NEUTRAL AXIS LOCATION**

Calculate force in concrete:

$$F_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from concrete about column centroid:

$$M_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] \cdot y dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in rebar assuming design max stress in concrete:

$$y_{SY_q} := \begin{cases} y_{nbar} \cdot \frac{q}{ns + 1} & \text{if } (f_c = 0) \cdot (A_{BAR} > 0) \\ y_{SY_q} & \text{otherwise} \end{cases}$$

$$\varepsilon_{S_{j,q}} := \begin{cases} \frac{y_{SY_q} - y_{Obar_j}}{y_{nbar} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{if } f_c = 0 \\ \frac{y_{SY_q} - y_{Obar_j}}{H_{CY} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{otherwise} \end{cases}$$

Calculate force in each rebar:

$$F_{S_{j,q}} := \begin{cases} \varepsilon_{S_{j,q}} \cdot E_S \cdot A_{bar_j} & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total force in reinforcement:

$$F_{R_q} := \sum_j F_{S_{j,q}}$$

Calculate moment from reinforcement about section centroid:

$$M_{R_q} := \begin{cases} \sum_j -(\varepsilon_{S_{j,q}} E_S A_{bar_j} y_{bar_j}) & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in steel tube at extreme tension fiber:

$$\varepsilon_{tds_q} := \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate strain in steel tube at extreme compression fiber:

$$\varepsilon_{tdc_q} := \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate tensile force in steel tube:

$$F_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS} := \begin{cases} F_{TS1} - F_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate compressive force in steel tube:

$$F_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$



$$F_{TC2q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] dy$$

$$F_{TC} := \begin{cases} F_{TC1} - F_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from tensile force in steel tube:

$$M_{TS1q} := \int_{\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2} + y_{tt}} -2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS2q} := \int_{\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} -2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS} := \begin{cases} M_{TS1} - M_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from compressive force in steel tube:

$$M_{TC1q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC2q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC} := \begin{cases} M_{TC1} - M_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total axial response from section:

$$F_T := F_C + F_R + F_{TS} + F_{TC}$$

$$F_{TC} := F_C$$

Calculate total moment response from section:

$$M_T := M_C + M_R + M_{TS} + M_{TC}$$

$$M_{TC} := M_C$$

**CALCULATE MAXIMUM ALLOWABLE AXIAL FORCE IN SECTION**

Limiting strain in axial  
compression:

$$\varepsilon_{cL} := \begin{cases} \min(\varepsilon_{cc}, \varepsilon_{tc}) & \text{if } (A_{BAR} = 0) \cdot (ts \neq 0) \cdot (f_c \neq 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}) & \text{if } (ts = 0) \cdot (A_{BAR} \neq 0) \cdot (f_c \neq 0) \\ \varepsilon_{tc} & \text{if } (A_{BAR} = 0) \cdot (f_c = 0) \\ \varepsilon_{rc} & \text{if } (ts = 0) \cdot (f_c = 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}, \varepsilon_{tc}) & \text{otherwise} \end{cases} \quad \varepsilon_{cL} = 0.001950$$

Limiting concrete stress in axial compression

$$\sigma_{cL} := \begin{cases} \sigma_{cd2} & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases} \quad \sigma_{cL} = 18.93 \text{ MPa}$$

$$P_{MAX} := \sigma_{cL} \cdot A_C (1 - \rho) + \varepsilon_{cL} \cdot E_S (A_{BAR} + A_{ST})$$

$$P_{MAX} = 26894.6 \text{ kN} \quad F_{T_1} := P_{MAX} \quad M_{T_1} := 0 \cdot \text{kN} \cdot \text{m}$$

$$P_{MAXC} := \sigma_{cL} \cdot A_C \cdot (1 - \rho)$$

$$P_{MAXC} = 17484.9 \text{ kN} \quad F_{TC_1} := P_{MAXC} \quad M_{TC_1} := 0 \cdot \text{kN} \cdot \text{m}$$

**CALCULATE MINIMUM ALLOWABLE AXIAL FORCE IN SECTION**

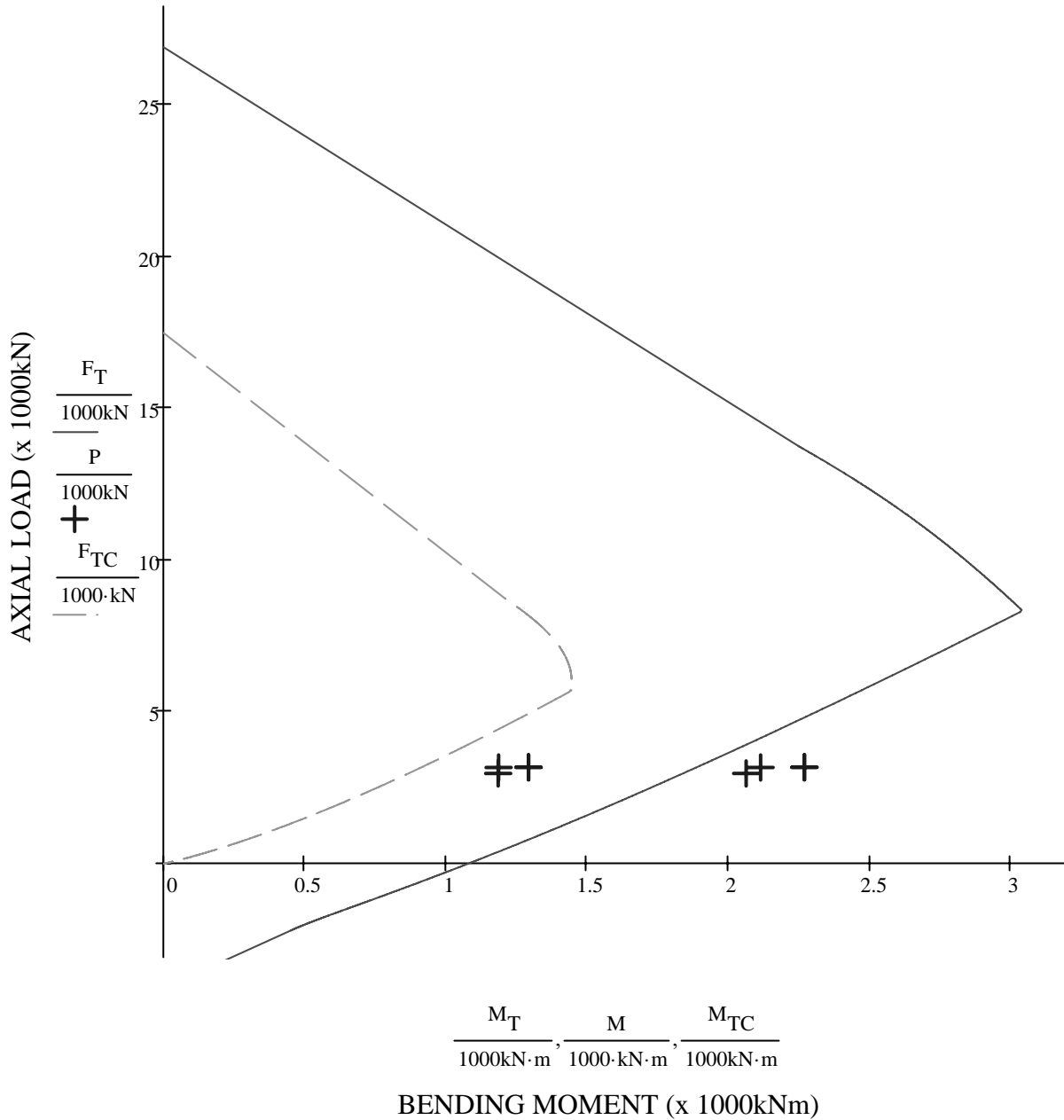
$$P_{MIN} := \begin{cases} \varepsilon_{rs} \cdot E_S (A_{BAR}) & \text{if } ts = 0 \\ \varepsilon_{ts} \cdot E_S (A_{ST}) & \text{if } A_{BAR} = 0 \\ \max(\varepsilon_{ts}, \varepsilon_{rs}) \cdot E_S (A_{BAR} + A_{ST}) & \text{otherwise} \end{cases}$$

$$P_{MIN} = -4101.7 \text{ kN} \quad F_{T_{ns+1}} := P_{MIN} \quad M_{T_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

$$\text{Limit} := \begin{cases} \min(P, F_T) \cdot 0.75 & \text{if } \min(P) > 0 \\ \min(P, F_T) \cdot 1.25 & \text{otherwise} \end{cases}$$

$$P_{MINC} := 0 \text{ kN} \quad M_{TC_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

Diameter of Column	D = 1100 mm	Characteristic strength of concrete	$f_c = 30 \text{ MPa}$
Percentage reinforcement	$\rho = 2.55 \%$	Yield Strength of Rebar	$f_y = 390 \text{ MPa}$
Thickness of CHS	$t_s = 0 \text{ mm}$	Yield Strength of CHS	$f_{ys} = 250 \text{ MPa}$



**INTERACTION CURVE AT SERVICEABILITY LIMIT STATE**

Equation of interaction line - upper region (between 1 and 2 calculation points)

$$m1 := \frac{M_{T_2} - M_{T_1}}{F_{T_2} - F_{T_1}} \quad c1 := F_{T_1}$$

Equation of interaction line - lower region (between ns and ns+1 calculation points)

$$m2 := \frac{M_{T_{ns}} - M_{T_{ns+1}}}{F_{T_{ns}} - F_{T_{ns+1}}} \quad c2 := F_{T_{ns+1}}$$

r := 1 .. 8

$$M_{SLS_r} := \begin{cases} 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r > F_{T_1} \\ 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r < F_{T_{ns+1}} \\ (P_r - c1) \cdot m1 & \text{if } (P_r > F_{T_2}) \cdot (P_r \leq F_{T_1}) \\ (P_r - c2) \cdot m2 & \text{if } (P_r \geq F_{T_{ns+1}}) \cdot (P_r < F_{T_{ns}}) \\ \text{otherwise} \\ \quad j \leftarrow 1 \\ \quad \text{while } F_{T_j} > P_r \\ \quad \quad j \leftarrow j + 1 \\ \quad M_{T_j} \end{cases}$$

$$\text{StressFactor}_r := \begin{cases} \text{"No Result"} & \text{if } M_{SLS_r} < 0.00000000000000001 \cdot \text{kN}\cdot\text{m} \\ \frac{M_r}{M_{SLS_r}} & \text{otherwise} \end{cases}$$

$$P = \begin{pmatrix} 3173 \\ 3173 \\ 3178 \\ 3178 \\ 2974 \\ 2974 \\ 3172 \\ 3172 \end{pmatrix} \text{ kN} \quad M = \begin{pmatrix} 2269 \\ 1293 \\ 2271 \\ 1293 \\ 2063 \\ 1186 \\ 2115 \\ 1187 \end{pmatrix} \text{ kN}\cdot\text{m} \quad M_{SLS} = \begin{pmatrix} 1884.6 \\ 1884.6 \\ 1884.6 \\ 1884.6 \\ 1828.4 \\ 1828.4 \\ 1884.6 \\ 1884.6 \end{pmatrix} \text{ kN}\cdot\text{m} \quad \text{StressFactor} = \begin{pmatrix} 1.204 \\ 0.686 \\ 1.205 \\ 0.686 \\ 1.129 \\ 0.649 \\ 1.122 \\ 0.630 \end{pmatrix}$$

**RESULTS SUMMARY**  
**SERVICEABILITY LIMIT STATE ANALYSIS OF CIRCULAR BEAM COLUMN**

Diameter of Column		1100	mm				
Percentage of rebar		2.55	%				
Load Case Ref	Pier	Applied Service Axial Load kN	Applied Service Bending Moment kNm	Service Limit State Bending Moment kNm	Allowable Stress Factor	Applied Stress Factor	Serviceability Limit State Design Result
1	P21	3173	2269	1884.6	140%	120%	OK
2	P21	3173	1293	1884.6	140%	69%	OK
3	P22	3178	2271	1884.6	140%	120%	OK
4	P22	3178	1293	1884.6	140%	69%	OK

**BASE**

## **Serviceability Check - Traffic Load Only**





**KATAHIRA & ENGINEERS  
INTERNATIONAL**

**Project:** Detailed Design Study of  
North Java Corridor Flyover Project

**Calculation:** Balaraja Flyover  
Serviceability Check - Traffic Load Only  
1100 mm Dia Circular RC Column - P2 Base Section

**Reference:** Project Specific Design Criteria

**Section Data**

MPa := 1000000·Pa

kN := 1000·N

Input Item		
Concrete Compressive Strength	fc	30 MPa
Structural Steel Yield Strength	fys	250 MPa
Rebar Yield Strength	fy	390 MPa
Diameter of reinforced concrete section	D	1100 mm
Thickness of CHS section	t	0 mm
Diameter of rebar - layer 1	dia1	32 mm
Diameter of rebar - layer 2	dia2	0 mm
Number bars - layer 1 (max 100)	n1	12
Number bars - layer 2 (max 100)	n2	0
Cover from face of section - layer 1	cov1	60 mm
Cover from face of section - layer 2	cov2	115 mm

**Load Data**

Ref	Pier	Load Case	P	M	Stress
			kN	kNm	Allowance
1	P21	Combination 1 - P + Traffic Load Only	3336.8	70.0	100%
2	P21	Combination 1 - P + Traffic Load Only	3336.8	322.1	100%
3	P22	Combination 1 - P + Traffic Load Only	3341.4	69.5	100%
4	P22	Combination 1 - P + Traffic Load Only	3341.4	322.6	100%

$$f_c := f_c \cdot \text{MPa} \quad f_{ys} := f_{ys} \cdot \text{MPa} \quad f_y := f_y \cdot \text{MPa} \quad D := D \cdot \text{mm} \quad ts := ts \cdot \text{mm}$$

$$\text{dia1} := \text{dia1} \cdot \text{mm} \quad \text{dia2} := \text{dia2} \cdot \text{mm} \quad \text{cov1} := \text{cov1} \cdot \text{mm} \quad \text{cov2} := \text{cov2} \cdot \text{mm}$$

$$P := P \cdot \text{kN} \quad M := M \cdot \text{kN} \cdot \text{m}$$

$$E_S := 200000 \cdot \text{MPa} \quad E_C := 4700 \sqrt{\frac{f_c}{\text{MPa}}} \cdot \text{MPa} \quad \text{Modular ratio} \quad \alpha := \begin{cases} \frac{E_S}{E_C} & \text{if } E_C > 0 \\ 1 & \text{otherwise} \end{cases} \quad \alpha = 7.77$$

$$E_C = 25743 \text{ MPa}$$

### Calculate Basic Allowable Stresses

Calculate rupture stress:

$$\sigma_{ct} := 0.5 \cdot \left( \frac{f_c}{\text{MPa}} \right)^{\frac{2}{3}} \cdot \text{MPa} \quad \sigma_{ct} = 4.8 \text{ MPa}$$

Calculate basic allowable stress of concrete

$$\sigma_{cc} := 1.0 \cdot f_c \quad \sigma_{cc} = 30.0 \text{ MPa}$$

Calculate basic allowable tensile stress of rebar

$$\sigma_{rs} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 170 \text{ MPa} \\ 170 \text{ MPa} & \text{otherwise} \end{cases} \quad \sigma_{rs} = 170 \text{ MPa}$$

Calculate basic allowable compressive stress of rebar

$$\sigma_{rc} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 110 \text{ MPa} \\ f_y & \text{otherwise} \end{cases} \quad \sigma_{rc} = 390 \text{ MPa}$$

Calculate basic allowable stress of structural steel

$$\sigma_{ts} := -0.6 f_{ys} \quad \sigma_{ts} = -150 \text{ MPa}$$

$$\sigma_{tc} := 1 f_{ys} \quad \sigma_{tc} = 250 \text{ MPa}$$

Limiting strain of rebar

$$\epsilon_{rs} := -\frac{\sigma_{rs}}{E_S} \quad \epsilon_{rs} = -0.000850$$

$$\epsilon_{rc} := \frac{\sigma_{rc}}{E_S} \quad \epsilon_{rc} = 0.001950$$

Limiting strain of structural steel

$$\epsilon_{ts} := \frac{\sigma_{ts}}{E_S} \quad \epsilon_{ts} = -0.000750$$

$$\epsilon_{tc} := \frac{\sigma_{tc}}{E_S} \quad \epsilon_{tc} = 0.001250$$

### Concrete Cross Section Data - generated

n := 50      Number of Points - 50 points maximum

i := 1 .. n + 1      Range from 1 to n+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	550
2	-69	-546	27	69	546
3	-137	-533	28	137	533
4	-202	-511	29	202	511
5	-265	-482	30	265	482
6	-323	-445	31	323	445
7	-377	-401	32	377	401
8	-424	-351	33	424	351
9	-464	-295	34	464	295
10	-498	-234	35	498	234
11	-523	-170	36	523	170
12	-540	-103	37	540	103
13	-549	-35	38	549	35
14	-549	35	39	549	-35
15	-540	103	40	540	-103
16	-523	170	41	523	-170
17	-498	234	42	498	-234
18	-464	295	43	464	-295
19	-424	351	44	424	-351
20	-377	401	45	377	-401
21	-323	445	46	323	-445
22	-265	482	47	265	-482
23	-202	511	48	202	-511
24	-137	533	49	137	-533
25	-69	546	50	69	-546

k := 1 .. 25      XS1 := XS1·mm    XS2 := XS2·mm    YS1 := YS1·mm    YS2 := YS2·mm

$x_k := XS1_k$        $y_k := YS1_k$        $x_{k+25} := XS2_k$        $y_{k+25} := YS2_k$        $x_{n+1} := XS1_1$        $y_{n+1} := YS1_1$

### Calculate Section Properties of Concrete Section

$$A_C := - \sum_{i=1}^n \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{2} \right] \quad A_C = 0.94783 \text{ m}^2$$

$$x_C := - \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{y_{i+1} - y_i}{8} \cdot \left[ (x_{i+1} + x_i)^2 + \frac{(x_{i+1} - x_i)^2}{3} \right] \right] \quad x_C = 0 \text{ m}$$

$$y_C := \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{x_{i+1} - x_i}{8} \cdot \left[ (y_{i+1} + y_i)^2 + \frac{(y_{i+1} - y_i)^2}{3} \right] \right] \quad y_C = 0 \text{ m}$$

$$I_x := \sum_{i=1}^n \left[ \left[ (x_{i+1} - x_i) \cdot \frac{y_{i+1} + y_i}{24} \right] \cdot \left[ (y_{i+1} + y_i)^2 + (y_{i+1} - y_i)^2 \right] \right] \quad I_x = 0.07149 \text{ m}^4$$

$$I_y := - \sum_{i=1}^n \left[ \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{24} \right] \cdot \left[ (x_{i+1} + x_i)^2 + (x_{i+1} - x_i)^2 \right] \right] \quad I_y = 0.07149 \text{ m}^4$$

$$I_{xC} := I_x - A_C \cdot x_C^2 \quad I_{xC} = 0.07149 \text{ m}^4$$

$$I_{yC} := I_y - A_C \cdot y_C^2 \quad I_{yC} = 0.07149 \text{ m}^4$$

### Steel Tube Cross Section Data - generated from input

ns := 50      Number of Points - 50 points maximum

ps := 1 .. ns + 1      Range from 1 to ns+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	-550
2	-142	-531	27	142	-531
3	-275	-476	28	275	-476
4	-389	-389	29	389	-389
5	-476	-275	30	476	-275
6	-531	-142	31	531	-142
7	-550	0	32	550	0
8	-531	142	33	531	142
9	-476	275	34	476	275
10	-389	389	35	389	389
11	-275	476	36	275	476
12	-142	531	37	142	531
13	0	550	38	0	550
14	142	531	39	-142	531
15	275	476	40	-275	476
16	389	389	41	-389	389
17	476	275	42	-476	275
18	531	142	43	-531	142
19	550	0	44	-550	0
20	531	-142	45	-531	-142
21	476	-275	46	-476	-275
22	389	-389	47	-389	-389
23	275	-476	48	-275	-476
24	142	-531	49	-142	-531
25	0	-550	50	0	-550

XSS1 := XSS1·mm      XSS2 := XSS2·mm      YSS1 := YSS1·mm      YSS2 := YSS2·mm

z := 1 .. 25       $xs_z := XSS1_z$        $ys_z := YSS1_z$

z := 26 .. 50       $xs_z := XSS2_{z-25}$        $ys_z := YSS2_{z-25}$

$xs_{ns+1} := XSS1_1$        $ys_{ns+1} := YSS1_1$

**Calculate Section Properties of Steel Tube Section**

$$A_{ST} := - \sum_{ps=1}^{ns} \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{2} \right] \quad A_{ST} = 0 \text{ m}^2$$

$$x_{ST} := - \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{y_{ps+1}^{s} - y_{ps}^{s}}{8} \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + \frac{(x_{ps+1}^{s} - x_{ps}^{s})^2}{3} \right] \right] \quad x_{ST} = 0.2 \text{ m}$$

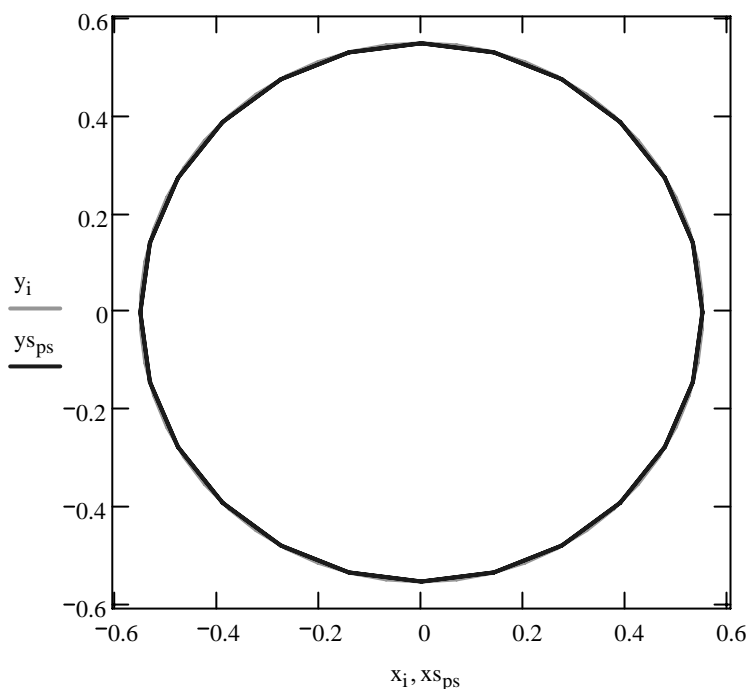
$$y_{ST} := \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{x_{ps+1}^{s} - x_{ps}^{s}}{8} \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + \frac{(y_{ps+1}^{s} - y_{ps}^{s})^2}{3} \right] \right] \quad y_{ST} = -0.011 \text{ m}$$

$$I_{xS} := \sum_{ps=1}^{ns} \left[ \left[ (x_{ps+1}^{s} - x_{ps}^{s}) \cdot \frac{y_{ps+1}^{s} + y_{ps}^{s}}{24} \right] \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + (y_{ps+1}^{s} - y_{ps}^{s})^2 \right] \right] \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := - \sum_{ps=1}^{ns} \left[ \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{24} \right] \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + (x_{ps+1}^{s} - x_{ps}^{s})^2 \right] \right] \quad I_{yS} = 0 \text{ m}^4$$

$$I_{xS} := I_{xS} - A_{ST} \cdot x_{ST}^2 \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := I_{yS} - A_{ST} \cdot y_{ST}^2 \quad I_{yS} = 0.00000 \text{ m}^4$$



**Rebar Data Layer 1 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	804	0	-474	51	0	0	0
2	804	-237	-410	52	0	0	0
3	804	-410	-237	53	0	0	0
4	804	-474	0	54	0	0	0
5	804	-410	237	55	0	0	0
6	804	-237	410	56	0	0	0
7	804	0	474	57	0	0	0
8	804	237	410	58	0	0	0
9	804	410	237	59	0	0	0
10	804	474	0	60	0	0	0
11	804	410	-237	61	0	0	0
12	804	237	-410	62	0	0	0
13	0	0	0	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

**Rebar Data Layer 2 - generated from input**

Ref	Area mm2	X mm	Y mm	Ref	Area mm2	X mm	Y mm
1	0	0	0	51	0	0	0
2	0	0	0	52	0	0	0
3	0	0	0	53	0	0	0
4	0	0	0	54	0	0	0
5	0	0	0	55	0	0	0
6	0	0	0	56	0	0	0
7	0	0	0	57	0	0	0
8	0	0	0	58	0	0	0
9	0	0	0	59	0	0	0
10	0	0	0	60	0	0	0
11	0	0	0	61	0	0	0
12	0	0	0	62	0	0	0
13	0	0	0	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0



$$A1 := A1 \cdot \text{mm}^2 \quad A2 := A2 \cdot \text{mm}^2 \quad A3 := A3 \cdot \text{mm}^2 \quad A4 := A4 \cdot \text{mm}^2$$

$$X1 := X1 \cdot \text{mm} \quad X2 := X2 \cdot \text{mm} \quad X3 := X3 \cdot \text{mm} \quad X4 := X4 \cdot \text{mm}$$

$$Y1 := Y1 \cdot \text{mm} \quad Y2 := Y2 \cdot \text{mm} \quad Y3 := Y3 \cdot \text{mm} \quad Y4 := Y4 \cdot \text{mm}$$

$$k := 1..50$$

$$A_{\text{bar}_k} := A1_k \quad x_{\text{bar}_k} := X1_k \quad y_{\text{bar}_k} := Y1_k$$

$$A_{\text{bar}_{k+50}} := A2_k \quad x_{\text{bar}_{k+50}} := X2_k \quad y_{\text{bar}_{k+50}} := Y2_k$$

$$A_{\text{bar}_{k+100}} := A3_k \quad x_{\text{bar}_{k+100}} := X3_k \quad y_{\text{bar}_{k+100}} := Y3_k$$

$$A_{\text{bar}_{k+150}} := A4_k \quad x_{\text{bar}_{k+150}} := X4_k \quad y_{\text{bar}_{k+150}} := Y4_k$$

### Calculate Section Properties of Reinforcement

$$A_{\text{BAR}} := \sum_{j=1}^{200} A_{\text{bar}_j} \quad A_{\text{BAR}} = 9651 \text{ mm}^2$$

$$\rho := \frac{A_{\text{BAR}}}{A_C} \quad \rho = 0.0102$$

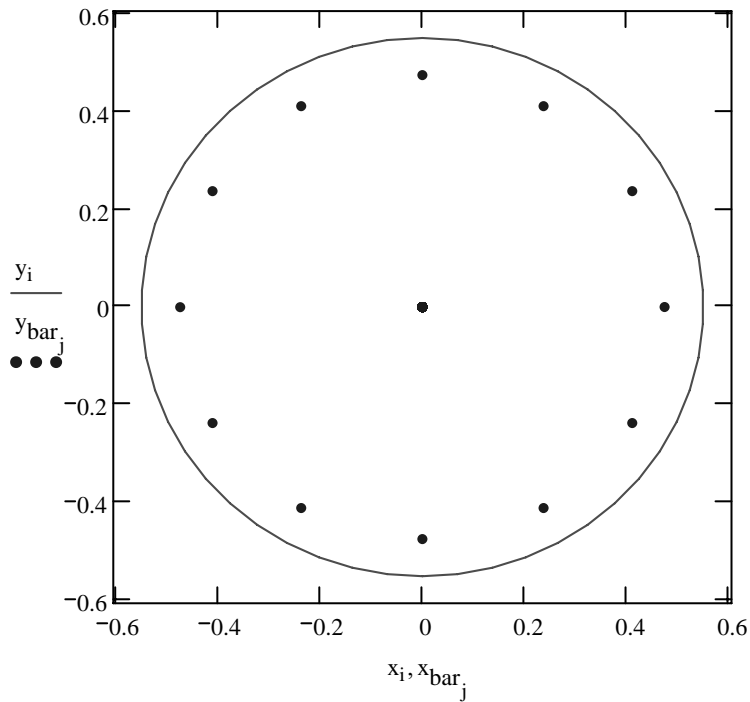
$$x_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot x_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad x_b = 0 \text{ m}$$

$$y_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot y_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad y_b = 0 \text{ m}$$

$$I_{x_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (x_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot x_b^2 \quad I_{x_b} = 0.00108 \text{ m}^4$$

$$I_{y_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (y_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot y_b^2 \quad I_{y_b} = 0.00108 \text{ m}^4$$

$j := 1 .. 200$



**Calculate Composite Section Properties (before cracking)**

Effective area  $A_E := A_C \cdot [1 + \rho \cdot (\alpha - 1)] + A_{ST} \cdot \alpha$   $A_E = 1013161 \text{ mm}^2$

Effective centroid  $x_E := \frac{A_C \cdot [(1 - \rho) \cdot x_C + \rho \cdot x_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot x_{ST}}{A_E}$   $x_E = 0.000 \text{ m}$

$y_E := \frac{A_C \cdot [(1 - \rho) \cdot y_C + \rho \cdot y_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot y_{ST}}{A_E}$   $y_E = 0.000 \text{ m}$

Effective stiffness  $I_{EX} := I_{xC} + I_{xb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot x_C^2 + \rho \cdot x_b^2 \cdot \alpha] + (I_{xS} + A_{ST} \cdot x_{ST}^2) \cdot \alpha$   
 $I_{EX} = 0 \text{ m}^4$

$I_{EY} := I_{yC} + I_{yb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot y_C^2 + \rho \cdot y_b^2 \cdot \alpha] + (I_{yS} + A_{ST} \cdot y_{ST}^2) \cdot \alpha$   
 $I_{EY} = 0 \text{ m}^4$

Distance from extreme concrete fiber to centroid

$x_{F_{pos}} := \max(x - x_E)$   $x_{F_{neg}} := \min(x - x_E)$

$y_{F_{pos}} := \max(y - y_E)$   $y_{F_{neg}} := \min(y - y_E)$

Total depth of concrete section

$H_{CX} := x_{F_{pos}} - x_{F_{neg}}$   $H_{CX} = 1 \text{ m}$

$H_{CY} := y_{F_{pos}} - y_{F_{neg}}$   $H_{CY} = 1 \text{ m}$

Section modulus

$$Z_{Xpos} := \frac{I_{EX}}{xF_{pos}}$$

$$Z_{Xneg} := \frac{I_{EX}}{xF_{neg}}$$

$$Z_{Ypos} := \frac{I_{EY}}{yF_{pos}}$$

$$Z_{Yneg} := \frac{I_{EY}}{yF_{neg}}$$

Thickness of steel tube:

$$ts := y_1 - ys_1$$

$$ts = 0 \text{ mm}$$

**Establish Section Dimensions**

Positive case - determine coord of extreme concrete fiber

$$y_{Epos} := \max(y)$$

$$y_{Epos} = 550 \text{ mm}$$

Negative case - determine coord of extreme concrete fiber

$$y_{Eneg} := \min(y)$$

$$y_{Eneg} = -550 \text{ mm}$$

Offsets of rebar from extreme fiber

$$y_{Obar} := y_{Epos} - y_{bar}$$

Determine most extreme rebar (minimum offset)

$$y_{1bar} := \min(y_{Epos} - y_{bar})$$

$$y_{1bar} = 76 \text{ mm}$$

Determine most extreme rebar (maximum offset)

$$y_{nbar} := \max(y_{Epos} - y_{bar})$$

$$y_{nbar} = 1024 \text{ mm}$$

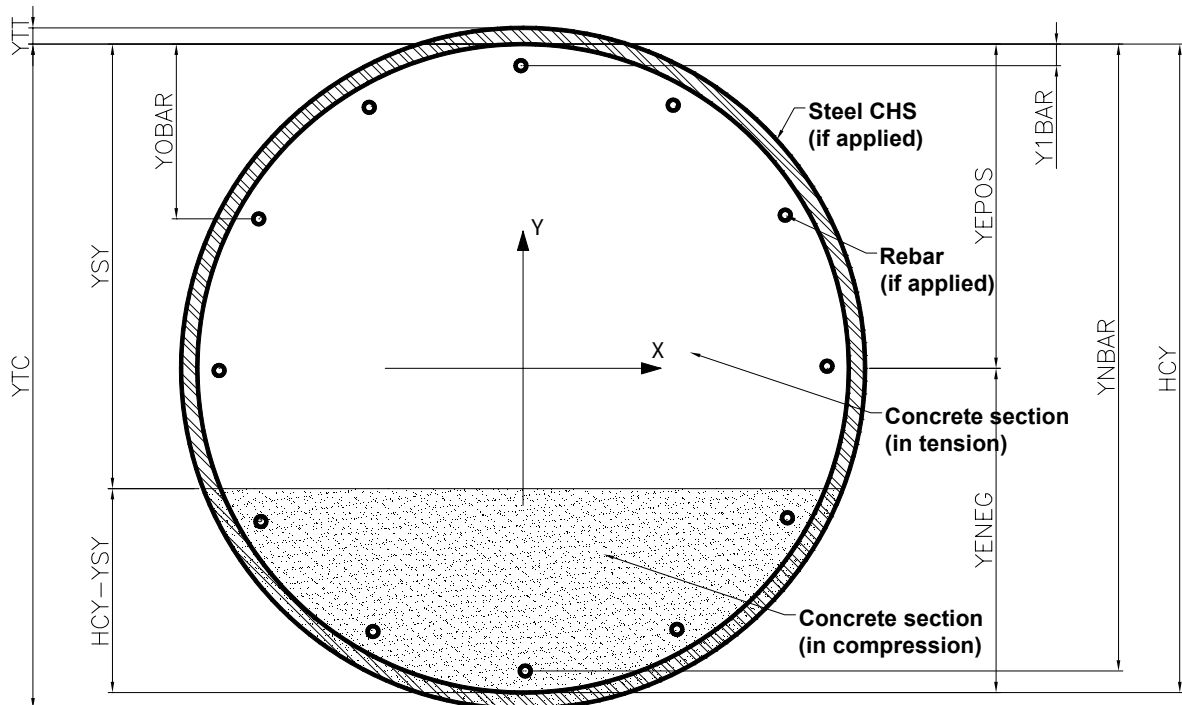
Offsets of extreme steel tube fiber from extreme concrete fiber

$$y_{tt} := ts$$

$$y_{tt} = 0 \text{ mm}$$

$$y_{tc} := H_{CY} + ts$$

$$y_{tc} = 1100 \text{ mm}$$



**ASSIGN NEUTRAL AXIS VALUES**

Number of sections to analysed                      ns := 500

q := 2 .. ns

Distance of neutral axis from extreme fiber in tension                       $y_{SY_q} := H_{CY} \cdot \frac{q}{ns + 1}$

**Calculate stresses and strains in reinforcement and concrete at extreme fibers**

Calculate strain at extreme compression fiber assuming max allowable stress in concrete:

Trial value of concrete strain

$$\epsilon_{cc} := \frac{\sigma_{cc}}{E_C} \cdot 2 \qquad \frac{\sigma_{cc}}{E_C} = 0.001165$$

Given

$$\sigma_{cc} = \epsilon_{cc} \cdot \left( 4700 \sqrt{\frac{f_c \cdot 2}{MPa}} - \frac{4700^2}{2.68} \cdot \epsilon_{cc} \right) \cdot MPa$$

$$\epsilon_{cc} := \text{Find}(\epsilon_{cc}) \qquad \epsilon_{cc} = 0.003321$$

$$\epsilon_{cc} := \begin{cases} \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \epsilon_{cc} & \text{otherwise} \end{cases} \qquad \epsilon_{cc} = 0.003321$$

Strain at other stresses taken to be linear:

$$\epsilon_{cc}(f_c, \sigma_{cd}) := \begin{cases} \frac{\sigma_{cd}}{\sigma_{tc}} \cdot \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \frac{\sigma_{cd}}{\sigma_{rc}} \cdot \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \frac{\sigma_{cd}}{\sigma_{cc}} \cdot \epsilon_{cc} & \text{otherwise} \end{cases}$$

Calculate strain in steel tube assuming max allowable stress in concrete:

$$\begin{aligned} \text{In compression} \quad \epsilon_{tcc_q} &:= \epsilon_{cc} \cdot \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \\ \text{In tension} \quad \epsilon_{tct_q} &:= \epsilon_{cc} \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \end{aligned}$$

Calculate strain in rebar assuming max allowable stress in concrete:

$$\begin{array}{l} \text{In} \\ \text{compression} \end{array} \quad \varepsilon_{rcc_q} := \varepsilon_{cc} \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

$$\begin{array}{l} \text{In} \\ \text{tension} \end{array} \quad \varepsilon_{rct_q} := \varepsilon_{cc} \cdot \frac{y_{1bar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

Calculate design max stress in compression taking account of other limits:

$$\sigma_{cd}(\varepsilon_{tcc}, q) := \left\{ \begin{array}{l} \sigma_{cd} \leftarrow \sigma_{cc} \quad \text{if } f_c > 0 \\ \sigma_{cd} \leftarrow \sigma_{tc} \quad \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \sigma_{cd} \leftarrow \sigma_{rc} \quad \text{if } (f_c = 0) \cdot (ts = 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{tc}}{\varepsilon_{tcc}} \quad \text{if } (\varepsilon_{tcc} > \varepsilon_{tc}) \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rc}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}} \quad \text{if } \left( \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}} > \varepsilon_{rc} \right) \cdot (A_{BAR} > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{ts}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}}} \quad \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} < \varepsilon_{ts} \right] \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rs}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}}} \quad \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}} < \varepsilon_{rs} \right] \cdot (A_{BAR} > 0) \\ \sigma_{cc} \quad \text{otherwise} \end{array} \right.$$

$$\sigma_{cd_q} := \sigma_{cd}(\varepsilon_{tcc_q}, q)$$

**CALCULATE FORCES AND MOMENTS AT EACH NEUTRAL AXIS LOCATION**

Calculate force in concrete:

$$F_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from concrete about column centroid:

$$M_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] \cdot y dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in rebar assuming design max stress in concrete:

$$y_{SY_q} := \begin{cases} y_{nbar} \cdot \frac{q}{ns + 1} & \text{if } (f_c = 0) \cdot (A_{BAR} > 0) \\ y_{SY_q} & \text{otherwise} \end{cases}$$

$$\varepsilon_{S_{j,q}} := \begin{cases} \frac{y_{SY_q} - y_{Obar_j}}{y_{nbar} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{if } f_c = 0 \\ \frac{y_{SY_q} - y_{Obar_j}}{H_{CY} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{otherwise} \end{cases}$$

Calculate force in each rebar:

$$F_{S_{j,q}} := \begin{cases} \varepsilon_{S_{j,q}} \cdot E_S \cdot A_{bar_j} & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total force in reinforcement:

$$F_{R_q} := \sum_j F_{S_{j,q}}$$

Calculate moment from reinforcement about section centroid:

$$M_{R_q} := \begin{cases} \sum_j -(\varepsilon_{S_{j,q}} E_S A_{bar_j} y_{bar_j}) & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in steel tube at extreme tension fiber:

$$\varepsilon_{tds_q} := \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate strain in steel tube at extreme compression fiber:

$$\varepsilon_{tdc_q} := \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate tensile force in steel tube:

$$F_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS} := \begin{cases} F_{TS1} - F_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate compressive force in steel tube:

$$F_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TC2_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TC} := \begin{cases} F_{TC1} - F_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from tensile force in steel tube:

$$M_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} -2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} -2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS} := \begin{cases} M_{TS1} - M_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from compressive force in steel tube:

$$M_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC2_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$



$$M_{TC} := \begin{cases} M_{TC1} - M_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total axial response from section:

$$F_T := F_C + F_R + F_{TS} + F_{TC}$$

$$F_{TC} := F_C$$

Calculate total moment response from section:

$$M_T := M_C + M_R + M_{TS} + M_{TC}$$

$$M_{TC} := M_C$$

**CALCULATE MAXIMUM ALLOWABLE AXIAL FORCE IN SECTION**

Limiting strain in axial  
compression:

$$\varepsilon_{cL} := \begin{cases} \min(\varepsilon_{cc}, \varepsilon_{tc}) & \text{if } (A_{BAR} = 0) \cdot (ts \neq 0) \cdot (f_c \neq 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}) & \text{if } (ts = 0) \cdot (A_{BAR} \neq 0) \cdot (f_c \neq 0) \\ \varepsilon_{tc} & \text{if } (A_{BAR} = 0) \cdot (f_c = 0) \\ \varepsilon_{rc} & \text{if } (ts = 0) \cdot (f_c = 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}, \varepsilon_{tc}) & \text{otherwise} \end{cases} \quad \varepsilon_{cL} = 0.001950$$

Limiting concrete stress in axial compression

$$\sigma_{cL} := \begin{cases} \sigma_{cd2} & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases} \quad \sigma_{cL} = 18.93 \text{ MPa}$$

$$P_{MAX} := \sigma_{cL} \cdot A_C (1 - \rho) + \varepsilon_{cL} \cdot E_S (A_{BAR} + A_{ST})$$

$$P_{MAX} = 21522.8 \text{ kN} \quad F_{T_1} := P_{MAX} \quad M_{T_1} := 0 \cdot \text{kN} \cdot \text{m}$$

$$P_{MAXC} := \sigma_{cL} \cdot A_C \cdot (1 - \rho)$$

$$P_{MAXC} = 17758.9 \text{ kN} \quad F_{TC_1} := P_{MAXC} \quad M_{TC_1} := 0 \cdot \text{kN} \cdot \text{m}$$

**CALCULATE MINIMUM ALLOWABLE AXIAL FORCE IN SECTION**

$$P_{MIN} := \begin{cases} \varepsilon_{rs} \cdot E_S (A_{BAR}) & \text{if } ts = 0 \\ \varepsilon_{ts} \cdot E_S (A_{ST}) & \text{if } A_{BAR} = 0 \\ \max(\varepsilon_{ts}, \varepsilon_{rs}) \cdot E_S (A_{BAR} + A_{ST}) & \text{otherwise} \end{cases}$$

$$P_{MIN} = -1640.7 \text{ kN} \quad F_{T_{ns+1}} := P_{MIN} \quad M_{T_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

$$\text{Limit} := \begin{cases} \min(P, F_T) \cdot 0.75 & \text{if } \min(P) > 0 \\ \min(P, F_T) \cdot 1.25 & \text{otherwise} \end{cases}$$

$$P_{MINC} := 0 \text{ kN} \quad M_{TC_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

Diameter of Column  $D = 1100 \text{ mm}$

Percentage reinforcement  $\rho = 1.02 \%$

Thickness of CHS  $t_s = 0 \text{ mm}$

Characteristic strength of concrete

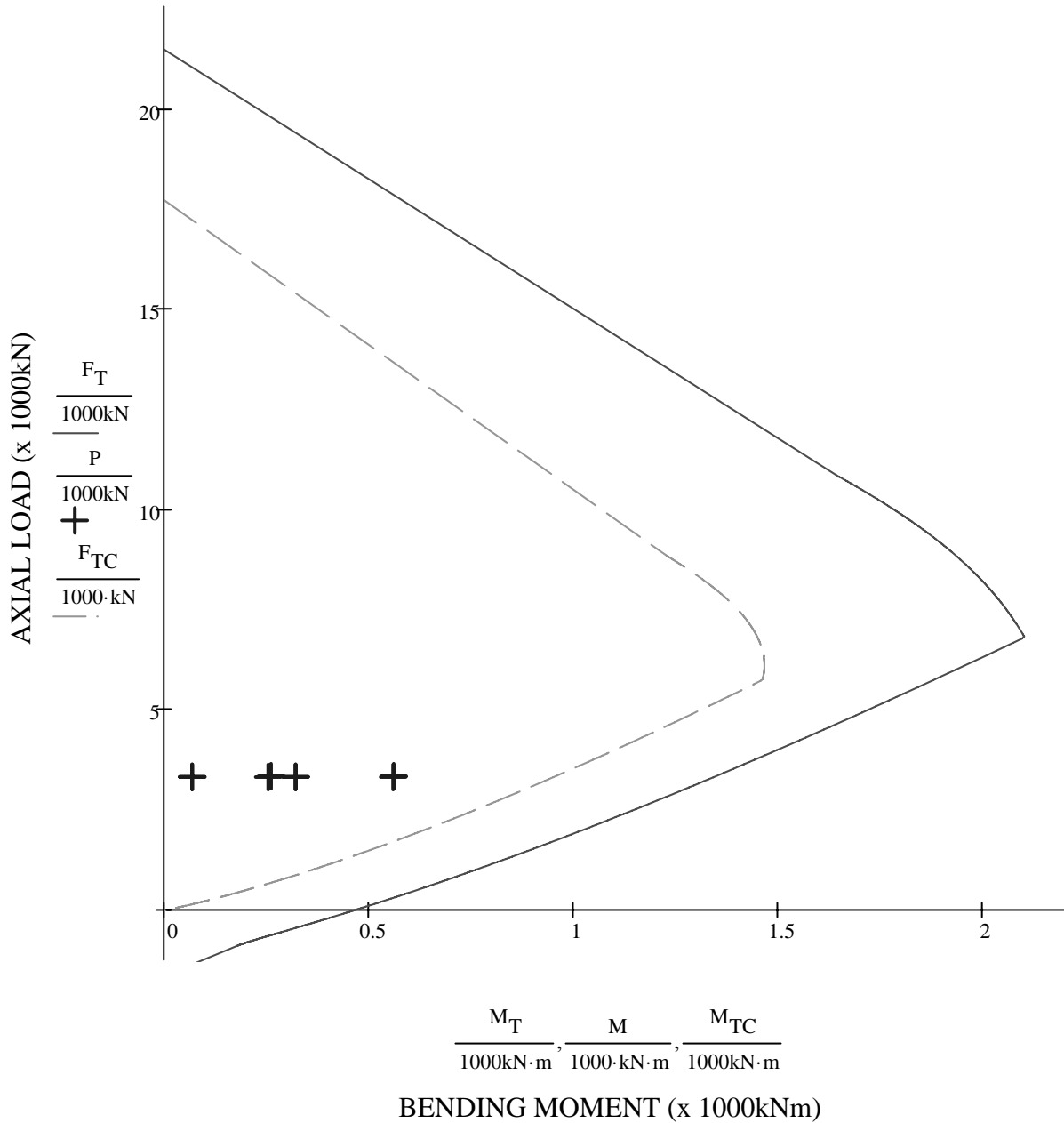
Yield Strength of Rebar

Yield Strength of CHS

$f_c = 30 \text{ MPa}$

$f_y = 390 \text{ MPa}$

$f_{ys} = 250 \text{ MPa}$



INTERACTION CURVE AT SERVICEABILITY LIMIT STATE

Equation of interaction line - upper region (between 1 and 2 calculation points)

$$m1 := \frac{M_{T_2} - M_{T_1}}{F_{T_2} - F_{T_1}} \quad c1 := F_{T_1}$$

Equation of interaction line - lower region (between ns and ns+1 calculation points)

$$m2 := \frac{M_{T_{ns}} - M_{T_{ns+1}}}{F_{T_{ns}} - F_{T_{ns+1}}} \quad c2 := F_{T_{ns+1}}$$

r := 1 .. 8

$$M_{SLS_r} := \begin{cases} 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r > F_{T_1} \\ 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r < F_{T_{ns+1}} \\ (P_r - c1) \cdot m1 & \text{if } (P_r > F_{T_2}) \cdot (P_r \leq F_{T_1}) \\ (P_r - c2) \cdot m2 & \text{if } (P_r \geq F_{T_{ns+1}}) \cdot (P_r < F_{T_{ns}}) \\ \text{otherwise} \\ \quad j \leftarrow 1 \\ \quad \text{while } F_{T_j} > P_r \\ \quad \quad j \leftarrow j + 1 \\ \quad M_{T_j} \end{cases}$$

$$\text{StressFactor}_r := \begin{cases} \text{"No Result"} & \text{if } M_{SLS_r} < 0.000000000000000001 \cdot \text{kN}\cdot\text{m} \\ \frac{M_r}{M_{SLS_r}} & \text{otherwise} \end{cases}$$

$$P = \begin{pmatrix} 3337 \\ 3337 \\ 3341 \\ 3341 \\ 3355 \\ 3355 \\ 3335 \\ 3335 \end{pmatrix} \text{ kN} \quad M = \begin{pmatrix} 70 \\ 322 \\ 70 \\ 323 \\ 562 \\ 263 \\ 561 \\ 256 \end{pmatrix} \text{ kN}\cdot\text{m} \quad M_{SLS} = \begin{pmatrix} 1343.2 \\ 1343.2 \\ 1343.2 \\ 1343.2 \\ 1343.2 \\ 1343.2 \\ 1343.2 \\ 1343.2 \end{pmatrix} \text{ kN}\cdot\text{m} \quad \text{StressFactor} = \begin{pmatrix} 0.052 \\ 0.240 \\ 0.052 \\ 0.240 \\ 0.419 \\ 0.195 \\ 0.417 \\ 0.190 \end{pmatrix}$$

**RESULTS SUMMARY**  
**SERVICEABILITY LIMIT STATE ANALYSIS OF CIRCULAR BEAM COLUMN**

Diameter of Column		1100	mm				
Percentage of rebar		1.02	%				
Load Case Ref	Pier	Applied Service Axial Load kN	Applied Service Bending Moment kNm	Service Limit State Bending Moment kNm	Allowable Stress Factor	Applied Stress Factor	Serviceability Limit State Design Result
1	P21	3337	70	1343.2	100%	5%	OK
2	P21	3337	322	1343.2	100%	24%	OK
3	P22	3341	70	1343.2	100%	5%	OK
4	P22	3341	323	1343.2	100%	24%	OK

## **Serviceability Check - Full Live Load**



**KATAHIRA & ENGINEERS  
INTERNATIONAL**

**Project:** Detailed Design Study of  
North Java Corridor Flyover Project

**Calculation:** Balaraja Flyover  
Serviceability Check - Full Live Load  
1100 mm Dia Circular RC Column - P2 Base Section

**Reference:** Project Specific Design Criteria

**Section Data**

MPa := 1000000·Pa

kN := 1000·N

Input Item		
Concrete Compressive Strength	fc	30 MPa
Structural Steel Yield Strength	fys	250 MPa
Rebar Yield Strength	fy	390 MPa
Diameter of reinforced concrete section	D	1100 mm
Thickness of CHS section	t	0 mm
Diameter of rebar - layer 1	dia1	32 mm
Diameter of rebar - layer 2	dia2	0 mm
Number bars - layer 1 (max 100)	n1	12
Number bars - layer 2 (max 100)	n2	0
Cover from face of section - layer 1	cov1	60 mm
Cover from face of section - layer 2	cov2	115 mm

**Load Data**

Ref	Pier	Load Case	P	M	Stress
			kN	kNm	Allowance
1	P21	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+CRSH	3336.8	287.0	140%
2	P21	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+CRSH	3336.8	544.2	140%
3	P22	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+CRSH	3341.4	286.7	140%
4	P22	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+CRSH	3341.4	544.8	140%

$$f_c := f_c \cdot \text{MPa} \quad f_{ys} := f_{ys} \cdot \text{MPa} \quad f_y := f_y \cdot \text{MPa} \quad D := D \cdot \text{mm} \quad ts := ts \cdot \text{mm}$$

$$\text{dia1} := \text{dia1} \cdot \text{mm} \quad \text{dia2} := \text{dia2} \cdot \text{mm} \quad \text{cov1} := \text{cov1} \cdot \text{mm} \quad \text{cov2} := \text{cov2} \cdot \text{mm}$$

$$P := P \cdot \text{kN} \quad M := M \cdot \text{kN} \cdot \text{m}$$

$$E_S := 200000 \cdot \text{MPa} \quad E_C := 4700 \sqrt{\frac{f_c}{\text{MPa}}} \cdot \text{MPa} \quad \text{Modular ratio} \quad \alpha := \begin{cases} \frac{E_S}{E_C} & \text{if } E_C > 0 \\ 1 & \text{otherwise} \end{cases} \quad \alpha = 7.77$$

$$E_C = 25743 \text{ MPa}$$

### Calculate Basic Allowable Stresses

Calculate rupture stress:

$$\sigma_{ct} := 0.5 \cdot \left( \frac{f_c}{\text{MPa}} \right)^{\frac{2}{3}} \cdot \text{MPa} \quad \sigma_{ct} = 4.8 \text{ MPa}$$

Calculate basic allowable stress of concrete

$$\sigma_{cc} := 1.0 \cdot f_c \quad \sigma_{cc} = 30.0 \text{ MPa}$$

Calculate basic allowable tensile stress of rebar

$$\sigma_{rs} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 170 \text{ MPa} \\ 170 \text{ MPa} & \text{otherwise} \end{cases} \quad \sigma_{rs} = 170 \text{ MPa}$$

Calculate basic allowable compressive stress of rebar

$$\sigma_{rc} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 110 \text{ MPa} \\ f_y & \text{otherwise} \end{cases} \quad \sigma_{rc} = 390 \text{ MPa}$$

Calculate basic allowable stress of structural steel

$$\sigma_{ts} := -0.6 f_{ys} \quad \sigma_{ts} = -150 \text{ MPa}$$

$$\sigma_{tc} := 1 f_{ys} \quad \sigma_{tc} = 250 \text{ MPa}$$

Limiting strain of rebar

$$\epsilon_{rs} := -\frac{\sigma_{rs}}{E_S} \quad \epsilon_{rs} = -0.000850$$

$$\epsilon_{rc} := \frac{\sigma_{rc}}{E_S} \quad \epsilon_{rc} = 0.001950$$

Limiting strain of structural steel

$$\epsilon_{ts} := \frac{\sigma_{ts}}{E_S} \quad \epsilon_{ts} = -0.000750$$

$$\epsilon_{tc} := \frac{\sigma_{tc}}{E_S} \quad \epsilon_{tc} = 0.001250$$



### Concrete Cross Section Data - generated

n := 50      Number of Points - 50 points maximum

i := 1 .. n + 1    Range from 1 to n+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	550
2	-69	-546	27	69	546
3	-137	-533	28	137	533
4	-202	-511	29	202	511
5	-265	-482	30	265	482
6	-323	-445	31	323	445
7	-377	-401	32	377	401
8	-424	-351	33	424	351
9	-464	-295	34	464	295
10	-498	-234	35	498	234
11	-523	-170	36	523	170
12	-540	-103	37	540	103
13	-549	-35	38	549	35
14	-549	35	39	549	-35
15	-540	103	40	540	-103
16	-523	170	41	523	-170
17	-498	234	42	498	-234
18	-464	295	43	464	-295
19	-424	351	44	424	-351
20	-377	401	45	377	-401
21	-323	445	46	323	-445
22	-265	482	47	265	-482
23	-202	511	48	202	-511
24	-137	533	49	137	-533
25	-69	546	50	69	-546

k := 1 .. 25      XS1 := XS1·mm    XS2 := XS2·mm      YS1 := YS1·mm    YS2 := YS2·mm

$x_k := XS1_k$        $y_k := YS1_k$        $x_{k+25} := XS2_k$        $y_{k+25} := YS2_k$        $x_{n+1} := XS1_1$        $y_{n+1} := YS1_1$

### Calculate Section Properties of Concrete Section

$$A_C := - \sum_{i=1}^n \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{2} \right] \quad A_C = 0.94783 \text{ m}^2$$

$$x_C := - \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{y_{i+1} - y_i}{8} \cdot \left[ (x_{i+1} + x_i)^2 + \frac{(x_{i+1} - x_i)^2}{3} \right] \right] \quad x_C = 0 \text{ m}$$

$$y_C := \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{x_{i+1} - x_i}{8} \cdot \left[ (y_{i+1} + y_i)^2 + \frac{(y_{i+1} - y_i)^2}{3} \right] \right] \quad y_C = 0 \text{ m}$$

$$I_x := \sum_{i=1}^n \left[ \left[ (x_{i+1} - x_i) \cdot \frac{y_{i+1} + y_i}{24} \right] \cdot \left[ (y_{i+1} + y_i)^2 + (y_{i+1} - y_i)^2 \right] \right] \quad I_x = 0.07149 \text{ m}^4$$

$$I_y := - \sum_{i=1}^n \left[ \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{24} \right] \cdot \left[ (x_{i+1} + x_i)^2 + (x_{i+1} - x_i)^2 \right] \right] \quad I_y = 0.07149 \text{ m}^4$$

$$I_{xC} := I_x - A_C \cdot x_C^2 \quad I_{xC} = 0.07149 \text{ m}^4$$

$$I_{yC} := I_y - A_C \cdot y_C^2 \quad I_{yC} = 0.07149 \text{ m}^4$$

### Steel Tube Cross Section Data - generated from input

ns := 50      Number of Points - 50 points maximum

ps := 1 .. ns + 1      Range from 1 to ns+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	-550
2	-142	-531	27	142	-531
3	-275	-476	28	275	-476
4	-389	-389	29	389	-389
5	-476	-275	30	476	-275
6	-531	-142	31	531	-142
7	-550	0	32	550	0
8	-531	142	33	531	142
9	-476	275	34	476	275
10	-389	389	35	389	389
11	-275	476	36	275	476
12	-142	531	37	142	531
13	0	550	38	0	550
14	142	531	39	-142	531
15	275	476	40	-275	476
16	389	389	41	-389	389
17	476	275	42	-476	275
18	531	142	43	-531	142
19	550	0	44	-550	0
20	531	-142	45	-531	-142
21	476	-275	46	-476	-275
22	389	-389	47	-389	-389
23	275	-476	48	-275	-476
24	142	-531	49	-142	-531
25	0	-550	50	0	-550

$$XSS1 := XSS1 \cdot \text{mm}$$

$$XSS2 := XSS2 \cdot \text{mm}$$

$$YSS1 := YSS1 \cdot \text{mm}$$

$$YSS2 := YSS2 \cdot \text{mm}$$

$$z := 1 .. 25$$

$$xs_z := XSS1_z$$

$$ys_z := YSS1_z$$

$$z := 26 .. 50$$

$$xs_z := XSS2_{z-25}$$

$$ys_z := YSS2_{z-25}$$

$$xs_{ns+1} := XSS1_1$$

$$ys_{ns+1} := YSS1_1$$

**Calculate Section Properties of Steel Tube Section**

$$A_{ST} := - \sum_{ps=1}^{ns} \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{2} \right] \quad A_{ST} = 0 \text{ m}^2$$

$$x_{ST} := - \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{y_{ps+1}^{s} - y_{ps}^{s}}{8} \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + \frac{(x_{ps+1}^{s} - x_{ps}^{s})^2}{3} \right] \right] \quad x_{ST} = 0.2 \text{ m}$$

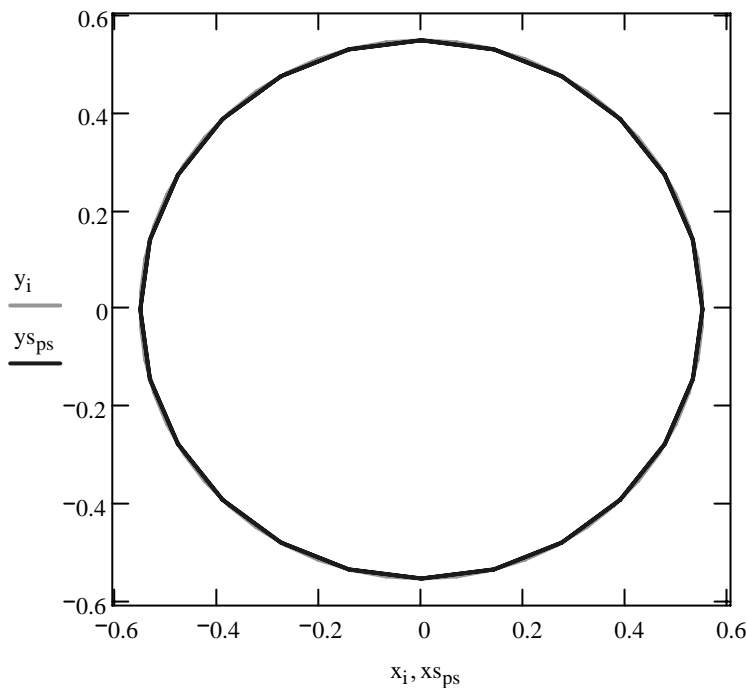
$$y_{ST} := \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{x_{ps+1}^{s} - x_{ps}^{s}}{8} \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + \frac{(y_{ps+1}^{s} - y_{ps}^{s})^2}{3} \right] \right] \quad y_{ST} = -0.011 \text{ m}$$

$$I_{xS} := \sum_{ps=1}^{ns} \left[ \left[ (x_{ps+1}^{s} - x_{ps}^{s}) \cdot \frac{y_{ps+1}^{s} + y_{ps}^{s}}{24} \right] \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + (y_{ps+1}^{s} - y_{ps}^{s})^2 \right] \right] \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := - \sum_{ps=1}^{ns} \left[ \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{24} \right] \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + (x_{ps+1}^{s} - x_{ps}^{s})^2 \right] \right] \quad I_{yS} = 0 \text{ m}^4$$

$$I_{xS} := I_{xS} - A_{ST} \cdot x_{ST}^2 \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := I_{yS} - A_{ST} \cdot y_{ST}^2 \quad I_{yS} = 0.00000 \text{ m}^4$$



**Rebar Data Layer 1 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	804	0	-474	51	0	0	0
2	804	-237	-410	52	0	0	0
3	804	-410	-237	53	0	0	0
4	804	-474	0	54	0	0	0
5	804	-410	237	55	0	0	0
6	804	-237	410	56	0	0	0
7	804	0	474	57	0	0	0
8	804	237	410	58	0	0	0
9	804	410	237	59	0	0	0
10	804	474	0	60	0	0	0
11	804	410	-237	61	0	0	0
12	804	237	-410	62	0	0	0
13	0	0	0	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

**Rebar Data Layer 2 - generated from input**

Ref	Area mm2	X mm	Y mm	Ref	Area mm2	X mm	Y mm
1	0	0	0	51	0	0	0
2	0	0	0	52	0	0	0
3	0	0	0	53	0	0	0
4	0	0	0	54	0	0	0
5	0	0	0	55	0	0	0
6	0	0	0	56	0	0	0
7	0	0	0	57	0	0	0
8	0	0	0	58	0	0	0
9	0	0	0	59	0	0	0
10	0	0	0	60	0	0	0
11	0	0	0	61	0	0	0
12	0	0	0	62	0	0	0
13	0	0	0	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

$$A1 := A1 \cdot \text{mm}^2 \quad A2 := A2 \cdot \text{mm}^2 \quad A3 := A3 \cdot \text{mm}^2 \quad A4 := A4 \cdot \text{mm}^2$$

$$X1 := X1 \cdot \text{mm} \quad X2 := X2 \cdot \text{mm} \quad X3 := X3 \cdot \text{mm} \quad X4 := X4 \cdot \text{mm}$$

$$Y1 := Y1 \cdot \text{mm} \quad Y2 := Y2 \cdot \text{mm} \quad Y3 := Y3 \cdot \text{mm} \quad Y4 := Y4 \cdot \text{mm}$$

$$k := 1..50$$

$$A_{\text{bar}_k} := A1_k \quad x_{\text{bar}_k} := X1_k \quad y_{\text{bar}_k} := Y1_k$$

$$A_{\text{bar}_{k+50}} := A2_k \quad x_{\text{bar}_{k+50}} := X2_k \quad y_{\text{bar}_{k+50}} := Y2_k$$

$$A_{\text{bar}_{k+100}} := A3_k \quad x_{\text{bar}_{k+100}} := X3_k \quad y_{\text{bar}_{k+100}} := Y3_k$$

$$A_{\text{bar}_{k+150}} := A4_k \quad x_{\text{bar}_{k+150}} := X4_k \quad y_{\text{bar}_{k+150}} := Y4_k$$

### Calculate Section Properties of Reinforcement

$$A_{\text{BAR}} := \sum_{j=1}^{200} A_{\text{bar}_j} \quad A_{\text{BAR}} = 9651 \text{ mm}^2$$

$$\rho := \frac{A_{\text{BAR}}}{A_C} \quad \rho = 0.0102$$

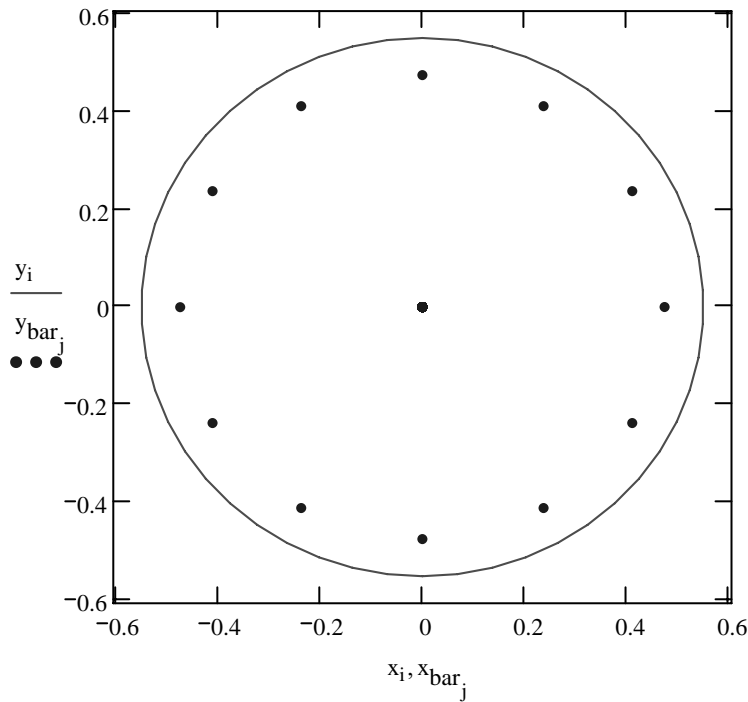
$$x_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot x_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad x_b = 0 \text{ m}$$

$$y_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot y_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad y_b = 0 \text{ m}$$

$$I_{x_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (x_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot x_b^2 \quad I_{x_b} = 0.00108 \text{ m}^4$$

$$I_{y_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (y_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot y_b^2 \quad I_{y_b} = 0.00108 \text{ m}^4$$

$j := 1 .. 200$



**Calculate Composite Section Properties (before cracking)**

Effective area  $A_E := A_C \cdot [1 + \rho \cdot (\alpha - 1)] + A_{ST} \cdot \alpha$   $A_E = 1013161 \text{ mm}^2$

Effective centroid  $x_E := \frac{A_C \cdot [(1 - \rho) \cdot x_C + \rho \cdot x_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot x_{ST}}{A_E}$   $x_E = 0.000 \text{ m}$

$y_E := \frac{A_C \cdot [(1 - \rho) \cdot y_C + \rho \cdot y_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot y_{ST}}{A_E}$   $y_E = 0.000 \text{ m}$

Effective stiffness  $I_{EX} := I_{xC} + I_{xb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot x_C^2 + \rho \cdot x_b^2 \cdot \alpha] + (I_{xS} + A_{ST} \cdot x_{ST}^2) \cdot \alpha$   
 $I_{EX} = 0 \text{ m}^4$

$I_{EY} := I_{yC} + I_{yb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot y_C^2 + \rho \cdot y_b^2 \cdot \alpha] + (I_{yS} + A_{ST} \cdot y_{ST}^2) \cdot \alpha$   
 $I_{EY} = 0 \text{ m}^4$

Distance from extreme concrete fiber to centroid

$x_{F_{pos}} := \max(x - x_E)$   $x_{F_{neg}} := \min(x - x_E)$

$y_{F_{pos}} := \max(y - y_E)$   $y_{F_{neg}} := \min(y - y_E)$

Total depth of concrete section

$H_{CX} := x_{F_{pos}} - x_{F_{neg}}$   $H_{CX} = 1 \text{ m}$

$H_{CY} := y_{F_{pos}} - y_{F_{neg}}$   $H_{CY} = 1 \text{ m}$



Section modulus

$$Z_{Xpos} := \frac{I_{EX}}{xF_{pos}}$$

$$Z_{Xneg} := \frac{I_{EX}}{xF_{neg}}$$

$$Z_{Ypos} := \frac{I_{EY}}{yF_{pos}}$$

$$Z_{Yneg} := \frac{I_{EY}}{yF_{neg}}$$

Thickness of steel tube:

$$ts := y_1 - ys_1$$

$$ts = 0 \text{ mm}$$

**Establish Section Dimensions**

Positive case - determine coord of extreme concrete fiber

$$y_{Epos} := \max(y)$$

$$y_{Epos} = 550 \text{ mm}$$

Negative case - determine coord of extreme concrete fiber

$$y_{Eneg} := \min(y)$$

$$y_{Eneg} = -550 \text{ mm}$$

Offsets of rebar from extreme fiber

$$y_{Obar} := y_{Epos} - y_{bar}$$

Determine most extreme rebar (minimum offset)

$$y_{1bar} := \min(y_{Epos} - y_{bar})$$

$$y_{1bar} = 76 \text{ mm}$$

Determine most extreme rebar (maximum offset)

$$y_{nbar} := \max(y_{Epos} - y_{bar})$$

$$y_{nbar} = 1024 \text{ mm}$$

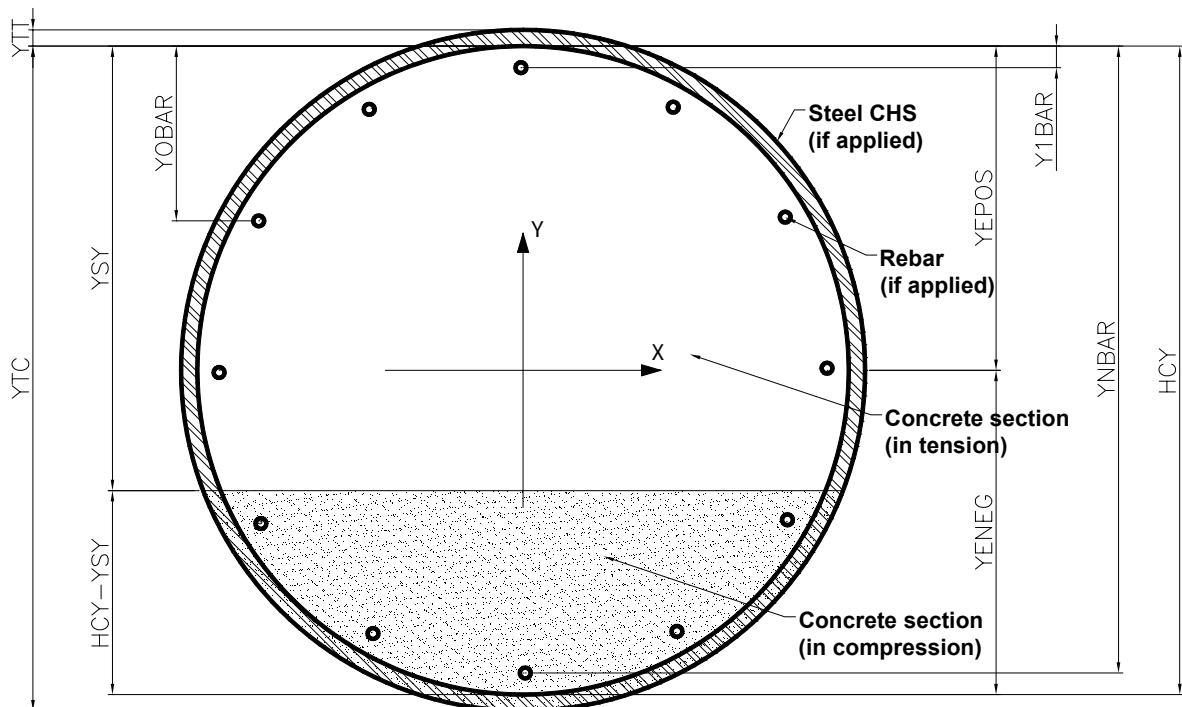
Offsets of extreme steel tube fiber from extreme concrete fiber

$$y_{tt} := ts$$

$$y_{tt} = 0 \text{ mm}$$

$$y_{tc} := H_{CY} + ts$$

$$y_{tc} = 1100 \text{ mm}$$



**ASSIGN NEUTRAL AXIS VALUES**

Number of sections to analysed                      ns := 500

q := 2 .. ns

Distance of neutral axis from extreme fiber in tension                       $y_{SY_q} := H_{CY} \cdot \frac{q}{ns + 1}$

**Calculate stresses and strains in reinforcement and concrete at extreme fibers**

Calculate strain at extreme compression fiber assuming max allowable stress in concrete:

Trial value of concrete strain

$$\epsilon_{cc} := \frac{\sigma_{cc}}{E_C} \cdot 2 \qquad \frac{\sigma_{cc}}{E_C} = 0.001165$$

Given

$$\sigma_{cc} = \epsilon_{cc} \cdot \left( 4700 \sqrt{\frac{f_c \cdot 2}{MPa}} - \frac{4700^2}{2.68} \cdot \epsilon_{cc} \right) \cdot MPa$$

$$\epsilon_{cc} := \text{Find}(\epsilon_{cc}) \qquad \epsilon_{cc} = 0.003321$$

$$\epsilon_{cc} := \begin{cases} \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \epsilon_{cc} & \text{otherwise} \end{cases} \qquad \epsilon_{cc} = 0.003321$$

Strain at other stresses taken to be linear:

$$\epsilon_{cc}(f_c, \sigma_{cd}) := \begin{cases} \frac{\sigma_{cd}}{\sigma_{tc}} \cdot \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \frac{\sigma_{cd}}{\sigma_{rc}} \cdot \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \frac{\sigma_{cd}}{\sigma_{cc}} \cdot \epsilon_{cc} & \text{otherwise} \end{cases}$$

Calculate strain in steel tube assuming max allowable stress in concrete:

$$\begin{aligned} \text{In compression} \quad \epsilon_{tcc_q} &:= \epsilon_{cc} \cdot \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \\ \text{In tension} \quad \epsilon_{tct_q} &:= \epsilon_{cc} \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \end{aligned}$$

Calculate strain in rebar assuming max allowable stress in concrete:

$$\text{In compression} \quad \varepsilon_{rcc_q} := \varepsilon_{cc} \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

$$\text{In tension} \quad \varepsilon_{rct_q} := \varepsilon_{cc} \cdot \frac{y_{1bar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

Calculate design max stress in compression taking account of other limits:

$$\sigma_{cd}(\varepsilon_{tcc}, q) := \begin{cases} \sigma_{cd} \leftarrow \sigma_{cc} & \text{if } f_c > 0 \\ \sigma_{cd} \leftarrow \sigma_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \sigma_{cd} \leftarrow \sigma_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{tc}}{\varepsilon_{tcc}} & \text{if } (\varepsilon_{tcc} > \varepsilon_{tc}) \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rc}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}} & \text{if } \left( \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}} > \varepsilon_{rc} \right) \cdot (A_{BAR} > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{ts}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}}} & \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} < \varepsilon_{ts} \right] \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rs}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}}} & \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}} < \varepsilon_{rs} \right] \cdot (A_{BAR} > 0) \\ \sigma_{cc} & \text{otherwise} \end{cases}$$

$$\sigma_{cd_q} := \sigma_{cd}(\varepsilon_{tcc_q}, q)$$

**CALCULATE FORCES AND MOMENTS AT EACH NEUTRAL AXIS LOCATION**

Calculate force in concrete:

$$F_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from concrete about column centroid:

$$M_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] \cdot y dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in rebar assuming design max stress in concrete:

$$y_{SY_q} := \begin{cases} y_{nbar} \cdot \frac{q}{ns + 1} & \text{if } (f_c = 0) \cdot (A_{BAR} > 0) \\ y_{SY_q} & \text{otherwise} \end{cases}$$

$$\epsilon_{S_{j,q}} := \begin{cases} \frac{y_{SY_q} - y_{Obar_j}}{y_{nbar} - y_{SY_q}} \cdot \epsilon_{cc}(f_c, \sigma_{cd_q}) & \text{if } f_c = 0 \\ \frac{y_{SY_q} - y_{Obar_j}}{H_{CY} - y_{SY_q}} \cdot \epsilon_{cc}(f_c, \sigma_{cd_q}) & \text{otherwise} \end{cases}$$

Calculate force in each rebar:

$$F_{S_{j,q}} := \begin{cases} \epsilon_{S_{j,q}} \cdot E_S \cdot A_{bar_j} & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total force in reinforcement:

$$F_{R_q} := \sum_j F_{S_{j,q}}$$

Calculate moment from reinforcement about section centroid:

$$M_{R_q} := \begin{cases} \sum_j -(\varepsilon_{S_{j,q}} E_S A_{bar_j} y_{bar_j}) & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in steel tube at extreme tension fiber:

$$\varepsilon_{tds_q} := \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate strain in steel tube at extreme compression fiber:

$$\varepsilon_{tdc_q} := \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate tensile force in steel tube:

$$F_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS} := \begin{cases} F_{TS1} - F_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate compressive force in steel tube:

$$F_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TC2_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TC} := \begin{cases} F_{TC1} - F_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from tensile force in steel tube:

$$M_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} -2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} -2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS} := \begin{cases} M_{TS1} - M_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from compressive force in steel tube:

$$M_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC2_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC} := \begin{cases} M_{TC1} - M_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total axial response from section:

$$F_T := F_C + F_R + F_{TS} + F_{TC}$$

$$F_{TC} := F_C$$

Calculate total moment response from section:

$$M_T := M_C + M_R + M_{TS} + M_{TC}$$

$$M_{TC} := M_C$$

**CALCULATE MAXIMUM ALLOWABLE AXIAL FORCE IN SECTION**

Limiting strain in axial  
compression:

$$\varepsilon_{cL} := \begin{cases} \min(\varepsilon_{cc}, \varepsilon_{tc}) & \text{if } (A_{BAR} = 0) \cdot (ts \neq 0) \cdot (f_c \neq 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}) & \text{if } (ts = 0) \cdot (A_{BAR} \neq 0) \cdot (f_c \neq 0) \\ \varepsilon_{tc} & \text{if } (A_{BAR} = 0) \cdot (f_c = 0) \\ \varepsilon_{rc} & \text{if } (ts = 0) \cdot (f_c = 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}, \varepsilon_{tc}) & \text{otherwise} \end{cases} \quad \varepsilon_{cL} = 0.001950$$

Limiting concrete stress in axial compression

$$\sigma_{cL} := \begin{cases} \sigma_{cd2} & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases} \quad \sigma_{cL} = 18.93 \text{ MPa}$$

$$P_{MAX} := \sigma_{cL} \cdot A_C (1 - \rho) + \varepsilon_{cL} \cdot E_S (A_{BAR} + A_{ST})$$

$$P_{MAX} = 21522.8 \text{ kN} \quad F_{T_1} := P_{MAX} \quad M_{T_1} := 0 \cdot \text{kN} \cdot \text{m}$$

$$P_{MAXC} := \sigma_{cL} \cdot A_C \cdot (1 - \rho)$$

$$P_{MAXC} = 17758.9 \text{ kN} \quad F_{TC_1} := P_{MAXC} \quad M_{TC_1} := 0 \cdot \text{kN} \cdot \text{m}$$

**CALCULATE MINIMUM ALLOWABLE AXIAL FORCE IN SECTION**

$$P_{MIN} := \begin{cases} \varepsilon_{rs} \cdot E_S (A_{BAR}) & \text{if } ts = 0 \\ \varepsilon_{ts} \cdot E_S (A_{ST}) & \text{if } A_{BAR} = 0 \\ \max(\varepsilon_{ts}, \varepsilon_{rs}) \cdot E_S (A_{BAR} + A_{ST}) & \text{otherwise} \end{cases}$$

$$P_{MIN} = -1640.7 \text{ kN} \quad F_{T_{ns+1}} := P_{MIN} \quad M_{T_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

$$\text{Limit} := \begin{cases} \min(P, F_T) \cdot 0.75 & \text{if } \min(P) > 0 \\ \min(P, F_T) \cdot 1.25 & \text{otherwise} \end{cases}$$

$$P_{MINC} := 0 \text{ kN} \quad M_{TC_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$



Diameter of Column  $D = 1100 \text{ mm}$

Percentage reinforcement  $\rho = 1.02 \%$

Thickness of CHS  $t_s = 0 \text{ mm}$

Characteristic strength of concrete

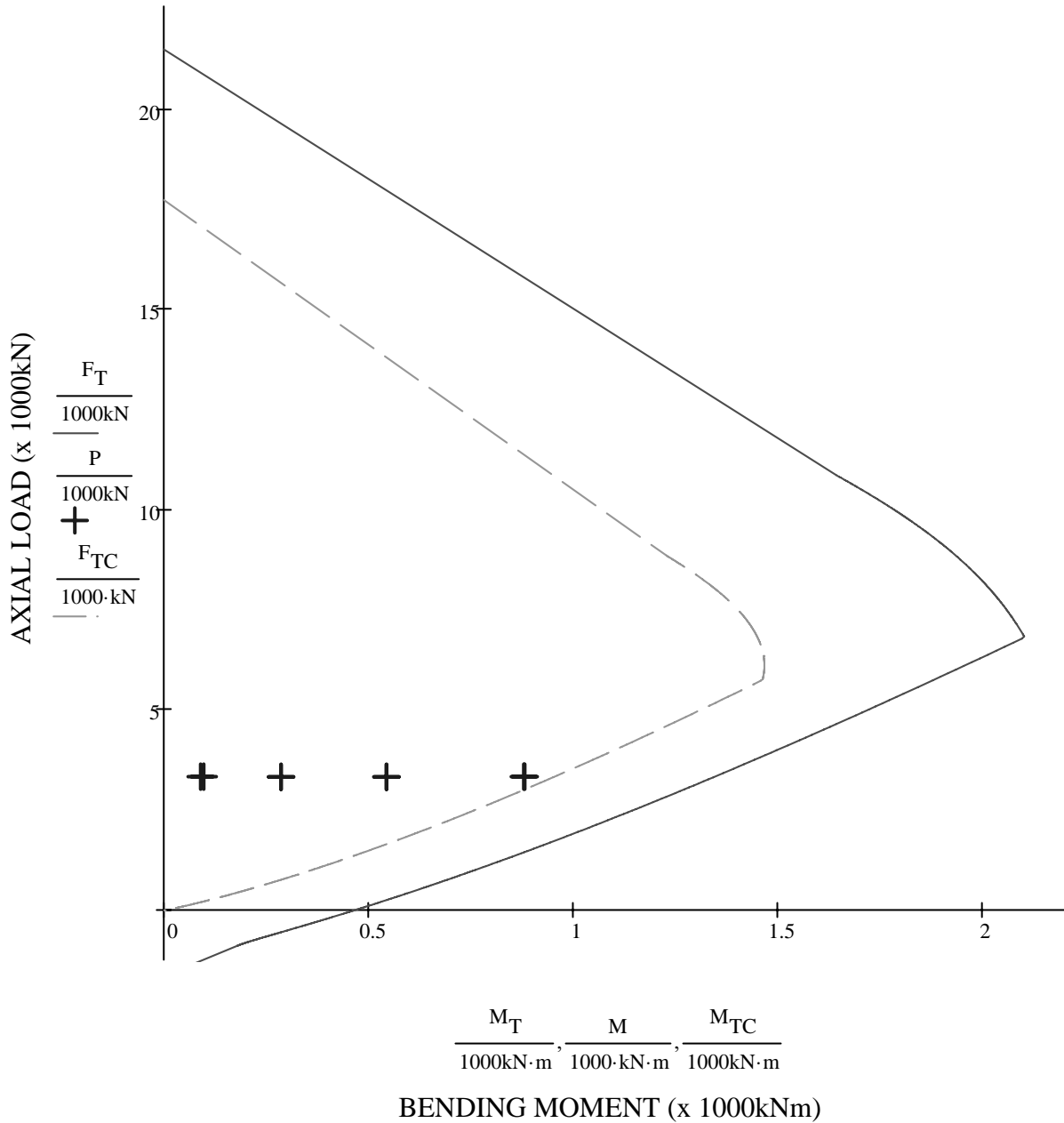
Yield Strength of Rebar

Yield Strength of CHS

$f_c = 30 \text{ MPa}$

$f_y = 390 \text{ MPa}$

$f_{ys} = 250 \text{ MPa}$



INTERACTION CURVE AT SERVICEABILITY LIMIT STATE

Equation of interaction line - upper region (between 1 and 2 calculation points)

$$m1 := \frac{M_{T_2} - M_{T_1}}{F_{T_2} - F_{T_1}} \quad c1 := F_{T_1}$$

Equation of interaction line - lower region (between ns and ns+1 calculation points)

$$m2 := \frac{M_{T_{ns}} - M_{T_{ns+1}}}{F_{T_{ns}} - F_{T_{ns+1}}} \quad c2 := F_{T_{ns+1}}$$

r := 1 .. 8

$$M_{SLS_r} := \begin{cases} 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r > F_{T_1} \\ 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r < F_{T_{ns+1}} \\ (P_r - c1) \cdot m1 & \text{if } (P_r > F_{T_2}) \cdot (P_r \leq F_{T_1}) \\ (P_r - c2) \cdot m2 & \text{if } (P_r \geq F_{T_{ns+1}}) \cdot (P_r < F_{T_{ns}}) \\ \text{otherwise} \\ \quad \begin{cases} j \leftarrow 1 \\ \text{while } F_{T_j} > P_r \\ \quad j \leftarrow j + 1 \\ M_{T_j} \end{cases} \end{cases}$$

$$\text{StressFactor}_r := \begin{cases} \text{"No Result"} & \text{if } M_{SLS_r} < 0.000000000000000001 \cdot \text{kN}\cdot\text{m} \\ \frac{M_r}{M_{SLS_r}} & \text{otherwise} \end{cases}$$

$$P = \begin{pmatrix} 3337 \\ 3337 \\ 3341 \\ 3341 \\ 3346 \\ 3346 \\ 3344 \\ 3344 \end{pmatrix} \text{ kN} \quad M = \begin{pmatrix} 287 \\ 544 \\ 287 \\ 545 \\ 880 \\ 90 \\ 883 \\ 98 \end{pmatrix} \text{ kN}\cdot\text{m} \quad M_{SLS} = \begin{pmatrix} 1343.2 \\ 1343.2 \\ 1343.2 \\ 1343.2 \\ 1343.2 \\ 1343.2 \\ 1343.2 \\ 1343.2 \end{pmatrix} \text{ kN}\cdot\text{m} \quad \text{StressFactor} = \begin{pmatrix} 0.214 \\ 0.405 \\ 0.213 \\ 0.406 \\ 0.655 \\ 0.067 \\ 0.657 \\ 0.073 \end{pmatrix}$$

**RESULTS SUMMARY**  
**SERVICEABILITY LIMIT STATE ANALYSIS OF CIRCULAR BEAM COLUMN**

Diameter of Column		1100	mm				
Percentage of rebar		1.02	%				
Load Case Ref	Pier	Applied Service Axial Load kN	Applied Service Bending Moment kNm	Service Limit State Bending Moment kNm	Allowable Stress Factor	Applied Stress Factor	Serviceability Limit State Design Result
1	P21	3337	287	1343.2	140%	21%	OK
2	P21	3337	544	1343.2	140%	41%	OK
3	P22	3341	287	1343.2	140%	21%	OK
4	P22	3341	545	1343.2	140%	41%	OK

**P3 SINGLE COLUMN 1.7 M DIAMETER**



**KATAHIRA & ENGINEERS  
INTERNATIONAL**

**Project:** Detailed Design Study of  
North Java Corridor Flyover Project

**Calculation:** Balaraja Flyover  
Serviceability Check - Full Live Load  
1700 mm Dia Circular RC Column - P3 Base Section

**Reference:** Project Specific Design Criteria

**Section Data**

MPa := 1000000·Pa

kN := 1000·N

Input Item		
Concrete Compressive Strength	$f_c$	30 MPa
Structural Steel Yield Strength	$f_{ys}$	250 MPa
Rebar Yield Strength	$f_y$	390 MPa
Diameter of reinforced concrete section	$D$	1700 mm
Thickness of CHS section	$t$	0 mm
Diameter of rebar - layer 1	$dia_1$	32 mm
Diameter of rebar - layer 2	$dia_2$	0 mm
Number bars - layer 1 (max 100)	$n_1$	64
Number bars - layer 2 (max 100)	$n_2$	0
Cover from face of section - layer 1	$cov_1$	60 mm
Cover from face of section - layer 2	$cov_2$	115 mm

**Load Data**

Ref	Pier	Load Case	P	M	Stress
			kN	kNm	Allowance
1	P30	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+CRSH	5809.4	299.5	140%
2	P30	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+CRSH	5809.4	277.2	140%

$$f_c := f_c \cdot \text{MPa} \quad f_{ys} := f_{ys} \cdot \text{MPa} \quad f_y := f_y \cdot \text{MPa} \quad D := D \cdot \text{mm} \quad t_s := t_s \cdot \text{mm}$$

$$\text{dia1} := \text{dia1} \cdot \text{mm} \quad \text{dia2} := \text{dia2} \cdot \text{mm} \quad \text{cov1} := \text{cov1} \cdot \text{mm} \quad \text{cov2} := \text{cov2} \cdot \text{mm}$$

$$P := P \cdot \text{kN} \quad M := M \cdot \text{kN} \cdot \text{m}$$

$$E_S := 200000 \cdot \text{MPa} \quad E_C := 4700 \sqrt{\frac{f_c}{\text{MPa}}} \cdot \text{MPa} \quad \text{Modular ratio} \quad \alpha := \begin{cases} \frac{E_S}{E_C} & \text{if } E_C > 0 \\ 1 & \text{otherwise} \end{cases} \quad \alpha = 7.77$$

$$E_C = 25743 \text{ MPa}$$

### Calculate Basic Allowable Stresses

Calculate rupture stress:

$$\sigma_{ct} := 0.5 \cdot \left( \frac{f_c}{\text{MPa}} \right)^{\frac{2}{3}} \cdot \text{MPa} \quad \sigma_{ct} = 4.8 \text{ MPa}$$

Calculate basic allowable stress of concrete

$$\sigma_{cc} := 1.0 \cdot f_c \quad \sigma_{cc} = 30.0 \text{ MPa}$$

Calculate basic allowable tensile stress of rebar

$$\sigma_{rs} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 170 \text{ MPa} \\ 170 \text{ MPa} & \text{otherwise} \end{cases} \quad \sigma_{rs} = 170 \text{ MPa}$$

Calculate basic allowable compressive stress of rebar

$$\sigma_{rc} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 110 \text{ MPa} \\ f_y & \text{otherwise} \end{cases} \quad \sigma_{rc} = 390 \text{ MPa}$$

Calculate basic allowable stress of structural steel

$$\sigma_{ts} := -0.6 f_{ys} \quad \sigma_{ts} = -150 \text{ MPa}$$

$$\sigma_{tc} := 1 f_{ys} \quad \sigma_{tc} = 250 \text{ MPa}$$

Limiting strain of rebar

$$\epsilon_{rs} := \frac{\sigma_{rs}}{E_S} \quad \epsilon_{rs} = -0.000850$$

$$\epsilon_{rc} := \frac{\sigma_{rc}}{E_S} \quad \epsilon_{rc} = 0.001950$$

Limiting strain of structural steel

$$\epsilon_{ts} := \frac{\sigma_{ts}}{E_S} \quad \epsilon_{ts} = -0.000750$$

$$\epsilon_{tc} := \frac{\sigma_{tc}}{E_S} \quad \epsilon_{tc} = 0.001250$$

### Concrete Cross Section Data - generated

n := 50      Number of Points - 50 points maximum

i := 1 .. n + 1      Range from 1 to n+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-850	26	0	850
2	-107	-843	27	107	843
3	-211	-823	28	211	823
4	-313	-790	29	313	790
5	-409	-745	30	409	745
6	-500	-688	31	500	688
7	-582	-620	32	582	620
8	-655	-542	33	655	542
9	-718	-455	34	718	455
10	-769	-362	35	769	362
11	-808	-263	36	808	263
12	-835	-159	37	835	159
13	-848	-53	38	848	53
14	-848	53	39	848	-53
15	-835	159	40	835	-159
16	-808	263	41	808	-263
17	-769	362	42	769	-362
18	-718	455	43	718	-455
19	-655	542	44	655	-542
20	-582	620	45	582	-620
21	-500	688	46	500	-688
22	-409	745	47	409	-745
23	-313	790	48	313	-790
24	-211	823	49	211	-823
25	-107	843	50	107	-843

k := 1 .. 25       $\overset{\text{XXXXXX}}{XS1} := XS1 \cdot \text{mm}$      $\overset{\text{XXXXXX}}{XS2} := XS2 \cdot \text{mm}$      $\overset{\text{XXXXXX}}{YS1} := YS1 \cdot \text{mm}$      $\overset{\text{XXXXXX}}{YS2} := YS2 \cdot \text{mm}$

$x_k := XS1_k$        $y_k := YS1_k$        $x_{k+25} := XS2_k$        $y_{k+25} := YS2_k$        $x_{n+1} := XS1_1$        $y_{n+1} := YS1_1$

### Calculate Section Properties of Concrete Section

$$A_C := - \sum_{i=1}^n \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{2} \right] \quad A_C = 2.26383 \text{ m}^2$$

$$x_C := - \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{y_{i+1} - y_i}{8} \cdot \left[ (x_{i+1} + x_i)^2 + \frac{(x_{i+1} - x_i)^2}{3} \right] \right] \quad x_C = 0 \text{ m}$$

$$y_C := \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{x_{i+1} - x_i}{8} \cdot \left[ (y_{i+1} + y_i)^2 + \frac{(y_{i+1} - y_i)^2}{3} \right] \right] \quad y_C = 0 \text{ m}$$

$$I_x := \sum_{i=1}^n \left[ \left[ (x_{i+1} - x_i) \cdot \frac{y_{i+1} + y_i}{24} \right] \cdot \left[ (y_{i+1} + y_i)^2 + (y_{i+1} - y_i)^2 \right] \right] \quad I_x = 0.40783 \text{ m}^4$$

$$I_y := - \sum_{i=1}^n \left[ \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{24} \right] \cdot \left[ (x_{i+1} + x_i)^2 + (x_{i+1} - x_i)^2 \right] \right] \quad I_y = 0.40783 \text{ m}^4$$

$$I_{xC} := I_x - A_C \cdot x_C^2 \quad I_{xC} = 0.40783 \text{ m}^4$$

$$I_{yC} := I_y - A_C \cdot y_C^2 \quad I_{yC} = 0.40783 \text{ m}^4$$



## Steel Tube Cross Section Data - generated from input

ns := 50      Number of Points - 50 points maximum

ps := 1 .. ns + 1      Range from 1 to ns+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-850	26	0	-850
2	-220	-821	27	220	-821
3	-425	-736	28	425	-736
4	-601	-601	29	601	-601
5	-736	-425	30	736	-425
6	-821	-220	31	821	-220
7	-850	0	32	850	0
8	-821	220	33	821	220
9	-736	425	34	736	425
10	-601	601	35	601	601
11	-425	736	36	425	736
12	-220	821	37	220	821
13	0	850	38	0	850
14	220	821	39	-220	821
15	425	736	40	-425	736
16	601	601	41	-601	601
17	736	425	42	-736	425
18	821	220	43	-821	220
19	850	0	44	-850	0
20	821	-220	45	-821	-220
21	736	-425	46	-736	-425
22	601	-601	47	-601	-601
23	425	-736	48	-425	-736
24	220	-821	49	-220	-821
25	0	-850	50	0	-850

$$\underline{\underline{XSS1}} := XSS1 \cdot \text{mm}$$

$$\underline{\underline{XSS2}} := XSS2 \cdot \text{mm}$$

$$\underline{\underline{YSS1}} := YSS1 \cdot \text{mm}$$

$$\underline{\underline{YSS2}} := YSS2 \cdot \text{mm}$$

z := 1 .. 25

$$x_{s_z} := XSS1_z$$

$$y_{s_z} := YSS1_z$$

z := 26 .. 50

$$x_{s_z} := XSS2_{z-25}$$

$$y_{s_z} := YSS2_{z-25}$$

$$x_{s_{ns+1}} := XSS1_1$$

$$y_{s_{ns+1}} := YSS1_1$$

### Calculate Section Properties of Steel Tube Section

$$A_{ST} := - \sum_{ps=1}^{ns} \left[ (y_{ps+1}^s - y_{ps}^s) \cdot \frac{x_{ps+1}^s + x_{ps}^s}{2} \right] \quad A_{ST} = 0 \text{ m}^2$$

$$x_{ST} := - \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{y_{ps+1}^s - y_{ps}^s}{8} \cdot \left[ (x_{ps+1}^s + x_{ps}^s)^2 + \frac{(x_{ps+1}^s - x_{ps}^s)^2}{3} \right] \right] \quad x_{ST} = -0.5 \text{ m}$$

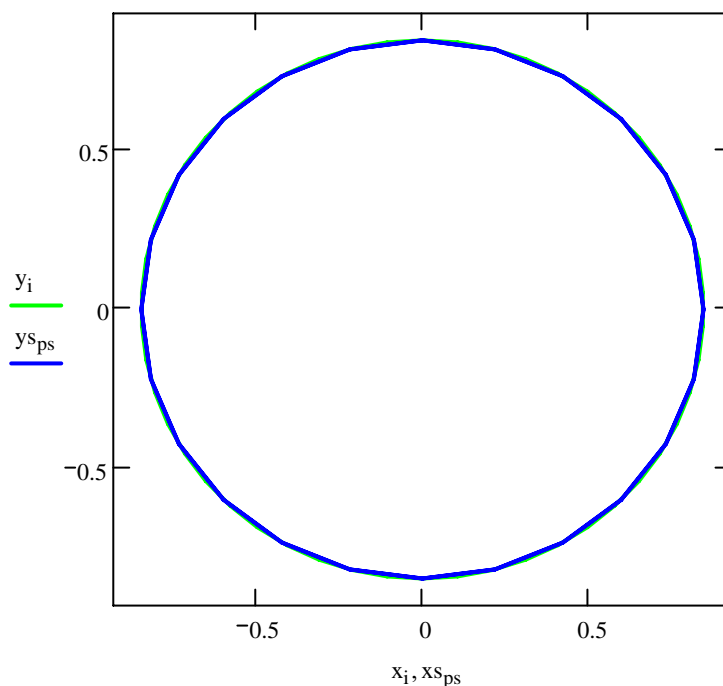
$$y_{ST} := \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{x_{ps+1}^s - x_{ps}^s}{8} \cdot \left[ (y_{ps+1}^s + y_{ps}^s)^2 + \frac{(y_{ps+1}^s - y_{ps}^s)^2}{3} \right] \right] \quad y_{ST} = -0.024 \text{ m}$$

$$I_{xS} := \sum_{ps=1}^{ns} \left[ \left[ (x_{ps+1}^s - x_{ps}^s) \cdot \frac{y_{ps+1}^s + y_{ps}^s}{24} \right] \cdot \left[ (y_{ps+1}^s + y_{ps}^s)^2 + (y_{ps+1}^s - y_{ps}^s)^2 \right] \right] \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := - \sum_{ps=1}^{ns} \left[ \left[ (y_{ps+1}^s - y_{ps}^s) \cdot \frac{x_{ps+1}^s + x_{ps}^s}{24} \right] \cdot \left[ (x_{ps+1}^s + x_{ps}^s)^2 + (x_{ps+1}^s - x_{ps}^s)^2 \right] \right] \quad I_{yS} = 0 \text{ m}^4$$

$$I_{xS} := I_{xS} - A_{ST} \cdot x_{ST}^2 \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := I_{yS} - A_{ST} \cdot y_{ST}^2 \quad I_{yS} = 0.00000 \text{ m}^4$$



**Rebar Data Layer 1 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	804	0	-774	51	804	759	-151
2	804	-76	-770	52	804	741	-225
3	804	-151	-759	53	804	715	-296
4	804	-225	-741	54	804	683	-365
5	804	-296	-715	55	804	644	-430
6	804	-365	-683	56	804	598	-491
7	804	-430	-644	57	804	547	-547
8	804	-491	-598	58	804	491	-598
9	804	-547	-547	59	804	430	-644
10	804	-598	-491	60	804	365	-683
11	804	-644	-430	61	804	296	-715
12	804	-683	-365	62	804	225	-741
13	804	-715	-296	63	804	151	-759
14	804	-741	-225	64	804	76	-770
15	804	-759	-151	65	0	0	0
16	804	-770	-76	66	0	0	0
17	804	-774	0	67	0	0	0
18	804	-770	76	68	0	0	0
19	804	-759	151	69	0	0	0
20	804	-741	225	70	0	0	0
21	804	-715	296	71	0	0	0
22	804	-683	365	72	0	0	0
23	804	-644	430	73	0	0	0
24	804	-598	491	74	0	0	0
25	804	-547	547	75	0	0	0
26	804	-491	598	76	0	0	0
27	804	-430	644	77	0	0	0
28	804	-365	683	78	0	0	0
29	804	-296	715	79	0	0	0
30	804	-225	741	80	0	0	0
31	804	-151	759	81	0	0	0
32	804	-76	770	82	0	0	0
33	804	0	774	83	0	0	0
34	804	76	770	84	0	0	0
35	804	151	759	85	0	0	0
36	804	225	741	86	0	0	0
37	804	296	715	87	0	0	0
38	804	365	683	88	0	0	0
39	804	430	644	89	0	0	0
40	804	491	598	90	0	0	0
41	804	547	547	91	0	0	0
42	804	598	491	92	0	0	0
43	804	644	430	93	0	0	0
44	804	683	365	94	0	0	0
45	804	715	296	95	0	0	0
46	804	741	225	96	0	0	0
47	804	759	151	97	0	0	0
48	804	770	76	98	0	0	0
49	804	774	0	99	0	0	0
50	804	770	-76	100	0	0	0

**Rebar Data Layer 2 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	0	0	0	51	0	0	0
2	0	0	0	52	0	0	0
3	0	0	0	53	0	0	0
4	0	0	0	54	0	0	0
5	0	0	0	55	0	0	0
6	0	0	0	56	0	0	0
7	0	0	0	57	0	0	0
8	0	0	0	58	0	0	0
9	0	0	0	59	0	0	0
10	0	0	0	60	0	0	0
11	0	0	0	61	0	0	0
12	0	0	0	62	0	0	0
13	0	0	0	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

$$\underline{A1}_j := A1 \cdot \text{mm}^2 \quad \underline{A2}_j := A2 \cdot \text{mm}^2 \quad \underline{A3}_j := A3 \cdot \text{mm}^2 \quad \underline{A4}_j := A4 \cdot \text{mm}^2$$

$$\underline{X1}_j := X1 \cdot \text{mm} \quad \underline{X2}_j := X2 \cdot \text{mm} \quad \underline{X3}_j := X3 \cdot \text{mm} \quad \underline{X4}_j := X4 \cdot \text{mm}$$

$$\underline{Y1}_j := Y1 \cdot \text{mm} \quad \underline{Y2}_j := Y2 \cdot \text{mm} \quad \underline{Y3}_j := Y3 \cdot \text{mm} \quad \underline{Y4}_j := Y4 \cdot \text{mm}$$

$$k := 1..50$$

$$A_{\text{bar}_k} := A1_k \quad x_{\text{bar}_k} := X1_k \quad y_{\text{bar}_k} := Y1_k$$

$$A_{\text{bar}_{k+50}} := A2_k \quad x_{\text{bar}_{k+50}} := X2_k \quad y_{\text{bar}_{k+50}} := Y2_k$$

$$A_{\text{bar}_{k+100}} := A3_k \quad x_{\text{bar}_{k+100}} := X3_k \quad y_{\text{bar}_{k+100}} := Y3_k$$

$$A_{\text{bar}_{k+150}} := A4_k \quad x_{\text{bar}_{k+150}} := X4_k \quad y_{\text{bar}_{k+150}} := Y4_k$$

### Calculate Section Properties of Reinforcement

$$A_{\text{BAR}} := \sum_{j=1}^{200} A_{\text{bar}_j} \quad A_{\text{BAR}} = 51472 \text{ mm}^2$$

$$\rho := \frac{A_{\text{BAR}}}{A_C} \quad \rho = 0.0227$$

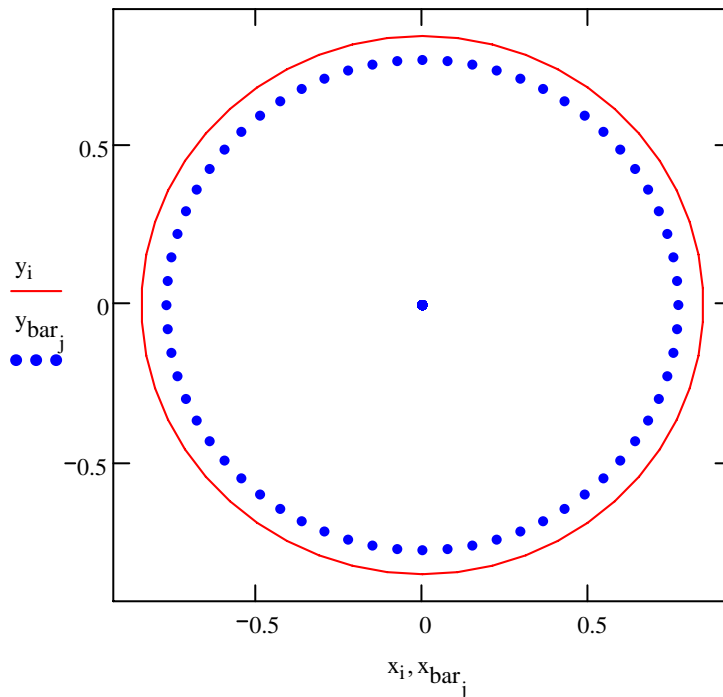
$$x_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot x_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad x_b = 0 \text{ m}$$

$$y_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot y_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad y_b = 0 \text{ m}$$

$$I_{x_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (x_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot x_b^2 \quad I_{x_b} = 0.01542 \text{ m}^4$$

$$I_{y_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (y_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot y_b^2 \quad I_{y_b} = 0.01542 \text{ m}^4$$

$j := 1 \dots 200$



**Calculate Composite Section Properties (before cracking)**

Effective area  $A_E := A_C \cdot [1 + \rho \cdot (\alpha - 1)] + A_{ST} \cdot \alpha$   $A_E = 2612250 \text{ mm}^2$

Effective centroid  $x_E := \frac{A_C \cdot [(1 - \rho) \cdot x_C + \rho \cdot x_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot x_{ST}}{A_E}$   $x_E = 0.000 \text{ m}$

$y_E := \frac{A_C \cdot [(1 - \rho) \cdot y_C + \rho \cdot y_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot y_{ST}}{A_E}$   $y_E = 0.000 \text{ m}$

Effective stiffness  $I_{EX} := I_{xC} + I_{xb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot x_C^2 + \rho \cdot x_b^2 \cdot \alpha] + (I_{xS} + A_{ST} \cdot x_{ST}^2) \cdot \alpha$   
 $I_{EX} = 1 \text{ m}^4$

$I_{EY} := I_{yC} + I_{yb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot y_C^2 + \rho \cdot y_b^2 \cdot \alpha] + (I_{yS} + A_{ST} \cdot y_{ST}^2) \cdot \alpha$   
 $I_{EY} = 1 \text{ m}^4$

Distance from extreme concrete fiber to centroid

$x_{F_{pos}} := \max(x - x_E)$   $x_{F_{neg}} := \min(x - x_E)$

$y_{F_{pos}} := \max(y - y_E)$   $y_{F_{neg}} := \min(y - y_E)$

Total depth of concrete section

$H_{CX} := x_{F_{pos}} - x_{F_{neg}}$   $H_{CX} = 2 \text{ m}$

$H_{CY} := y_{F_{pos}} - y_{F_{neg}}$   $H_{CY} = 2 \text{ m}$

Section modulus

$$Z_{Xpos} := \frac{I_{EX}}{xF_{pos}}$$

$$Z_{Xneg} := \frac{I_{EX}}{xF_{neg}}$$

$$Z_{Ypos} := \frac{I_{EY}}{yF_{pos}}$$

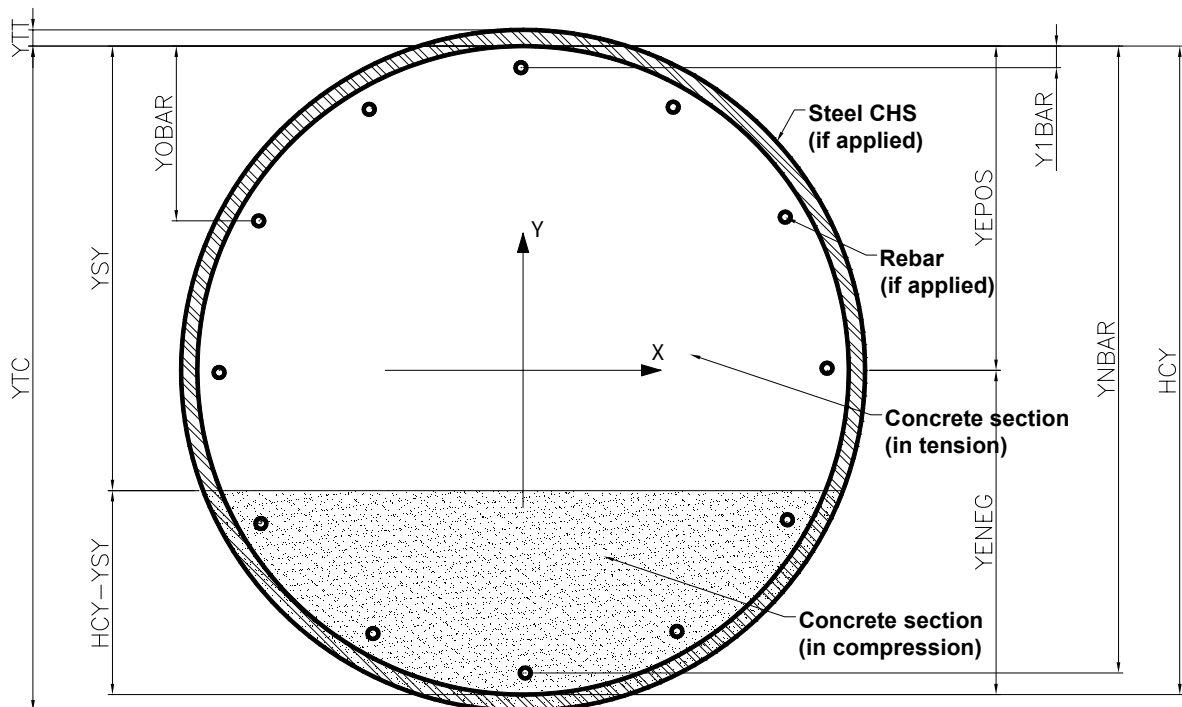
$$Z_{Yneg} := \frac{I_{EY}}{yF_{neg}}$$

Thickness of steel tube:

$$t_s := y_1 - y_{s1} \quad t_s = 0 \text{ mm}$$

**Establish Section Dimensions**

Positive case - determine coord of extreme concrete fiber	$y_{Epos} := \max(y)$	$y_{Epos} = 850 \text{ mm}$
Negative case - determine coord of extreme concrete fiber	$y_{Eneg} := \min(y)$	$y_{Eneg} = -850 \text{ mm}$
Offsets of rebar from extreme fiber	$y_{Obar} := y_{Epos} - y_{bar}$	
Determine most extreme rebar (minimum offset)	$y_{1bar} := \min(y_{Epos} - y_{bar})$	$y_{1bar} = 76 \text{ mm}$
Determine most extreme rebar (maximum offset)	$y_{nbar} := \max(y_{Epos} - y_{bar})$	$y_{nbar} = 1624 \text{ mm}$
Offsets of extreme steel tube fiber from extreme concrete fiber	$y_{tt} := t_s$	$y_{tt} = 0 \text{ mm}$
	$y_{tc} := H_{CY} + t_s$	$y_{tc} = 1700 \text{ mm}$



**ASSIGN NEUTRAL AXIS VALUES**

Number of sections to analysed  $ns := 500$

$q := 2..ns$

Distance of neutral axis from extreme fiber in tension  $y_{SY_q} := H_{CY} \cdot \frac{q}{ns + 1}$

**Calculate stresses and strains in reinforcement and concrete at extreme fibers**

Calculate strain at extreme compression fiber assuming max allowable stress in concrete:

Trial value of concrete strain

$$\epsilon_{cc} := \frac{\sigma_{cc}}{E_C} \cdot 2 \qquad \frac{\sigma_{cc}}{E_C} = 0.001165$$

Given

$$\sigma_{cc} = \epsilon_{cc} \cdot \left( 4700 \sqrt{\frac{f_c \cdot 2}{MPa}} - \frac{4700^2}{2.68} \cdot \epsilon_{cc} \right) \cdot MPa$$

$$\epsilon_{cc} := \text{Find}(\epsilon_{cc}) \qquad \epsilon_{cc} = 0.003321$$

$$\epsilon_{\text{max}} := \begin{cases} \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \epsilon_{cc} & \text{otherwise} \end{cases} \qquad \epsilon_{cc} = 0.003321$$

Strain at other stresses taken to be linear:

$$\epsilon_{cc}(f_c, \sigma_{cd}) := \begin{cases} \frac{\sigma_{cd}}{\sigma_{tc}} \cdot \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \frac{\sigma_{cd}}{\sigma_{rc}} \cdot \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \frac{\sigma_{cd}}{\sigma_{cc}} \cdot \epsilon_{cc} & \text{otherwise} \end{cases}$$

Calculate strain in steel tube assuming max allowable stress in concrete:

$$\begin{aligned} \text{In compression} \quad \epsilon_{tcc_q} &:= \epsilon_{cc} \cdot \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \\ \text{In tension} \quad \epsilon_{tct_q} &:= \epsilon_{cc} \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \end{aligned}$$



Calculate strain in rebar assuming max allowable stress in concrete:

$$\begin{array}{l} \text{In} \\ \text{compression} \end{array} \quad \varepsilon_{rcc_q} := \varepsilon_{cc} \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

$$\begin{array}{l} \text{In} \\ \text{tension} \end{array} \quad \varepsilon_{rct_q} := \varepsilon_{cc} \cdot \frac{y_{1bar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

Calculate design max stress in compression taking account of other limits:

$$\sigma_{cd}(\varepsilon_{tcc}, q) := \left\{ \begin{array}{l} \sigma_{cd} \leftarrow \sigma_{cc} \quad \text{if } f_c > 0 \\ \sigma_{cd} \leftarrow \sigma_{tc} \quad \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \sigma_{cd} \leftarrow \sigma_{rc} \quad \text{if } (f_c = 0) \cdot (ts = 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{tc}}{\varepsilon_{tcc}} \quad \text{if } (\varepsilon_{tcc} > \varepsilon_{tc}) \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rc}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}} \quad \text{if } \left( \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}} > \varepsilon_{rc} \right) \cdot (A_{BAR} > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{ts}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}}} \quad \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} < \varepsilon_{ts} \right] \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rs}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}}} \quad \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}} < \varepsilon_{rs} \right] \cdot (A_{BAR} > 0) \\ \sigma_{cc} \quad \text{otherwise} \end{array} \right.$$

$$\sigma_{cd_q} := \sigma_{cd}(\varepsilon_{tcc_q}, q)$$

**CALCULATE FORCES AND MOMENTS AT EACH NEUTRAL AXIS LOCATION**

Calculate force in concrete:

$$F_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from concrete about column centroid:

$$M_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] \cdot y dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in rebar assuming design max stress in concrete:

$$y_{SY_q} := \begin{cases} y_{nbar} \cdot \frac{q}{ns + 1} & \text{if } (f_c = 0) \cdot (A_{BAR} > 0) \\ y_{SY_q} & \text{otherwise} \end{cases}$$

$$\varepsilon_{S_{j,q}} := \begin{cases} \frac{y_{SY_q} - y_{Obar_j}}{y_{nbar} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{if } f_c = 0 \\ \frac{y_{SY_q} - y_{Obar_j}}{H_{CY} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{otherwise} \end{cases}$$

Calculate force in each rebar:

$$F_{S_{j,q}} := \begin{cases} \varepsilon_{S_{j,q}} \cdot E_S \cdot A_{bar_j} & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total force in reinforcement:

$$F_{R_q} := \sum_j F_{S_{j,q}}$$

Calculate moment from reinforcement about section centroid:

$$M_{R_q} := \begin{cases} \sum_j -(\varepsilon_{S_{j,q}} E_S A_{bar_j} \cdot y_{bar_j}) & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in steel tube at extreme tension fiber:

$$\varepsilon_{tds_q} := \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate strain in steel tube at extreme compression fiber:

$$\varepsilon_{tdc_q} := \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate tensile force in steel tube:

$$F_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS} := \begin{cases} F_{TS1} - F_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate compressive force in steel tube:

$$F_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TC2q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] dy$$

$$F_{TC} := \begin{cases} F_{TC1} - F_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from tensile force in steel tube:

$$M_{TS1q} := \int_{\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2} + y_{tt}} -2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{y_{SYq} + y_{tt}} \right] \cdot y dy$$

$$M_{TS2q} := \int_{\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} -2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{y_{SYq} + y_{tt}} \right] \cdot y dy$$

$$M_{TS} := \begin{cases} M_{TS1} - M_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from compressive force in steel tube:

$$M_{TC1q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] \cdot y dy$$

$$M_{TC2q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] \cdot y dy$$

$$M_{TC} := \begin{cases} M_{TC1} - M_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total axial response from section:

$$F_T := F_C + F_R + F_{TS} + F_{TC}$$

$$F_{TC} := F_C$$

Calculate total moment response from section:

$$M_T := M_C + M_R + M_{TS} + M_{TC}$$

$$M_{TC} := M_C$$

**CALCULATE MAXIMUM ALLOWABLE AXIAL FORCE IN SECTION**

Limiting strain in axial  
compression:

$$\varepsilon_{cL} := \begin{cases} \min(\varepsilon_{cc}, \varepsilon_{tc}) & \text{if } (A_{BAR} = 0) \cdot (ts \neq 0) \cdot (f_c \neq 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}) & \text{if } (ts = 0) \cdot (A_{BAR} \neq 0) \cdot (f_c \neq 0) \\ \varepsilon_{tc} & \text{if } (A_{BAR} = 0) \cdot (f_c = 0) \\ \varepsilon_{rc} & \text{if } (ts = 0) \cdot (f_c = 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}, \varepsilon_{tc}) & \text{otherwise} \end{cases} \quad \varepsilon_{cL} = 0.001950$$

Limiting concrete stress in axial compression

$$\sigma_{cL} := \begin{cases} \sigma_{cd2} & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases} \quad \sigma_{cL} = 18.44 \text{ MPa}$$

$$P_{MAX} := \sigma_{cL} \cdot A_C (1 - \rho) + \varepsilon_{cL} \cdot E_S (A_{BAR} + A_{ST})$$

$$P_{MAX} = 60878.4 \text{ kN} \quad F_{T_1} := P_{MAX} \quad M_{T_1} := 0 \cdot \text{kN} \cdot \text{m}$$

$$P_{MAXC} := \sigma_{cL} \cdot A_C \cdot (1 - \rho)$$

$$P_{MAXC} = 40804.4 \text{ kN} \quad F_{TC_1} := P_{MAXC} \quad M_{TC_1} := 0 \cdot \text{kN} \cdot \text{m}$$

**CALCULATE MINIMUM ALLOWABLE AXIAL FORCE IN SECTION**

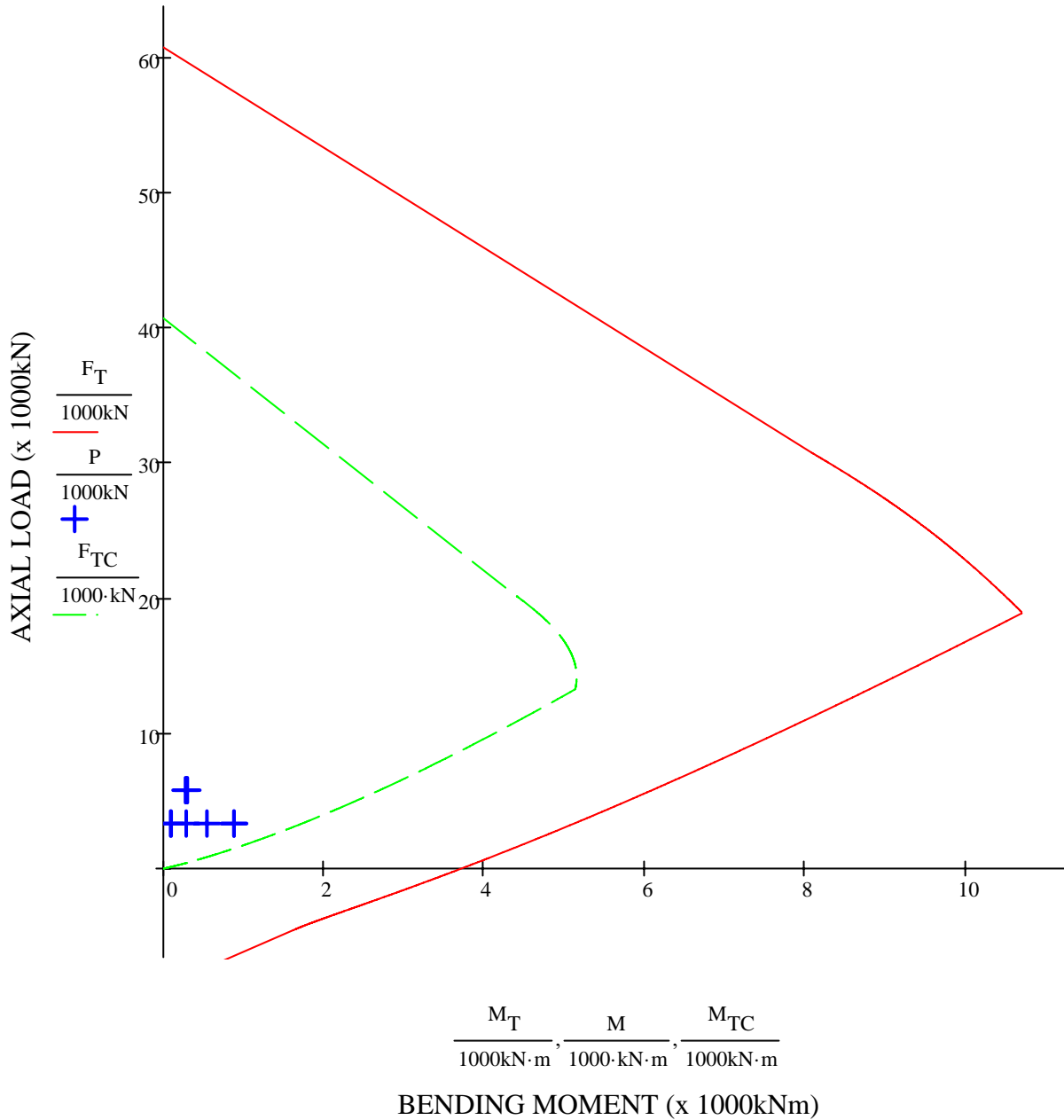
$$P_{MIN} := \begin{cases} \varepsilon_{rs} \cdot E_S (A_{BAR}) & \text{if } ts = 0 \\ \varepsilon_{ts} \cdot E_S (A_{ST}) & \text{if } A_{BAR} = 0 \\ \max(\varepsilon_{ts}, \varepsilon_{rs}) \cdot E_S (A_{BAR} + A_{ST}) & \text{otherwise} \end{cases}$$

$$P_{MIN} = -8750.2 \text{ kN} \quad F_{T_{ns+1}} := P_{MIN} \quad M_{T_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

$$\text{Limit} := \begin{cases} \min(P, F_T) \cdot 0.75 & \text{if } \min(P) > 0 \\ \min(P, F_T) \cdot 1.25 & \text{otherwise} \end{cases}$$

$$P_{MINC} := 0 \text{ kN} \quad M_{TC_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

Diameter of Column	D = 1700 mm	Characteristic strength of concrete	$f_c = 30 \text{ MPa}$
Percentage reinforcement	$\rho = 2.27 \%$	Yield Strength of Rebar	$f_y = 390 \text{ MPa}$
Thickness of CHS	$t_s = 0 \text{ mm}$	Yield Strength of CHS	$f_{ys} = 250 \text{ MPa}$



INTERACTION CURVE AT SERVICEABILITY LIMIT STATE

Equation of interaction line - upper region (between 1 and 2 calculation points)

$$m1 := \frac{M_{T_2} - M_{T_1}}{F_{T_2} - F_{T_1}} \quad c1 := F_{T_1}$$

Equation of interaction line - lower region (between ns and ns+1 calculation points)

$$m2 := \frac{M_{T_{ns}} - M_{T_{ns+1}}}{F_{T_{ns}} - F_{T_{ns+1}}} \quad c2 := F_{T_{ns+1}}$$

r := 1 .. 8

$$M_{SLS_r} := \begin{cases} 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r > F_{T_1} \\ 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r < F_{T_{ns+1}} \\ (P_r - c1) \cdot m1 & \text{if } (P_r > F_{T_2}) \cdot (P_r \leq F_{T_1}) \\ (P_r - c2) \cdot m2 & \text{if } (P_r \geq F_{T_{ns+1}}) \cdot (P_r < F_{T_{ns}}) \\ \text{otherwise} \\ \quad \begin{cases} j \leftarrow 1 \\ \text{while } F_{T_j} > P_r \\ \quad j \leftarrow j + 1 \\ \quad M_{T_j} \end{cases} \end{cases}$$

$$\text{StressFactor}_r := \begin{cases} \text{"No Result"} & \text{if } M_{SLS_r} < 0.000000000000000001 \cdot \text{kN}\cdot\text{m} \\ \frac{M_r}{M_{SLS_r}} & \text{otherwise} \end{cases}$$

$$P = \begin{pmatrix} 5809 \\ 5809 \\ 3341 \\ 3341 \\ 3346 \\ 3346 \\ 3344 \\ 3344 \end{pmatrix} \text{ kN} \quad M = \begin{pmatrix} 299 \\ 277 \\ 287 \\ 545 \\ 880 \\ 90 \\ 883 \\ 98 \end{pmatrix} \text{ kN}\cdot\text{m} \quad M_{SLS} = \begin{pmatrix} 6075.0 \\ 6075.0 \\ 5105.0 \\ 5105.0 \\ 5105.0 \\ 5105.0 \\ 5105.0 \\ 5105.0 \end{pmatrix} \text{ kN}\cdot\text{m} \quad \text{StressFactor} = \begin{pmatrix} 0.049 \\ 0.046 \\ 0.056 \\ 0.107 \\ 0.172 \\ 0.018 \\ 0.173 \\ 0.019 \end{pmatrix}$$



**RESULTS SUMMARY**  
**SERVICEABILITY LIMIT STATE ANALYSIS OF CIRCULAR BEAM COLUMN**

Diameter of Column		1700	mm				
Percentage of rebar		2.27	%				
Load Case Ref	Pier	Applied Service Axial Load kN	Applied Service Bending Moment kNm	Service Limit State Bending Moment kNm	Allowable Stress Factor	Applied Stress Factor	Serviceability Limit State Design Result
1	P30	5809	299	6075.0	140%	5%	OK
2	P30	5809	277	6075.0	140%	5%	OK



**KATAHIRA & ENGINEERS  
INTERNATIONAL**

**Project:** Detailed Design Study of  
North Java Corridor Flyover Project

**Calculation:** Balaraja Flyover  
Serviceability Check - Traffic Load Only  
1700 mm Dia Circular RC Column - P3 Base Section

**Reference:** Project Specific Design Criteria

**Section Data**

MPa := 1000000·Pa

kN := 1000·N

Input Item		
Concrete Compressive Strength	$f_c$	30 MPa
Structural Steel Yield Strength	$f_{ys}$	250 MPa
Rebar Yield Strength	$f_y$	390 MPa
Diameter of reinforced concrete section	$D$	1700 mm
Thickness of CHS section	$t$	0 mm
Diameter of rebar - layer 1	$dia_1$	32 mm
Diameter of rebar - layer 2	$dia_2$	0 mm
Number bars - layer 1 (max 100)	$n_1$	64
Number bars - layer 2 (max 100)	$n_2$	0
Cover from face of section - layer 1	$cov_1$	60 mm
Cover from face of section - layer 2	$cov_2$	115 mm

**Load Data**

Ref	Pier	Load Case	P	M	Stress
			kN	kNm	Allowance
1	P30	Combination 1 - P + Traffic Load Only	5278.4	2181.0	100%
2	P30	Combination 1 - P + Traffic Load Only	5278.4	2156.4	100%

$$f_c := f_c \cdot \text{MPa} \quad f_{ys} := f_{ys} \cdot \text{MPa} \quad f_y := f_y \cdot \text{MPa} \quad D := D \cdot \text{mm} \quad t_s := t_s \cdot \text{mm}$$

$$\text{dia1} := \text{dia1} \cdot \text{mm} \quad \text{dia2} := \text{dia2} \cdot \text{mm} \quad \text{cov1} := \text{cov1} \cdot \text{mm} \quad \text{cov2} := \text{cov2} \cdot \text{mm}$$

$$P := P \cdot \text{kN} \quad M := M \cdot \text{kN} \cdot \text{m}$$

$$E_S := 200000 \cdot \text{MPa} \quad E_C := 4700 \sqrt{\frac{f_c}{\text{MPa}}} \cdot \text{MPa} \quad \text{Modular ratio} \quad \alpha := \begin{cases} \frac{E_S}{E_C} & \text{if } E_C > 0 \\ 1 & \text{otherwise} \end{cases} \quad \alpha = 7.77$$

$$E_C = 25743 \text{ MPa}$$

### Calculate Basic Allowable Stresses

Calculate rupture stress:

$$\sigma_{ct} := 0.5 \cdot \left( \frac{f_c}{\text{MPa}} \right)^{\frac{2}{3}} \cdot \text{MPa} \quad \sigma_{ct} = 4.8 \text{ MPa}$$

Calculate basic allowable stress of concrete

$$\sigma_{cc} := 1.0 \cdot f_c \quad \sigma_{cc} = 30.0 \text{ MPa}$$

Calculate basic allowable tensile stress of rebar

$$\sigma_{rs} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 170 \text{ MPa} \\ 170 \text{ MPa} & \text{otherwise} \end{cases} \quad \sigma_{rs} = 170 \text{ MPa}$$

Calculate basic allowable compressive stress of rebar

$$\sigma_{rc} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 110 \text{ MPa} \\ f_y & \text{otherwise} \end{cases} \quad \sigma_{rc} = 390 \text{ MPa}$$

Calculate basic allowable stress of structural steel

$$\sigma_{ts} := -0.6 f_{ys} \quad \sigma_{ts} = -150 \text{ MPa}$$

$$\sigma_{tc} := 1 f_{ys} \quad \sigma_{tc} = 250 \text{ MPa}$$

Limiting strain of rebar

$$\epsilon_{rs} := \frac{\sigma_{rs}}{E_S} \quad \epsilon_{rs} = -0.000850$$

$$\epsilon_{rc} := \frac{\sigma_{rc}}{E_S} \quad \epsilon_{rc} = 0.001950$$

Limiting strain of structural steel

$$\epsilon_{ts} := \frac{\sigma_{ts}}{E_S} \quad \epsilon_{ts} = -0.000750$$

$$\epsilon_{tc} := \frac{\sigma_{tc}}{E_S} \quad \epsilon_{tc} = 0.001250$$

### Concrete Cross Section Data - generated

n := 50      Number of Points - 50 points maximum

i := 1 .. n + 1      Range from 1 to n+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-850	26	0	850
2	-107	-843	27	107	843
3	-211	-823	28	211	823
4	-313	-790	29	313	790
5	-409	-745	30	409	745
6	-500	-688	31	500	688
7	-582	-620	32	582	620
8	-655	-542	33	655	542
9	-718	-455	34	718	455
10	-769	-362	35	769	362
11	-808	-263	36	808	263
12	-835	-159	37	835	159
13	-848	-53	38	848	53
14	-848	53	39	848	-53
15	-835	159	40	835	-159
16	-808	263	41	808	-263
17	-769	362	42	769	-362
18	-718	455	43	718	-455
19	-655	542	44	655	-542
20	-582	620	45	582	-620
21	-500	688	46	500	-688
22	-409	745	47	409	-745
23	-313	790	48	313	-790
24	-211	823	49	211	-823
25	-107	843	50	107	-843

k := 1 .. 25       $\overset{\sim}{X}S1 := XS1 \cdot mm$      $\overset{\sim}{X}S2 := XS2 \cdot mm$      $\overset{\sim}{Y}S1 := YS1 \cdot mm$      $\overset{\sim}{Y}S2 := YS2 \cdot mm$

$x_k := XS1_k$        $y_k := YS1_k$        $x_{k+25} := XS2_k$        $y_{k+25} := YS2_k$        $x_{n+1} := XS1_1$        $y_{n+1} := YS1_1$

### Calculate Section Properties of Concrete Section

$$A_C := - \sum_{i=1}^n \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{2} \right] \quad A_C = 2.26383 \text{ m}^2$$

$$x_C := - \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{y_{i+1} - y_i}{8} \cdot \left[ (x_{i+1} + x_i)^2 + \frac{(x_{i+1} - x_i)^2}{3} \right] \right] \quad x_C = 0 \text{ m}$$

$$y_C := \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{x_{i+1} - x_i}{8} \cdot \left[ (y_{i+1} + y_i)^2 + \frac{(y_{i+1} - y_i)^2}{3} \right] \right] \quad y_C = 0 \text{ m}$$

$$I_x := \sum_{i=1}^n \left[ \left[ (x_{i+1} - x_i) \cdot \frac{y_{i+1} + y_i}{24} \right] \cdot \left[ (y_{i+1} + y_i)^2 + (y_{i+1} - y_i)^2 \right] \right] \quad I_x = 0.40783 \text{ m}^4$$

$$I_y := - \sum_{i=1}^n \left[ \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{24} \right] \cdot \left[ (x_{i+1} + x_i)^2 + (x_{i+1} - x_i)^2 \right] \right] \quad I_y = 0.40783 \text{ m}^4$$

$$I_{xC} := I_x - A_C \cdot x_C^2 \quad I_{xC} = 0.40783 \text{ m}^4$$

$$I_{yC} := I_y - A_C \cdot y_C^2 \quad I_{yC} = 0.40783 \text{ m}^4$$

## Steel Tube Cross Section Data - generated from input

ns := 50      Number of Points - 50 points maximum

ps := 1 .. ns + 1      Range from 1 to ns+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-850	26	0	-850
2	-220	-821	27	220	-821
3	-425	-736	28	425	-736
4	-601	-601	29	601	-601
5	-736	-425	30	736	-425
6	-821	-220	31	821	-220
7	-850	0	32	850	0
8	-821	220	33	821	220
9	-736	425	34	736	425
10	-601	601	35	601	601
11	-425	736	36	425	736
12	-220	821	37	220	821
13	0	850	38	0	850
14	220	821	39	-220	821
15	425	736	40	-425	736
16	601	601	41	-601	601
17	736	425	42	-736	425
18	821	220	43	-821	220
19	850	0	44	-850	0
20	821	-220	45	-821	-220
21	736	-425	46	-736	-425
22	601	-601	47	-601	-601
23	425	-736	48	-425	-736
24	220	-821	49	-220	-821
25	0	-850	50	0	-850

$$\underline{\underline{XSS1}} := XSS1 \cdot \text{mm}$$

$$\underline{\underline{XSS2}} := XSS2 \cdot \text{mm}$$

$$\underline{\underline{YSS1}} := YSS1 \cdot \text{mm}$$

$$\underline{\underline{YSS2}} := YSS2 \cdot \text{mm}$$

z := 1 .. 25

$$x_{s_z} := XSS1_z$$

$$y_{s_z} := YSS1_z$$

z := 26 .. 50

$$x_{s_z} := XSS2_{z-25}$$

$$y_{s_z} := YSS2_{z-25}$$

$$x_{s_{ns+1}} := XSS1_1$$

$$y_{s_{ns+1}} := YSS1_1$$

### Calculate Section Properties of Steel Tube Section

$$A_{ST} := - \sum_{ps=1}^{ns} \left[ (y_{ps+1}^s - y_{ps}^s) \cdot \frac{x_{ps+1}^s + x_{ps}^s}{2} \right] \quad A_{ST} = 0 \text{ m}^2$$

$$x_{ST} := - \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{y_{ps+1}^s - y_{ps}^s}{8} \cdot \left[ (x_{ps+1}^s + x_{ps}^s)^2 + \frac{(x_{ps+1}^s - x_{ps}^s)^2}{3} \right] \right] \quad x_{ST} = -0.5 \text{ m}$$

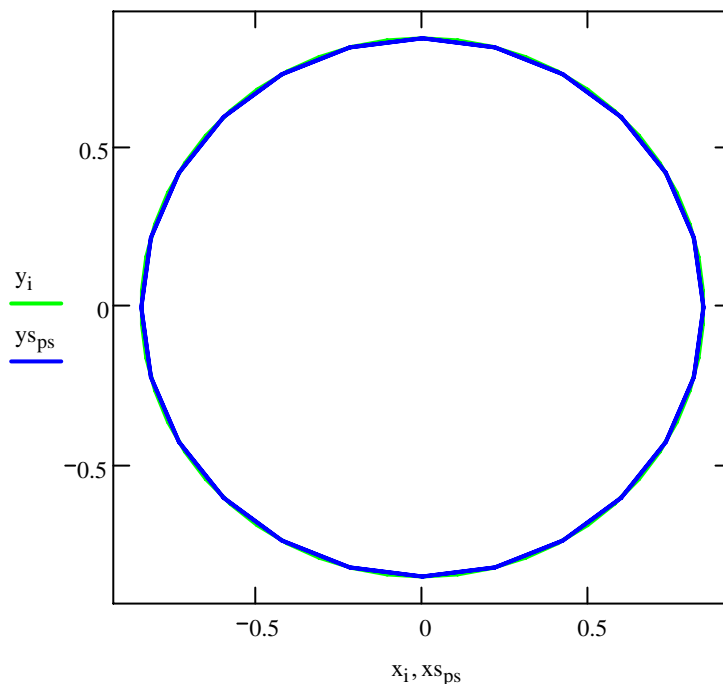
$$y_{ST} := \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{x_{ps+1}^s - x_{ps}^s}{8} \cdot \left[ (y_{ps+1}^s + y_{ps}^s)^2 + \frac{(y_{ps+1}^s - y_{ps}^s)^2}{3} \right] \right] \quad y_{ST} = -0.024 \text{ m}$$

$$I_{xS} := \sum_{ps=1}^{ns} \left[ \left[ (x_{ps+1}^s - x_{ps}^s) \cdot \frac{y_{ps+1}^s + y_{ps}^s}{24} \right] \cdot \left[ (y_{ps+1}^s + y_{ps}^s)^2 + (y_{ps+1}^s - y_{ps}^s)^2 \right] \right] \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := - \sum_{ps=1}^{ns} \left[ \left[ (y_{ps+1}^s - y_{ps}^s) \cdot \frac{x_{ps+1}^s + x_{ps}^s}{24} \right] \cdot \left[ (x_{ps+1}^s + x_{ps}^s)^2 + (x_{ps+1}^s - x_{ps}^s)^2 \right] \right] \quad I_{yS} = 0 \text{ m}^4$$

$$I_{xxS} := I_{xS} - A_{ST} \cdot x_{ST}^2 \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yyS} := I_{yS} - A_{ST} \cdot y_{ST}^2 \quad I_{yS} = 0.00000 \text{ m}^4$$



**Rebar Data Layer 1 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	804	0	-774	51	804	759	-151
2	804	-76	-770	52	804	741	-225
3	804	-151	-759	53	804	715	-296
4	804	-225	-741	54	804	683	-365
5	804	-296	-715	55	804	644	-430
6	804	-365	-683	56	804	598	-491
7	804	-430	-644	57	804	547	-547
8	804	-491	-598	58	804	491	-598
9	804	-547	-547	59	804	430	-644
10	804	-598	-491	60	804	365	-683
11	804	-644	-430	61	804	296	-715
12	804	-683	-365	62	804	225	-741
13	804	-715	-296	63	804	151	-759
14	804	-741	-225	64	804	76	-770
15	804	-759	-151	65	0	0	0
16	804	-770	-76	66	0	0	0
17	804	-774	0	67	0	0	0
18	804	-770	76	68	0	0	0
19	804	-759	151	69	0	0	0
20	804	-741	225	70	0	0	0
21	804	-715	296	71	0	0	0
22	804	-683	365	72	0	0	0
23	804	-644	430	73	0	0	0
24	804	-598	491	74	0	0	0
25	804	-547	547	75	0	0	0
26	804	-491	598	76	0	0	0
27	804	-430	644	77	0	0	0
28	804	-365	683	78	0	0	0
29	804	-296	715	79	0	0	0
30	804	-225	741	80	0	0	0
31	804	-151	759	81	0	0	0
32	804	-76	770	82	0	0	0
33	804	0	774	83	0	0	0
34	804	76	770	84	0	0	0
35	804	151	759	85	0	0	0
36	804	225	741	86	0	0	0
37	804	296	715	87	0	0	0
38	804	365	683	88	0	0	0
39	804	430	644	89	0	0	0
40	804	491	598	90	0	0	0
41	804	547	547	91	0	0	0
42	804	598	491	92	0	0	0
43	804	644	430	93	0	0	0
44	804	683	365	94	0	0	0
45	804	715	296	95	0	0	0
46	804	741	225	96	0	0	0
47	804	759	151	97	0	0	0
48	804	770	76	98	0	0	0
49	804	774	0	99	0	0	0
50	804	770	-76	100	0	0	0



**Rebar Data Layer 2 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	0	0	0	51	0	0	0
2	0	0	0	52	0	0	0
3	0	0	0	53	0	0	0
4	0	0	0	54	0	0	0
5	0	0	0	55	0	0	0
6	0	0	0	56	0	0	0
7	0	0	0	57	0	0	0
8	0	0	0	58	0	0	0
9	0	0	0	59	0	0	0
10	0	0	0	60	0	0	0
11	0	0	0	61	0	0	0
12	0	0	0	62	0	0	0
13	0	0	0	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

$$\underline{A1}_k := A1 \cdot \text{mm}^2 \quad \underline{A2}_k := A2 \cdot \text{mm}^2 \quad \underline{A3}_k := A3 \cdot \text{mm}^2 \quad \underline{A4}_k := A4 \cdot \text{mm}^2$$

$$\underline{X1}_k := X1 \cdot \text{mm} \quad \underline{X2}_k := X2 \cdot \text{mm} \quad \underline{X3}_k := X3 \cdot \text{mm} \quad \underline{X4}_k := X4 \cdot \text{mm}$$

$$\underline{Y1}_k := Y1 \cdot \text{mm} \quad \underline{Y2}_k := Y2 \cdot \text{mm} \quad \underline{Y3}_k := Y3 \cdot \text{mm} \quad \underline{Y4}_k := Y4 \cdot \text{mm}$$

$$k := 1..50$$

$$A_{\text{bar}_k} := A1_k \quad x_{\text{bar}_k} := X1_k \quad y_{\text{bar}_k} := Y1_k$$

$$A_{\text{bar}_{k+50}} := A2_k \quad x_{\text{bar}_{k+50}} := X2_k \quad y_{\text{bar}_{k+50}} := Y2_k$$

$$A_{\text{bar}_{k+100}} := A3_k \quad x_{\text{bar}_{k+100}} := X3_k \quad y_{\text{bar}_{k+100}} := Y3_k$$

$$A_{\text{bar}_{k+150}} := A4_k \quad x_{\text{bar}_{k+150}} := X4_k \quad y_{\text{bar}_{k+150}} := Y4_k$$

### Calculate Section Properties of Reinforcement

$$A_{\text{BAR}} := \sum_{j=1}^{200} A_{\text{bar}_j} \quad A_{\text{BAR}} = 51472 \text{ mm}^2$$

$$\rho := \frac{A_{\text{BAR}}}{A_C} \quad \rho = 0.0227$$

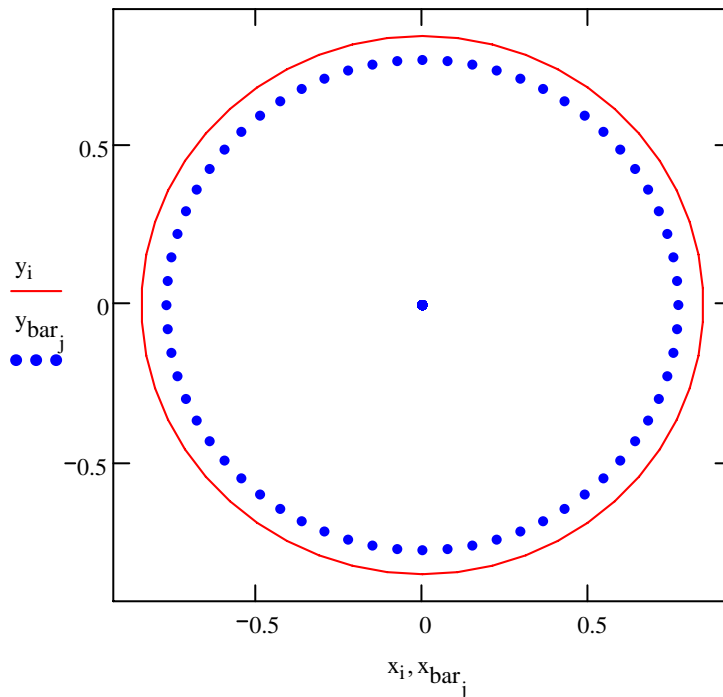
$$x_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot x_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad x_b = 0 \text{ m}$$

$$y_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot y_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad y_b = 0 \text{ m}$$

$$I_{x_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (x_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot x_b^2 \quad I_{x_b} = 0.01542 \text{ m}^4$$

$$I_{y_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (y_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot y_b^2 \quad I_{y_b} = 0.01542 \text{ m}^4$$

$j := 1 \dots 200$



**Calculate Composite Section Properties (before cracking)**

Effective area  $A_E := A_C \cdot [1 + \rho \cdot (\alpha - 1)] + A_{ST} \cdot \alpha$   $A_E = 2612250 \text{ mm}^2$

Effective centroid  $x_E := \frac{A_C \cdot [(1 - \rho) \cdot x_C + \rho \cdot x_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot x_{ST}}{A_E}$   $x_E = 0.000 \text{ m}$

$y_E := \frac{A_C \cdot [(1 - \rho) \cdot y_C + \rho \cdot y_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot y_{ST}}{A_E}$   $y_E = 0.000 \text{ m}$

Effective stiffness  $I_{EX} := I_{xC} + I_{xb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot x_C^2 + \rho \cdot x_b^2 \cdot \alpha] + (I_{xS} + A_{ST} \cdot x_{ST}^2) \cdot \alpha$   
 $I_{EX} = 1 \text{ m}^4$

$I_{EY} := I_{yC} + I_{yb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot y_C^2 + \rho \cdot y_b^2 \cdot \alpha] + (I_{yS} + A_{ST} \cdot y_{ST}^2) \cdot \alpha$   
 $I_{EY} = 1 \text{ m}^4$

Distance from extreme concrete fiber to centroid

$x_{F_{pos}} := \max(x - x_E)$   $x_{F_{neg}} := \min(x - x_E)$

$y_{F_{pos}} := \max(y - y_E)$   $y_{F_{neg}} := \min(y - y_E)$

Total depth of concrete section

$H_{CX} := x_{F_{pos}} - x_{F_{neg}}$   $H_{CX} = 2 \text{ m}$

$H_{CY} := y_{F_{pos}} - y_{F_{neg}}$   $H_{CY} = 2 \text{ m}$

Section modulus

$$Z_{Xpos} := \frac{I_{EX}}{xF_{pos}}$$

$$Z_{Xneg} := \frac{I_{EX}}{xF_{neg}}$$

$$Z_{Ypos} := \frac{I_{EY}}{yF_{pos}}$$

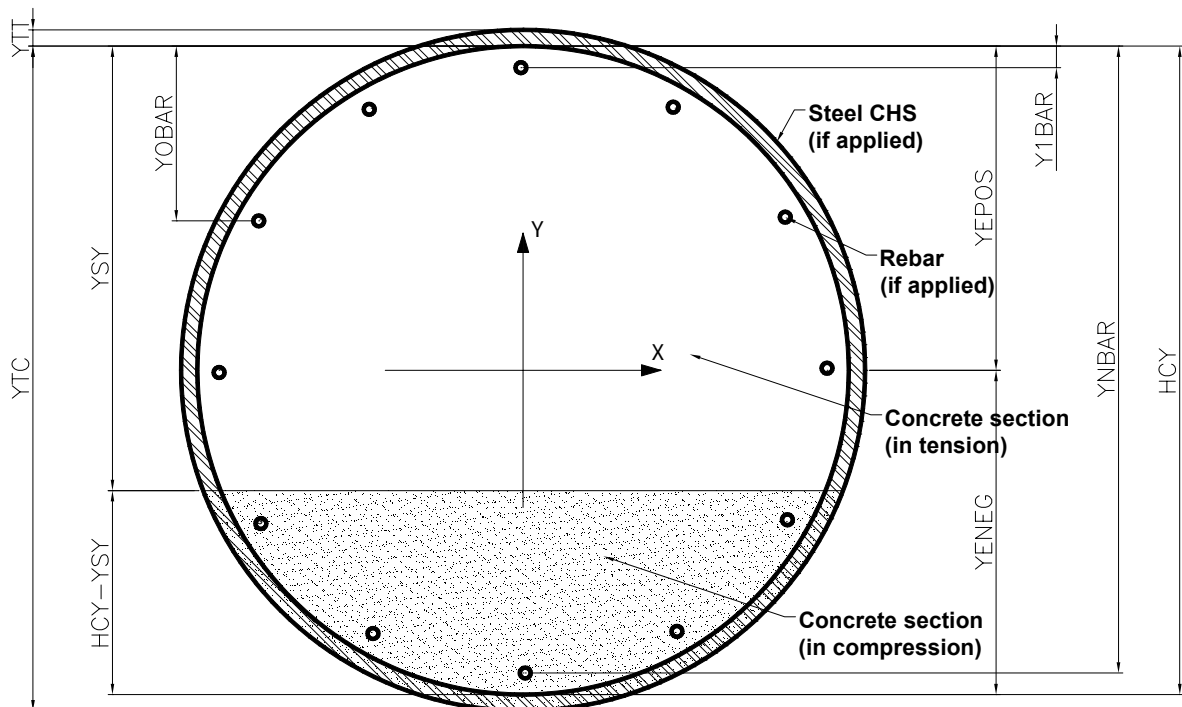
$$Z_{Yneg} := \frac{I_{EY}}{yF_{neg}}$$

Thickness of steel tube:

$$ts := y_1 - ys_1 \quad ts = 0 \text{ mm}$$

**Establish Section Dimensions**

Positive case - determine coord of extreme concrete fiber	$y_{Epos} := \max(y)$	$y_{Epos} = 850 \text{ mm}$
Negative case - determine coord of extreme concrete fiber	$y_{Eneg} := \min(y)$	$y_{Eneg} = -850 \text{ mm}$
Offsets of rebar from extreme fiber	$y_{Obar} := y_{Epos} - y_{bar}$	
Determine most extreme rebar (minimum offset)	$y_{1bar} := \min(y_{Epos} - y_{bar})$	$y_{1bar} = 76 \text{ mm}$
Determine most extreme rebar (maximum offset)	$y_{nbar} := \max(y_{Epos} - y_{bar})$	$y_{nbar} = 1624 \text{ mm}$
Offsets of extreme steel tube fiber from extreme concrete fiber	$y_{tt} := ts$	$y_{tt} = 0 \text{ mm}$
	$y_{tc} := H_{CY} + ts$	$y_{tc} = 1700 \text{ mm}$



**ASSIGN NEUTRAL AXIS VALUES**

Number of sections to analysed  $ns := 500$

$q := 2..ns$

Distance of neutral axis from extreme fiber in tension  $y_{SY_q} := H_{CY} \cdot \frac{q}{ns + 1}$

**Calculate stresses and strains in reinforcement and concrete at extreme fibers**

Calculate strain at extreme compression fiber assuming max allowable stress in concrete:

Trial value of concrete strain

$$\epsilon_{cc} := \frac{\sigma_{cc}}{E_C} \cdot 2 \qquad \frac{\sigma_{cc}}{E_C} = 0.001165$$

Given

$$\sigma_{cc} = \epsilon_{cc} \cdot \left( 4700 \sqrt{\frac{f_c \cdot 2}{MPa}} - \frac{4700^2}{2.68} \cdot \epsilon_{cc} \right) \cdot MPa$$

$$\epsilon_{cc} := \text{Find}(\epsilon_{cc}) \qquad \epsilon_{cc} = 0.003321$$

$$\epsilon_{\text{max}} := \begin{cases} \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \epsilon_{cc} & \text{otherwise} \end{cases} \qquad \epsilon_{cc} = 0.003321$$

Strain at other stresses taken to be linear:

$$\epsilon_{cc}(f_c, \sigma_{cd}) := \begin{cases} \frac{\sigma_{cd}}{\sigma_{tc}} \cdot \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \frac{\sigma_{cd}}{\sigma_{rc}} \cdot \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \frac{\sigma_{cd}}{\sigma_{cc}} \cdot \epsilon_{cc} & \text{otherwise} \end{cases}$$

Calculate strain in steel tube assuming max allowable stress in concrete:

$$\begin{aligned} \text{In compression} \quad \epsilon_{tcc_q} &:= \epsilon_{cc} \cdot \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \\ \text{In tension} \quad \epsilon_{tct_q} &:= \epsilon_{cc} \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \end{aligned}$$

Calculate strain in rebar assuming max allowable stress in concrete:

$$\begin{array}{l} \text{In} \\ \text{compression} \end{array} \quad \varepsilon_{rcc_q} := \varepsilon_{cc} \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

$$\begin{array}{l} \text{In} \\ \text{tension} \end{array} \quad \varepsilon_{rct_q} := \varepsilon_{cc} \cdot \frac{y_{1bar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

Calculate design max stress in compression taking account of other limits:

$$\sigma_{cd}(\varepsilon_{tcc}, q) := \left\{ \begin{array}{l} \sigma_{cd} \leftarrow \sigma_{cc} \quad \text{if } f_c > 0 \\ \sigma_{cd} \leftarrow \sigma_{tc} \quad \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \sigma_{cd} \leftarrow \sigma_{rc} \quad \text{if } (f_c = 0) \cdot (ts = 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{tc}}{\varepsilon_{tcc}} \quad \text{if } (\varepsilon_{tcc} > \varepsilon_{tc}) \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rc}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}} \quad \text{if } \left( \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}} > \varepsilon_{rc} \right) \cdot (A_{BAR} > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{ts}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}}} \quad \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} < \varepsilon_{ts} \right] \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rs}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}}} \quad \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}} < \varepsilon_{rs} \right] \cdot (A_{BAR} > 0) \\ \sigma_{cc} \quad \text{otherwise} \end{array} \right.$$

$$\sigma_{cd_q} := \sigma_{cd}(\varepsilon_{tcc_q}, q)$$

**CALCULATE FORCES AND MOMENTS AT EACH NEUTRAL AXIS LOCATION**

Calculate force in concrete:

$$F_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from concrete about column centroid:

$$M_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] \cdot y dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in rebar assuming design max stress in concrete:

$$y_{SY_q} := \begin{cases} y_{nbar} \cdot \frac{q}{ns + 1} & \text{if } (f_c = 0) \cdot (A_{BAR} > 0) \\ y_{SY_q} & \text{otherwise} \end{cases}$$

$$\varepsilon_{S_{j,q}} := \begin{cases} \frac{y_{SY_q} - y_{Obar_j}}{y_{nbar} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{if } f_c = 0 \\ \frac{y_{SY_q} - y_{Obar_j}}{H_{CY} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{otherwise} \end{cases}$$

Calculate force in each rebar:

$$F_{S_{j,q}} := \begin{cases} \varepsilon_{S_{j,q}} \cdot E_S \cdot A_{bar_j} & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total force in reinforcement:

$$F_{R_q} := \sum_j F_{S_{j,q}}$$

Calculate moment from reinforcement about section centroid:

$$M_{R_q} := \begin{cases} \sum_j -(\varepsilon_{S_{j,q}} \cdot E_S \cdot A_{bar_j} \cdot y_{bar_j}) & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in steel tube at extreme tension fiber:

$$\varepsilon_{tds_q} := \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate strain in steel tube at extreme compression fiber:

$$\varepsilon_{tdc_q} := \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate tensile force in steel tube:

$$F_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS} := \begin{cases} F_{TS1} - F_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate compressive force in steel tube:

$$F_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$



$$F_{TC2q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] dy$$

$$F_{TC} := \begin{cases} F_{TC1} - F_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from tensile force in steel tube:

$$M_{TS1q} := \int_{\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2} + y_{tt}} -2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS2q} := \int_{\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} -2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS} := \begin{cases} M_{TS1} - M_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from compressive force in steel tube:

$$M_{TC1q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC2q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC} := \begin{cases} M_{TC1} - M_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total axial response from section:

$$F_T := F_C + F_R + F_{TS} + F_{TC}$$

$$F_{TC} := F_C$$

Calculate total moment response from section:

$$M_T := M_C + M_R + M_{TS} + M_{TC}$$

$$M_{TC} := M_C$$

**CALCULATE MAXIMUM ALLOWABLE AXIAL FORCE IN SECTION**

Limiting strain in axial  
compression:

$$\varepsilon_{cL} := \begin{cases} \min(\varepsilon_{cc}, \varepsilon_{tc}) & \text{if } (A_{BAR} = 0) \cdot (ts \neq 0) \cdot (f_c \neq 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}) & \text{if } (ts = 0) \cdot (A_{BAR} \neq 0) \cdot (f_c \neq 0) \\ \varepsilon_{tc} & \text{if } (A_{BAR} = 0) \cdot (f_c = 0) \\ \varepsilon_{rc} & \text{if } (ts = 0) \cdot (f_c = 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}, \varepsilon_{tc}) & \text{otherwise} \end{cases} \quad \varepsilon_{cL} = 0.001950$$

Limiting concrete stress in axial compression

$$\sigma_{cL} := \begin{cases} \sigma_{cd2} & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases} \quad \sigma_{cL} = 18.44 \text{ MPa}$$

$$P_{MAX} := \sigma_{cL} \cdot A_C (1 - \rho) + \varepsilon_{cL} \cdot E_S (A_{BAR} + A_{ST})$$

$$P_{MAX} = 60878.4 \text{ kN} \quad F_{T_1} := P_{MAX} \quad M_{T_1} := 0 \cdot \text{kN} \cdot \text{m}$$

$$P_{MAXC} := \sigma_{cL} \cdot A_C \cdot (1 - \rho)$$

$$P_{MAXC} = 40804.4 \text{ kN} \quad F_{TC_1} := P_{MAXC} \quad M_{TC_1} := 0 \cdot \text{kN} \cdot \text{m}$$

**CALCULATE MINIMUM ALLOWABLE AXIAL FORCE IN SECTION**

$$P_{MIN} := \begin{cases} \varepsilon_{rs} \cdot E_S (A_{BAR}) & \text{if } ts = 0 \\ \varepsilon_{ts} \cdot E_S (A_{ST}) & \text{if } A_{BAR} = 0 \\ \max(\varepsilon_{ts}, \varepsilon_{rs}) \cdot E_S (A_{BAR} + A_{ST}) & \text{otherwise} \end{cases}$$

$$P_{MIN} = -8750.2 \text{ kN} \quad F_{T_{ns+1}} := P_{MIN} \quad M_{T_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

$$\text{Limit} := \begin{cases} \min(P, F_T) \cdot 0.75 & \text{if } \min(P) > 0 \\ \min(P, F_T) \cdot 1.25 & \text{otherwise} \end{cases}$$

$$P_{MINC} := 0 \text{ kN} \quad M_{TC_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

Diameter of Column  $D = 1700 \text{ mm}$

Characteristic strength of concrete

$f_c = 30 \text{ MPa}$

Percentage reinforcement  $\rho = 2.27 \%$

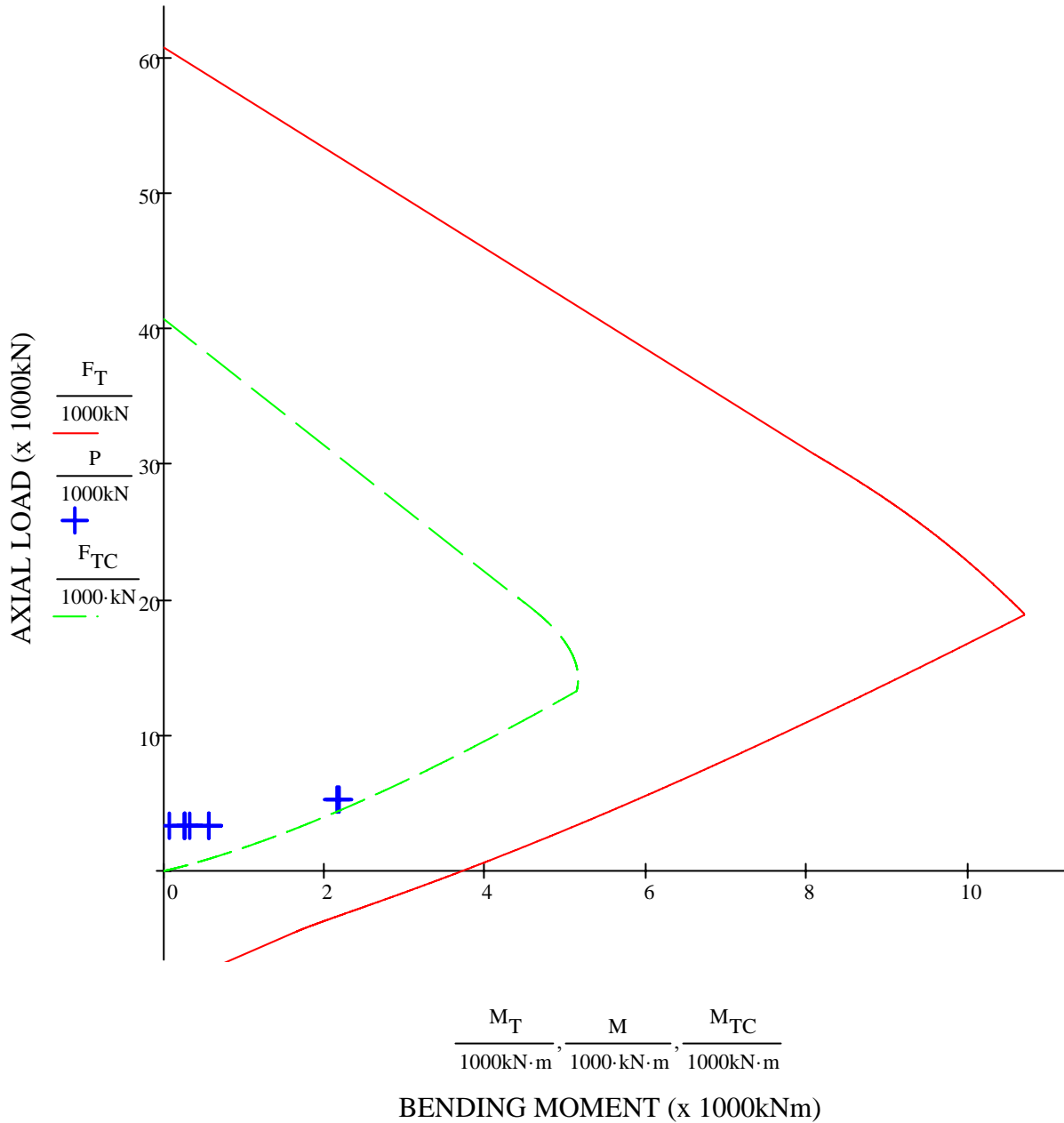
Yield Strength of Rebar

$f_y = 390 \text{ MPa}$

Thickness of CHS  $t_s = 0 \text{ mm}$

Yield Strength of CHS

$f_{ys} = 250 \text{ MPa}$



INTERACTION CURVE AT SERVICEABILITY LIMIT STATE

Equation of interaction line - upper region (between 1 and 2 calculation points)

$$m1 := \frac{M_{T_2} - M_{T_1}}{F_{T_2} - F_{T_1}} \quad c1 := F_{T_1}$$

Equation of interaction line - lower region (between ns and ns+1 calculation points)

$$m2 := \frac{M_{T_{ns}} - M_{T_{ns+1}}}{F_{T_{ns}} - F_{T_{ns+1}}} \quad c2 := F_{T_{ns+1}}$$

r := 1 .. 8

$$M_{SLS_r} := \begin{cases} 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r > F_{T_1} \\ 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r < F_{T_{ns+1}} \\ (P_r - c1) \cdot m1 & \text{if } (P_r > F_{T_2}) \cdot (P_r \leq F_{T_1}) \\ (P_r - c2) \cdot m2 & \text{if } (P_r \geq F_{T_{ns+1}}) \cdot (P_r < F_{T_{ns}}) \\ \text{otherwise} \\ \quad j \leftarrow 1 \\ \quad \text{while } F_{T_j} > P_r \\ \quad \quad j \leftarrow j + 1 \\ \quad M_{T_j} \end{cases}$$

$$\text{StressFactor}_r := \begin{cases} \text{"No Result"} & \text{if } M_{SLS_r} < 0.000000000000000001 \cdot \text{kN}\cdot\text{m} \\ \frac{M_r}{M_{SLS_r}} & \text{otherwise} \end{cases}$$

$$P = \begin{pmatrix} 5278 \\ 5278 \\ 3341 \\ 3341 \\ 3355 \\ 3355 \\ 3335 \\ 3335 \end{pmatrix} \text{ kN} \quad M = \begin{pmatrix} 2181 \\ 2156 \\ 70 \\ 323 \\ 562 \\ 263 \\ 561 \\ 256 \end{pmatrix} \text{ kN}\cdot\text{m} \quad M_{SLS} = \begin{pmatrix} 5863.3 \\ 5863.3 \\ 5105.0 \\ 5105.0 \\ 5105.0 \\ 5105.0 \\ 5105.0 \\ 5105.0 \end{pmatrix} \text{ kN}\cdot\text{m} \quad \text{StressFactor} = \begin{pmatrix} 0.372 \\ 0.368 \\ 0.014 \\ 0.063 \\ 0.110 \\ 0.051 \\ 0.110 \\ 0.050 \end{pmatrix}$$

**RESULTS SUMMARY**  
**SERVICEABILITY LIMIT STATE ANALYSIS OF CIRCULAR BEAM COLUMN**

Diameter of Column		1700	mm				
Percentage of rebar		2.27	%				
Load Case Ref	Pier	Applied Service Axial Load kN	Applied Service Bending Moment kNm	Service Limit State Bending Moment kNm	Allowable Stress Factor	Applied Stress Factor	Serviceability Limit State Design Result
1	P30	5278	2181	5863.3	100%	37%	OK
2	P30	5278	2156	5863.3	100%	37%	OK

**P6 PORTAL COLUMN 1.1 M DIAMETER**

**TOP**



## **Serviceability Check - Traffic Load Only**



**KATAHIRA & ENGINEERS  
INTERNATIONAL**

**Project:** Detailed Design Study of  
North Java Corridor Flyover Project

**Calculation:** Balaraja Flyover  
Serviceability Check - Traffic Load Only  
1100 mm Dia Circular RC Column - P6 Top Section

**Reference:** Project Specific Design Criteria

**Section Data**

MPa := 1000000·Pa

kN := 1000·N

Input Item		
Concrete Compressive Strength	fc	30 MPa
Structural Steel Yield Strength	fys	250 MPa
Rebar Yield Strength	fy	390 MPa
Diameter of reinforced concrete section	D	1100 mm
Thickness of CHS section	t	0 mm
Diameter of rebar - layer 1	dia1	32 mm
Diameter of rebar - layer 2	dia2	0 mm
Number bars - layer 1 (max 100)	n1	24
Number bars - layer 2 (max 100)	n2	0
Cover from face of section - layer 1	cov1	60 mm
Cover from face of section - layer 2	cov2	115 mm

**Load Data**

Ref	Pier	Load Case	P	M	Stress
			kN	kNm	Allowance
1	P61	Combination 1 - P + Traffic Load Only	2758.5	131.5	100%
2	P61	Combination 1 - P + Traffic Load Only	2758.5	12.8	100%
3	P62	Combination 1 - P + Traffic Load Only	2666.4	131.2	100%
4	P62	Combination 1 - P + Traffic Load Only	2666.4	12.6	100%

$$f_c := f_c \cdot \text{MPa} \quad f_{ys} := f_{ys} \cdot \text{MPa} \quad f_y := f_y \cdot \text{MPa} \quad D := D \cdot \text{mm} \quad ts := ts \cdot \text{mm}$$

$$\text{dia1} := \text{dia1} \cdot \text{mm} \quad \text{dia2} := \text{dia2} \cdot \text{mm} \quad \text{cov1} := \text{cov1} \cdot \text{mm} \quad \text{cov2} := \text{cov2} \cdot \text{mm}$$

$$P := P \cdot \text{kN} \quad M := M \cdot \text{kN} \cdot \text{m}$$

$$E_S := 200000 \cdot \text{MPa} \quad E_C := 4700 \sqrt{\frac{f_c}{\text{MPa}}} \cdot \text{MPa} \quad \text{Modular ratio} \quad \alpha := \begin{cases} \frac{E_S}{E_C} & \text{if } E_C > 0 \\ 1 & \text{otherwise} \end{cases} \quad \alpha = 7.77$$

$$E_C = 25743 \text{ MPa}$$

### Calculate Basic Allowable Stresses

Calculate rupture stress:

$$\sigma_{ct} := 0.5 \cdot \left( \frac{f_c}{\text{MPa}} \right)^{\frac{2}{3}} \cdot \text{MPa} \quad \sigma_{ct} = 4.8 \text{ MPa}$$

Calculate basic allowable stress of concrete

$$\sigma_{cc} := 1.0 \cdot f_c \quad \sigma_{cc} = 30.0 \text{ MPa}$$

Calculate basic allowable tensile stress of rebar

$$\sigma_{rs} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 170 \text{ MPa} \\ 170 \text{ MPa} & \text{otherwise} \end{cases} \quad \sigma_{rs} = 170 \text{ MPa}$$

Calculate basic allowable compressive stress of rebar

$$\sigma_{rc} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 110 \text{ MPa} \\ f_y & \text{otherwise} \end{cases} \quad \sigma_{rc} = 390 \text{ MPa}$$

Calculate basic allowable stress of structural steel

$$\sigma_{ts} := -0.6 f_{ys} \quad \sigma_{ts} = -150 \text{ MPa}$$

$$\sigma_{tc} := 1 f_{ys} \quad \sigma_{tc} = 250 \text{ MPa}$$

Limiting strain of rebar

$$\epsilon_{rs} := -\frac{\sigma_{rs}}{E_S} \quad \epsilon_{rs} = -0.000850$$

$$\epsilon_{rc} := \frac{\sigma_{rc}}{E_S} \quad \epsilon_{rc} = 0.001950$$

Limiting strain of structural steel

$$\epsilon_{ts} := \frac{\sigma_{ts}}{E_S} \quad \epsilon_{ts} = -0.000750$$

$$\epsilon_{tc} := \frac{\sigma_{tc}}{E_S} \quad \epsilon_{tc} = 0.001250$$

### Concrete Cross Section Data - generated

n := 50      Number of Points - 50 points maximum

i := 1 .. n + 1      Range from 1 to n+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	550
2	-69	-546	27	69	546
3	-137	-533	28	137	533
4	-202	-511	29	202	511
5	-265	-482	30	265	482
6	-323	-445	31	323	445
7	-377	-401	32	377	401
8	-424	-351	33	424	351
9	-464	-295	34	464	295
10	-498	-234	35	498	234
11	-523	-170	36	523	170
12	-540	-103	37	540	103
13	-549	-35	38	549	35
14	-549	35	39	549	-35
15	-540	103	40	540	-103
16	-523	170	41	523	-170
17	-498	234	42	498	-234
18	-464	295	43	464	-295
19	-424	351	44	424	-351
20	-377	401	45	377	-401
21	-323	445	46	323	-445
22	-265	482	47	265	-482
23	-202	511	48	202	-511
24	-137	533	49	137	-533
25	-69	546	50	69	-546

k := 1 .. 25      XS1 := XS1·mm    XS2 := XS2·mm    YS1 := YS1·mm    YS2 := YS2·mm

$x_k := XS1_k$        $y_k := YS1_k$        $x_{k+25} := XS2_k$        $y_{k+25} := YS2_k$        $x_{n+1} := XS1_1$        $y_{n+1} := YS1_1$

### Calculate Section Properties of Concrete Section

$$A_C := - \sum_{i=1}^n \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{2} \right] \quad A_C = 0.94783 \text{ m}^2$$

$$x_C := - \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{y_{i+1} - y_i}{8} \cdot \left[ (x_{i+1} + x_i)^2 + \frac{(x_{i+1} - x_i)^2}{3} \right] \right] \quad x_C = 0 \text{ m}$$

$$y_C := \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{x_{i+1} - x_i}{8} \cdot \left[ (y_{i+1} + y_i)^2 + \frac{(y_{i+1} - y_i)^2}{3} \right] \right] \quad y_C = 0 \text{ m}$$

$$I_x := \sum_{i=1}^n \left[ \left[ (x_{i+1} - x_i) \cdot \frac{y_{i+1} + y_i}{24} \right] \cdot \left[ (y_{i+1} + y_i)^2 + (y_{i+1} - y_i)^2 \right] \right] \quad I_x = 0.07149 \text{ m}^4$$

$$I_y := - \sum_{i=1}^n \left[ \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{24} \right] \cdot \left[ (x_{i+1} + x_i)^2 + (x_{i+1} - x_i)^2 \right] \right] \quad I_y = 0.07149 \text{ m}^4$$

$$I_{xC} := I_x - A_C \cdot x_C^2 \quad I_{xC} = 0.07149 \text{ m}^4$$

$$I_{yC} := I_y - A_C \cdot y_C^2 \quad I_{yC} = 0.07149 \text{ m}^4$$

### Steel Tube Cross Section Data - generated from input

ns := 50      Number of Points - 50 points maximum

ps := 1 .. ns + 1      Range from 1 to ns+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	-550
2	-142	-531	27	142	-531
3	-275	-476	28	275	-476
4	-389	-389	29	389	-389
5	-476	-275	30	476	-275
6	-531	-142	31	531	-142
7	-550	0	32	550	0
8	-531	142	33	531	142
9	-476	275	34	476	275
10	-389	389	35	389	389
11	-275	476	36	275	476
12	-142	531	37	142	531
13	0	550	38	0	550
14	142	531	39	-142	531
15	275	476	40	-275	476
16	389	389	41	-389	389
17	476	275	42	-476	275
18	531	142	43	-531	142
19	550	0	44	-550	0
20	531	-142	45	-531	-142
21	476	-275	46	-476	-275
22	389	-389	47	-389	-389
23	275	-476	48	-275	-476
24	142	-531	49	-142	-531
25	0	-550	50	0	-550

$$XSS1 := XSS1 \cdot \text{mm}$$

$$XSS2 := XSS2 \cdot \text{mm}$$

$$YSS1 := YSS1 \cdot \text{mm}$$

$$YSS2 := YSS2 \cdot \text{mm}$$

$$z := 1 .. 25$$

$$xs_z := XSS1_z$$

$$ys_z := YSS1_z$$

$$z := 26 .. 50$$

$$xs_z := XSS2_{z-25}$$

$$ys_z := YSS2_{z-25}$$

$$xs_{ns+1} := XSS1_1$$

$$ys_{ns+1} := YSS1_1$$

### Calculate Section Properties of Steel Tube Section

$$A_{ST} := - \sum_{ps=1}^{ns} \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{2} \right] \quad A_{ST} = 0 \text{ m}^2$$

$$x_{ST} := - \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{y_{ps+1}^{s} - y_{ps}^{s}}{8} \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + \frac{(x_{ps+1}^{s} - x_{ps}^{s})^2}{3} \right] \right] \quad x_{ST} = 0.2 \text{ m}$$

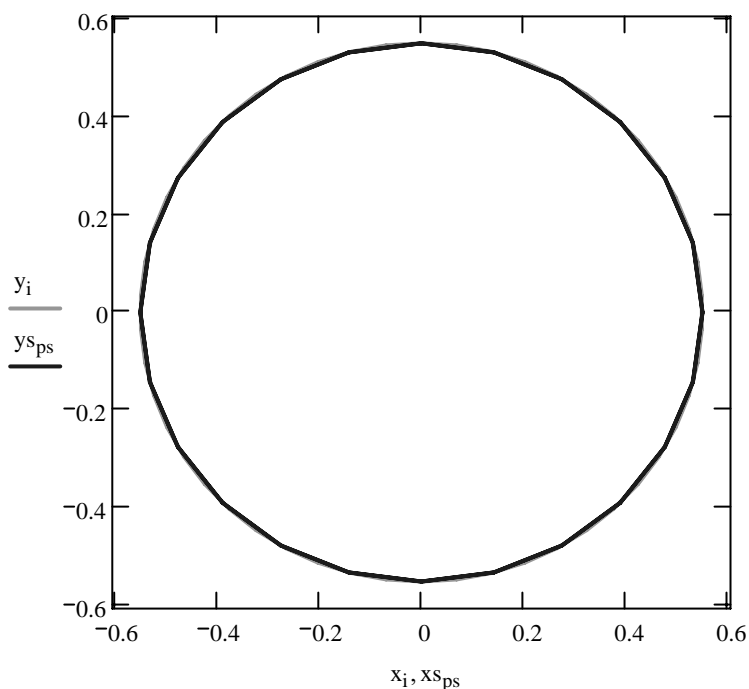
$$y_{ST} := \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{x_{ps+1}^{s} - x_{ps}^{s}}{8} \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + \frac{(y_{ps+1}^{s} - y_{ps}^{s})^2}{3} \right] \right] \quad y_{ST} = -0.011 \text{ m}$$

$$I_{xS} := \sum_{ps=1}^{ns} \left[ \left[ (x_{ps+1}^{s} - x_{ps}^{s}) \cdot \frac{y_{ps+1}^{s} + y_{ps}^{s}}{24} \right] \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + (y_{ps+1}^{s} - y_{ps}^{s})^2 \right] \right] \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := - \sum_{ps=1}^{ns} \left[ \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{24} \right] \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + (x_{ps+1}^{s} - x_{ps}^{s})^2 \right] \right] \quad I_{yS} = 0 \text{ m}^4$$

$$I_{xS} := I_{xS} - A_{ST} \cdot x_{ST}^2 \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := I_{yS} - A_{ST} \cdot y_{ST}^2 \quad I_{yS} = 0.00000 \text{ m}^4$$



**Rebar Data Layer 1 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	804	0	-474	51	0	0	0
2	804	-123	-458	52	0	0	0
3	804	-237	-410	53	0	0	0
4	804	-335	-335	54	0	0	0
5	804	-410	-237	55	0	0	0
6	804	-458	-123	56	0	0	0
7	804	-474	0	57	0	0	0
8	804	-458	123	58	0	0	0
9	804	-410	237	59	0	0	0
10	804	-335	335	60	0	0	0
11	804	-237	410	61	0	0	0
12	804	-123	458	62	0	0	0
13	804	0	474	63	0	0	0
14	804	123	458	64	0	0	0
15	804	237	410	65	0	0	0
16	804	335	335	66	0	0	0
17	804	410	237	67	0	0	0
18	804	458	123	68	0	0	0
19	804	474	0	69	0	0	0
20	804	458	-123	70	0	0	0
21	804	410	-237	71	0	0	0
22	804	335	-335	72	0	0	0
23	804	237	-410	73	0	0	0
24	804	123	-458	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0



**Rebar Data Layer 2 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	0	0	0	51	0	0	0
2	0	0	0	52	0	0	0
3	0	0	0	53	0	0	0
4	0	0	0	54	0	0	0
5	0	0	0	55	0	0	0
6	0	0	0	56	0	0	0
7	0	0	0	57	0	0	0
8	0	0	0	58	0	0	0
9	0	0	0	59	0	0	0
10	0	0	0	60	0	0	0
11	0	0	0	61	0	0	0
12	0	0	0	62	0	0	0
13	0	0	0	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

$$A1 := A1 \cdot \text{mm}^2 \quad A2 := A2 \cdot \text{mm}^2 \quad A3 := A3 \cdot \text{mm}^2 \quad A4 := A4 \cdot \text{mm}^2$$

$$X1 := X1 \cdot \text{mm} \quad X2 := X2 \cdot \text{mm} \quad X3 := X3 \cdot \text{mm} \quad X4 := X4 \cdot \text{mm}$$

$$Y1 := Y1 \cdot \text{mm} \quad Y2 := Y2 \cdot \text{mm} \quad Y3 := Y3 \cdot \text{mm} \quad Y4 := Y4 \cdot \text{mm}$$

$$k := 1..50$$

$$A_{\text{bar}_k} := A1_k \quad x_{\text{bar}_k} := X1_k \quad y_{\text{bar}_k} := Y1_k$$

$$A_{\text{bar}_{k+50}} := A2_k \quad x_{\text{bar}_{k+50}} := X2_k \quad y_{\text{bar}_{k+50}} := Y2_k$$

$$A_{\text{bar}_{k+100}} := A3_k \quad x_{\text{bar}_{k+100}} := X3_k \quad y_{\text{bar}_{k+100}} := Y3_k$$

$$A_{\text{bar}_{k+150}} := A4_k \quad x_{\text{bar}_{k+150}} := X4_k \quad y_{\text{bar}_{k+150}} := Y4_k$$

### Calculate Section Properties of Reinforcement

$$A_{\text{BAR}} := \sum_{j=1}^{200} A_{\text{bar}_j} \quad A_{\text{BAR}} = 19302 \text{ mm}^2$$

$$\rho := \frac{A_{\text{BAR}}}{A_C} \quad \rho = 0.0204$$

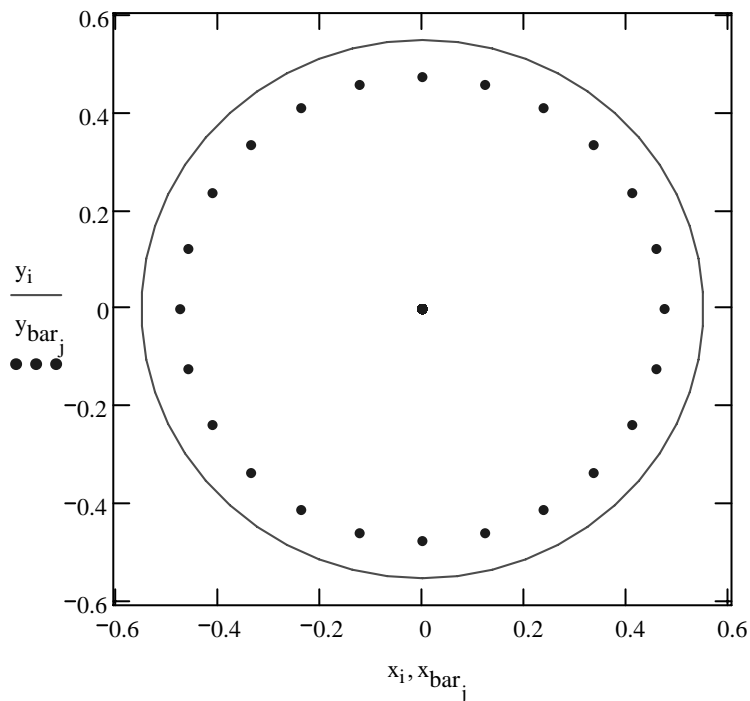
$$x_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot x_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad x_b = 0 \text{ m}$$

$$y_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot y_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad y_b = 0 \text{ m}$$

$$I_{x_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (x_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot x_b^2 \quad I_{x_b} = 0.00217 \text{ m}^4$$

$$I_{y_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (y_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot y_b^2 \quad I_{y_b} = 0.00217 \text{ m}^4$$

$j := 1 \dots 200$



**Calculate Composite Section Properties (before cracking)**

Effective area  $A_E := A_C \cdot [1 + \rho \cdot (\alpha - 1)] + A_{ST} \cdot \alpha$   $A_E = 1078490 \text{ mm}^2$

Effective centroid  $x_E := \frac{A_C \cdot [(1 - \rho) \cdot x_C + \rho \cdot x_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot x_{ST}}{A_E}$   $x_E = 0.000 \text{ m}$

$y_E := \frac{A_C \cdot [(1 - \rho) \cdot y_C + \rho \cdot y_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot y_{ST}}{A_E}$   $y_E = 0.000 \text{ m}$

Effective stiffness  $I_{EX} := I_{xC} + I_{xb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot x_C^2 + \rho \cdot x_b^2 \cdot \alpha] + (I_{xS} + A_{ST} \cdot x_{ST}^2) \cdot \alpha$   
 $I_{EX} = 0 \text{ m}^4$

$I_{EY} := I_{yC} + I_{yb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot y_C^2 + \rho \cdot y_b^2 \cdot \alpha] + (I_{yS} + A_{ST} \cdot y_{ST}^2) \cdot \alpha$   
 $I_{EY} = 0 \text{ m}^4$

Distance from extreme concrete fiber to centroid

$x_{F_{pos}} := \max(x - x_E)$   $x_{F_{neg}} := \min(x - x_E)$

$y_{F_{pos}} := \max(y - y_E)$   $y_{F_{neg}} := \min(y - y_E)$

Total depth of concrete section

$H_{CX} := x_{F_{pos}} - x_{F_{neg}}$   $H_{CX} = 1 \text{ m}$

$H_{CY} := y_{F_{pos}} - y_{F_{neg}}$   $H_{CY} = 1 \text{ m}$

Section modulus

$$Z_{Xpos} := \frac{I_{EX}}{xF_{pos}} \quad Z_{Xneg} := \frac{I_{EX}}{xF_{neg}}$$

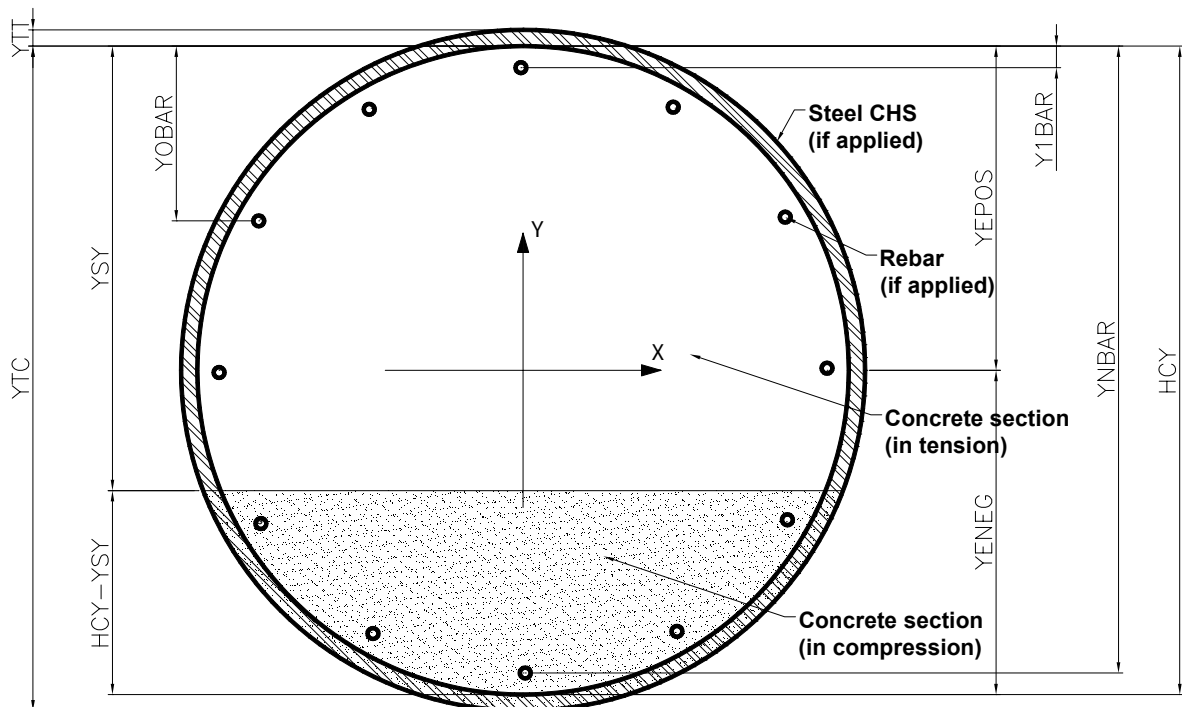
$$Z_{Ypos} := \frac{I_{EY}}{yF_{pos}} \quad Z_{Yneg} := \frac{I_{EY}}{yF_{neg}}$$

Thickness of steel tube:

$$ts := y_1 - ys_1 \quad ts = 0 \text{ mm}$$

**Establish Section Dimensions**

Positive case - determine coord of extreme concrete fiber	$y_{Epos} := \max(y)$	$y_{Epos} = 550 \text{ mm}$
Negative case - determine coord of extreme concrete fiber	$y_{Eneg} := \min(y)$	$y_{Eneg} = -550 \text{ mm}$
Offsets of rebar from extreme fiber	$y_{Obar} := y_{Epos} - y_{bar}$	
Determine most extreme rebar (minimum offset)	$y_{1bar} := \min(y_{Epos} - y_{bar})$	$y_{1bar} = 76 \text{ mm}$
Determine most extreme rebar (maximum offset)	$y_{nbar} := \max(y_{Epos} - y_{bar})$	$y_{nbar} = 1024 \text{ mm}$
Offsets of extreme steel tube fiber from extreme concrete fiber	$y_{tt} := ts$	$y_{tt} = 0 \text{ mm}$
	$y_{tc} := H_{CY} + ts$	$y_{tc} = 1100 \text{ mm}$



**ASSIGN NEUTRAL AXIS VALUES**

Number of sections to analysed                      ns := 500

q := 2 .. ns

Distance of neutral axis from extreme fiber in tension                       $y_{SY_q} := H_{CY} \cdot \frac{q}{ns + 1}$

**Calculate stresses and strains in reinforcement and concrete at extreme fibers**

Calculate strain at extreme compression fiber assuming max allowable stress in concrete:

Trial value of concrete strain

$$\epsilon_{cc} := \frac{\sigma_{cc}}{E_C} \cdot 2 \qquad \frac{\sigma_{cc}}{E_C} = 0.001165$$

Given

$$\sigma_{cc} = \epsilon_{cc} \cdot \left( 4700 \sqrt{\frac{f_c \cdot 2}{MPa}} - \frac{4700^2}{2.68} \cdot \epsilon_{cc} \right) \cdot MPa$$

$$\epsilon_{cc} := \text{Find}(\epsilon_{cc}) \qquad \epsilon_{cc} = 0.003321$$

$$\epsilon_{cc} := \begin{cases} \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \epsilon_{cc} & \text{otherwise} \end{cases} \qquad \epsilon_{cc} = 0.003321$$

Strain at other stresses taken to be linear:

$$\epsilon_{cc}(f_c, \sigma_{cd}) := \begin{cases} \frac{\sigma_{cd}}{\sigma_{tc}} \cdot \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \frac{\sigma_{cd}}{\sigma_{rc}} \cdot \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \frac{\sigma_{cd}}{\sigma_{cc}} \cdot \epsilon_{cc} & \text{otherwise} \end{cases}$$

Calculate strain in steel tube assuming max allowable stress in concrete:

In compression                       $\epsilon_{tcc_q} := \epsilon_{cc} \cdot \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}}$

In tension                       $\epsilon_{tct_q} := \epsilon_{cc} \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}}$

Calculate strain in rebar assuming max allowable stress in concrete:

$$\begin{array}{l} \text{In} \\ \text{compression} \end{array} \quad \varepsilon_{rcc_q} := \varepsilon_{cc} \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

$$\begin{array}{l} \text{In} \\ \text{tension} \end{array} \quad \varepsilon_{rct_q} := \varepsilon_{cc} \cdot \frac{y_{1bar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

Calculate design max stress in compression taking account of other limits:

$$\sigma_{cd}(\varepsilon_{tcc}, q) := \left\{ \begin{array}{l} \sigma_{cd} \leftarrow \sigma_{cc} \quad \text{if } f_c > 0 \\ \sigma_{cd} \leftarrow \sigma_{tc} \quad \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \sigma_{cd} \leftarrow \sigma_{rc} \quad \text{if } (f_c = 0) \cdot (ts = 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{tc}}{\varepsilon_{tcc}} \quad \text{if } (\varepsilon_{tcc} > \varepsilon_{tc}) \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rc}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}} \quad \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}} > \varepsilon_{rc} \right] \cdot (A_{BAR} > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{ts}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}}} \quad \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} < \varepsilon_{ts} \right] \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rs}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}}} \quad \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}} < \varepsilon_{rs} \right] \cdot (A_{BAR} > 0) \\ \sigma_{cc} \quad \text{otherwise} \end{array} \right.$$

$$\sigma_{cd_q} := \sigma_{cd}(\varepsilon_{tcc_q}, q)$$

**CALCULATE FORCES AND MOMENTS AT EACH NEUTRAL AXIS LOCATION**

Calculate force in concrete:

$$F_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from concrete about column centroid:

$$M_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] \cdot y dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in rebar assuming design max stress in concrete:

$$y_{SY_q} := \begin{cases} y_{nbar} \cdot \frac{q}{ns + 1} & \text{if } (f_c = 0) \cdot (A_{BAR} > 0) \\ y_{SY_q} & \text{otherwise} \end{cases}$$

$$\varepsilon_{S_{j,q}} := \begin{cases} \frac{y_{SY_q} - y_{Obar_j}}{y_{nbar} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{if } f_c = 0 \\ \frac{y_{SY_q} - y_{Obar_j}}{H_{CY} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{otherwise} \end{cases}$$

Calculate force in each rebar:

$$F_{S_{j,q}} := \begin{cases} \varepsilon_{S_{j,q}} \cdot E_S \cdot A_{bar_j} & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total force in reinforcement:

$$F_{R_q} := \sum_j F_{S_{j,q}}$$

Calculate moment from reinforcement about section centroid:

$$M_{R_q} := \begin{cases} \sum_j -(\varepsilon_{S_{j,q}} E_S \cdot A_{\text{bar}_j} \cdot y_{\text{bar}_j}) & \text{if } A_{\text{BAR}} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in steel tube at extreme tension fiber:

$$\varepsilon_{\text{tds}_q} := \frac{-(y_{\text{SY}_q} + y_{\text{tt}})}{H_{\text{CY}} - y_{\text{SY}_q}} \varepsilon_{\text{cc}}(f_c, \sigma_{\text{cd}_q})$$

Calculate strain in steel tube at extreme compression fiber:

$$\varepsilon_{\text{tdc}_q} := \frac{y_{\text{tc}} - y_{\text{SY}_q}}{H_{\text{CY}} - y_{\text{SY}_q}} \varepsilon_{\text{cc}}(f_c, \sigma_{\text{cd}_q})$$

Calculate tensile force in steel tube:

$$F_{\text{TS1}_q} := \int_{\left(\frac{H_{\text{CY}}}{2} - y_{\text{SY}_q}\right)}^{\frac{H_{\text{CY}}}{2} + y_{\text{tt}}} 2 \sqrt{\left(\frac{H_{\text{CY}}}{2} + y_{\text{tt}}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{\text{tds}_q} \cdot E_S \cdot \left[ y - \left(\frac{H_{\text{CY}}}{2} - y_{\text{SY}_q}\right) \right]}{y_{\text{SY}_q} + y_{\text{tt}}} \right] dy$$

$$F_{\text{TS2}_q} := \int_{\left(\frac{H_{\text{CY}}}{2} - y_{\text{SY}_q}\right)}^{\frac{H_{\text{CY}}}{2}} 2 \sqrt{\left(\frac{H_{\text{CY}}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{\text{tds}_q} \cdot E_S \cdot \left[ y - \left(\frac{H_{\text{CY}}}{2} - y_{\text{SY}_q}\right) \right]}{y_{\text{SY}_q} + y_{\text{tt}}} \right] dy$$

$$F_{\text{TS}} := \begin{cases} F_{\text{TS1}} - F_{\text{TS2}} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate compressive force in steel tube:

$$F_{\text{TC1}_q} := \int_{-\left(\frac{H_{\text{CY}}}{2} - y_{\text{SY}_q}\right)}^{\frac{H_{\text{CY}}}{2} + y_{\text{tt}}} 2 \sqrt{\left(\frac{H_{\text{CY}}}{2} + y_{\text{tt}}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{\text{tdc}_q} \cdot E_S \cdot \left[ y + \left(\frac{H_{\text{CY}}}{2} - y_{\text{SY}_q}\right) \right]}{H_{\text{CY}} - y_{\text{SY}_q} + y_{\text{tt}}} \right] dy$$



$$F_{TC2_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TC} := \begin{cases} F_{TC1} - F_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from tensile force in steel tube:

$$M_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} -2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} -2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS} := \begin{cases} M_{TS1} - M_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from compressive force in steel tube:

$$M_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC2_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC} := \begin{cases} M_{TC1} - M_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total axial response from section:

$$F_T := F_C + F_R + F_{TS} + F_{TC}$$

$$F_{TC} := F_C$$

Calculate total moment response from section:

$$M_T := M_C + M_R + M_{TS} + M_{TC}$$

$$M_{TC} := M_C$$

**CALCULATE MAXIMUM ALLOWABLE AXIAL FORCE IN SECTION**

Limiting strain in axial  
compression:

$$\varepsilon_{cL} := \begin{cases} \min(\varepsilon_{cc}, \varepsilon_{tc}) & \text{if } (A_{BAR} = 0) \cdot (ts \neq 0) \cdot (f_c \neq 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}) & \text{if } (ts = 0) \cdot (A_{BAR} \neq 0) \cdot (f_c \neq 0) \\ \varepsilon_{tc} & \text{if } (A_{BAR} = 0) \cdot (f_c = 0) \\ \varepsilon_{rc} & \text{if } (ts = 0) \cdot (f_c = 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}, \varepsilon_{tc}) & \text{otherwise} \end{cases} \quad \varepsilon_{cL} = 0.001950$$

Limiting concrete stress in axial compression

$$\sigma_{cL} := \begin{cases} \sigma_{cd2} & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases} \quad \sigma_{cL} = 18.93 \text{ MPa}$$

$$P_{MAX} := \sigma_{cL} \cdot A_C (1 - \rho) + \varepsilon_{cL} \cdot E_S (A_{BAR} + A_{ST})$$

$$P_{MAX} = 25104 \text{ kN} \quad F_{T_1} := P_{MAX} \quad M_{T_1} := 0 \cdot \text{kN} \cdot \text{m}$$

$$P_{MAXC} := \sigma_{cL} \cdot A_C \cdot (1 - \rho)$$

$$P_{MAXC} = 17576.2 \text{ kN} \quad F_{TC_1} := P_{MAXC} \quad M_{TC_1} := 0 \cdot \text{kN} \cdot \text{m}$$

**CALCULATE MINIMUM ALLOWABLE AXIAL FORCE IN SECTION**

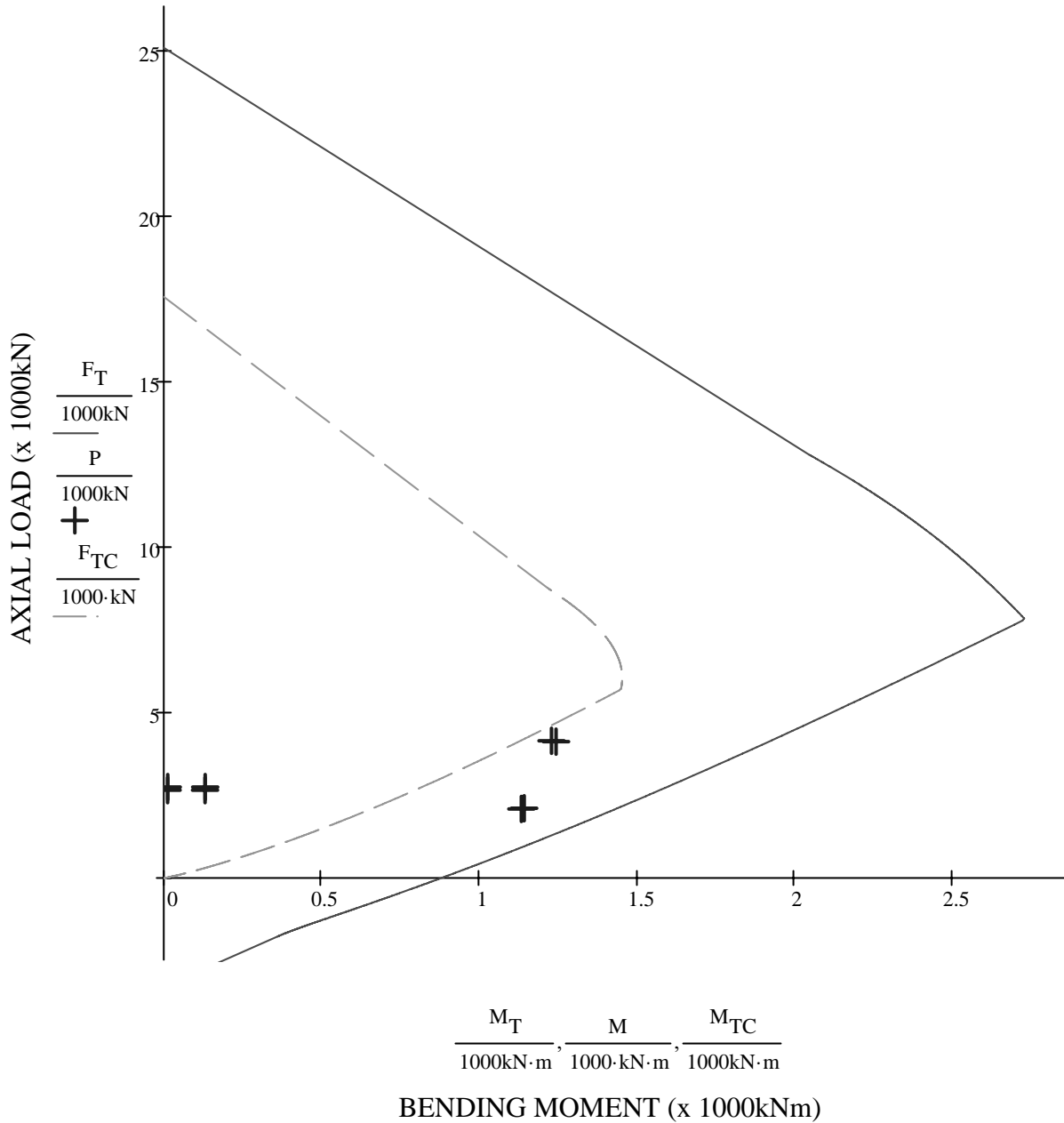
$$P_{MIN} := \begin{cases} \varepsilon_{rs} \cdot E_S (A_{BAR}) & \text{if } ts = 0 \\ \varepsilon_{ts} \cdot E_S (A_{ST}) & \text{if } A_{BAR} = 0 \\ \max(\varepsilon_{ts}, \varepsilon_{rs}) \cdot E_S (A_{BAR} + A_{ST}) & \text{otherwise} \end{cases}$$

$$P_{MIN} = -3281.3 \text{ kN} \quad F_{T_{ns+1}} := P_{MIN} \quad M_{T_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

$$\text{Limit} := \begin{cases} \min(P, F_T) \cdot 0.75 & \text{if } \min(P) > 0 \\ \min(P, F_T) \cdot 1.25 & \text{otherwise} \end{cases}$$

$$P_{MINC} := 0 \text{ kN} \quad M_{TC_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

Diameter of Column	D = 1100 mm	Characteristic strength of concrete	$f_c = 30 \text{ MPa}$
Percentage reinforcement	$\rho = 2.04 \%$	Yield Strength of Rebar	$f_y = 390 \text{ MPa}$
Thickness of CHS	$t_s = 0 \text{ mm}$	Yield Strength of CHS	$f_{ys} = 250 \text{ MPa}$



INTERACTION CURVE AT SERVICEABILITY LIMIT STATE

Equation of interaction line - upper region (between 1 and 2 calculation points)

$$m1 := \frac{M_{T_2} - M_{T_1}}{F_{T_2} - F_{T_1}} \quad c1 := F_{T_1}$$

Equation of interaction line - lower region (between ns and ns+1 calculation points)

$$m2 := \frac{M_{T_{ns}} - M_{T_{ns+1}}}{F_{T_{ns}} - F_{T_{ns+1}}} \quad c2 := F_{T_{ns+1}}$$

r := 1 .. 8

$$M_{SLS_r} := \begin{cases} 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r > F_{T_1} \\ 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r < F_{T_{ns+1}} \\ (P_r - c1) \cdot m1 & \text{if } (P_r > F_{T_2}) \cdot (P_r \leq F_{T_1}) \\ (P_r - c2) \cdot m2 & \text{if } (P_r \geq F_{T_{ns+1}}) \cdot (P_r < F_{T_{ns}}) \\ \text{otherwise} \\ \quad j \leftarrow 1 \\ \quad \text{while } F_{T_j} > P_r \\ \quad \quad j \leftarrow j + 1 \\ \quad M_{T_j} \end{cases}$$

$$\text{StressFactor}_r := \begin{cases} \text{"No Result"} & \text{if } M_{SLS_r} < 0.000000000000000001 \cdot \text{kN}\cdot\text{m} \\ \frac{M_r}{M_{SLS_r}} & \text{otherwise} \end{cases}$$

$$P = \begin{pmatrix} 2758 \\ 2758 \\ 2666 \\ 2666 \\ 2096 \\ 4131 \\ 2119 \\ 4157 \end{pmatrix} \text{ kN} \quad M = \begin{pmatrix} 132 \\ 13 \\ 131 \\ 13 \\ 1133 \\ 1243 \\ 1143 \\ 1229 \end{pmatrix} \text{ kN}\cdot\text{m} \quad M_{SLS} = \begin{pmatrix} 1589.0 \\ 1589.0 \\ 1564.4 \\ 1564.4 \\ 1426.5 \\ 1911.2 \\ 1437.4 \\ 1911.2 \end{pmatrix} \text{ kN}\cdot\text{m} \quad \text{StressFactor} = \begin{pmatrix} 0.083 \\ 0.008 \\ 0.084 \\ 0.008 \\ 0.794 \\ 0.651 \\ 0.795 \\ 0.643 \end{pmatrix}$$

**RESULTS SUMMARY**  
**SERVICEABILITY LIMIT STATE ANALYSIS OF CIRCULAR BEAM COLUMN**

Diameter of Column		1100	mm				
Percentage of rebar		2.04	%				
Load Case Ref	Pier	Applied Service Axial Load kN	Applied Service Bending Moment kNm	Service Limit State Bending Moment kNm	Allowable Stress Factor	Applied Stress Factor	Serviceability Limit State Design Result
1	P61	2758	132	1589.0	100%	8%	OK
2	P61	2758	13	1589.0	100%	1%	OK
3	P62	2666	131	1564.4	100%	8%	OK
4	P62	2666	13	1564.4	100%	1%	OK

## **Serviceability Check - Full Live Load**



**KATAHIRA & ENGINEERS  
INTERNATIONAL**

**Project:** Detailed Design Study of  
North Java Corridor Flyover Project

**Calculation:** Balaraja Flyover  
Serviceability Check - Full Live Load  
1100 mm Dia Circular RC Column - P6 Top Section

**Reference:** Project Specific Design Criteria

**Section Data**

MPa := 1000000·Pa

kN := 1000·N

Input Item		
Concrete Compressive Strength	fc	30 MPa
Structural Steel Yield Strength	fys	250 MPa
Rebar Yield Strength	fy	390 MPa
Diameter of reinforced concrete section	D	1100 mm
Thickness of CHS section	t	0 mm
Diameter of rebar - layer 1	dia1	32 mm
Diameter of rebar - layer 2	dia2	0 mm
Number bars - layer 1 (max 100)	n1	24
Number bars - layer 2 (max 100)	n2	0
Cover from face of section - layer 1	cov1	60 mm
Cover from face of section - layer 2	cov2	115 mm

**Load Data**

Ref	Pier	Load Case	P	M	Stress
			kN	kNm	Allowance
1	P61	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+CRSH	2747.9	177.8	140%
2	P61	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+CRSH	2747.9	58.0	140%
3	P62	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+CRSH	2669.5	177.5	140%
4	P62	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+CRSH	2669.5	58.2	140%



$$f_c := f_c \cdot \text{MPa} \quad f_{ys} := f_{ys} \cdot \text{MPa} \quad f_y := f_y \cdot \text{MPa} \quad D := D \cdot \text{mm} \quad ts := ts \cdot \text{mm}$$

$$\text{dia1} := \text{dia1} \cdot \text{mm} \quad \text{dia2} := \text{dia2} \cdot \text{mm} \quad \text{cov1} := \text{cov1} \cdot \text{mm} \quad \text{cov2} := \text{cov2} \cdot \text{mm}$$

$$P := P \cdot \text{kN} \quad M := M \cdot \text{kN} \cdot \text{m}$$

$$E_S := 200000 \cdot \text{MPa} \quad E_C := 4700 \sqrt{\frac{f_c}{\text{MPa}}} \cdot \text{MPa} \quad \text{Modular ratio} \quad \alpha := \begin{cases} \frac{E_S}{E_C} & \text{if } E_C > 0 \\ 1 & \text{otherwise} \end{cases} \quad \alpha = 7.77$$

$$E_C = 25743 \text{ MPa}$$

### Calculate Basic Allowable Stresses

Calculate rupture stress:

$$\sigma_{ct} := 0.5 \cdot \left( \frac{f_c}{\text{MPa}} \right)^{\frac{2}{3}} \cdot \text{MPa} \quad \sigma_{ct} = 4.8 \text{ MPa}$$

Calculate basic allowable stress of concrete

$$\sigma_{cc} := 1.0 \cdot f_c \quad \sigma_{cc} = 30.0 \text{ MPa}$$

Calculate basic allowable tensile stress of rebar

$$\sigma_{rs} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 170 \text{ MPa} \\ 170 \text{ MPa} & \text{otherwise} \end{cases} \quad \sigma_{rs} = 170 \text{ MPa}$$

Calculate basic allowable compressive stress of rebar

$$\sigma_{rc} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 110 \text{ MPa} \\ f_y & \text{otherwise} \end{cases} \quad \sigma_{rc} = 390 \text{ MPa}$$

Calculate basic allowable stress of structural steel

$$\sigma_{ts} := -0.6 f_{ys} \quad \sigma_{ts} = -150 \text{ MPa}$$

$$\sigma_{tc} := 1 f_{ys} \quad \sigma_{tc} = 250 \text{ MPa}$$

Limiting strain of rebar

$$\epsilon_{rs} := -\frac{\sigma_{rs}}{E_S} \quad \epsilon_{rs} = -0.000850$$

$$\epsilon_{rc} := \frac{\sigma_{rc}}{E_S} \quad \epsilon_{rc} = 0.001950$$

Limiting strain of structural steel

$$\epsilon_{ts} := \frac{\sigma_{ts}}{E_S} \quad \epsilon_{ts} = -0.000750$$

$$\epsilon_{tc} := \frac{\sigma_{tc}}{E_S} \quad \epsilon_{tc} = 0.001250$$

### Concrete Cross Section Data - generated

n := 50      Number of Points - 50 points maximum

i := 1 .. n + 1      Range from 1 to n+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	550
2	-69	-546	27	69	546
3	-137	-533	28	137	533
4	-202	-511	29	202	511
5	-265	-482	30	265	482
6	-323	-445	31	323	445
7	-377	-401	32	377	401
8	-424	-351	33	424	351
9	-464	-295	34	464	295
10	-498	-234	35	498	234
11	-523	-170	36	523	170
12	-540	-103	37	540	103
13	-549	-35	38	549	35
14	-549	35	39	549	-35
15	-540	103	40	540	-103
16	-523	170	41	523	-170
17	-498	234	42	498	-234
18	-464	295	43	464	-295
19	-424	351	44	424	-351
20	-377	401	45	377	-401
21	-323	445	46	323	-445
22	-265	482	47	265	-482
23	-202	511	48	202	-511
24	-137	533	49	137	-533
25	-69	546	50	69	-546

k := 1 .. 25      XS1 := XS1·mm    XS2 := XS2·mm      YS1 := YS1·mm    YS2 := YS2·mm

$x_k := XS1_k$        $y_k := YS1_k$        $x_{k+25} := XS2_k$        $y_{k+25} := YS2_k$        $x_{n+1} := XS1_1$        $y_{n+1} := YS1_1$

### Calculate Section Properties of Concrete Section

$$A_C := - \sum_{i=1}^n \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{2} \right] \quad A_C = 0.94783 \text{ m}^2$$

$$x_C := - \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{y_{i+1} - y_i}{8} \cdot \left[ (x_{i+1} + x_i)^2 + \frac{(x_{i+1} - x_i)^2}{3} \right] \right] \quad x_C = 0 \text{ m}$$

$$y_C := \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{x_{i+1} - x_i}{8} \cdot \left[ (y_{i+1} + y_i)^2 + \frac{(y_{i+1} - y_i)^2}{3} \right] \right] \quad y_C = 0 \text{ m}$$

$$I_x := \sum_{i=1}^n \left[ \left[ (x_{i+1} - x_i) \cdot \frac{y_{i+1} + y_i}{24} \right] \cdot \left[ (y_{i+1} + y_i)^2 + (y_{i+1} - y_i)^2 \right] \right] \quad I_x = 0.07149 \text{ m}^4$$

$$I_y := - \sum_{i=1}^n \left[ \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{24} \right] \cdot \left[ (x_{i+1} + x_i)^2 + (x_{i+1} - x_i)^2 \right] \right] \quad I_y = 0.07149 \text{ m}^4$$

$$I_{xC} := I_x - A_C \cdot x_C^2 \quad I_{xC} = 0.07149 \text{ m}^4$$

$$I_{yC} := I_y - A_C \cdot y_C^2 \quad I_{yC} = 0.07149 \text{ m}^4$$

### Steel Tube Cross Section Data - generated from input

ns := 50      Number of Points - 50 points maximum

ps := 1 .. ns + 1    Range from 1 to ns+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	-550
2	-142	-531	27	142	-531
3	-275	-476	28	275	-476
4	-389	-389	29	389	-389
5	-476	-275	30	476	-275
6	-531	-142	31	531	-142
7	-550	0	32	550	0
8	-531	142	33	531	142
9	-476	275	34	476	275
10	-389	389	35	389	389
11	-275	476	36	275	476
12	-142	531	37	142	531
13	0	550	38	0	550
14	142	531	39	-142	531
15	275	476	40	-275	476
16	389	389	41	-389	389
17	476	275	42	-476	275
18	531	142	43	-531	142
19	550	0	44	-550	0
20	531	-142	45	-531	-142
21	476	-275	46	-476	-275
22	389	-389	47	-389	-389
23	275	-476	48	-275	-476
24	142	-531	49	-142	-531
25	0	-550	50	0	-550

$$XSS1 := XSS1 \cdot \text{mm}$$

$$XSS2 := XSS2 \cdot \text{mm}$$

$$YSS1 := YSS1 \cdot \text{mm}$$

$$YSS2 := YSS2 \cdot \text{mm}$$

$$z := 1 .. 25$$

$$xs_z := XSS1_z$$

$$ys_z := YSS1_z$$

$$z := 26 .. 50$$

$$xs_z := XSS2_{z-25}$$

$$ys_z := YSS2_{z-25}$$

$$xs_{ns+1} := XSS1_1$$

$$ys_{ns+1} := YSS1_1$$

**Calculate Section Properties of Steel Tube Section**

$$A_{ST} := - \sum_{ps=1}^{ns} \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{2} \right] \quad A_{ST} = 0 \text{ m}^2$$

$$x_{ST} := - \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{y_{ps+1}^{s} - y_{ps}^{s}}{8} \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + \frac{(x_{ps+1}^{s} - x_{ps}^{s})^2}{3} \right] \right] \quad x_{ST} = 0.2 \text{ m}$$

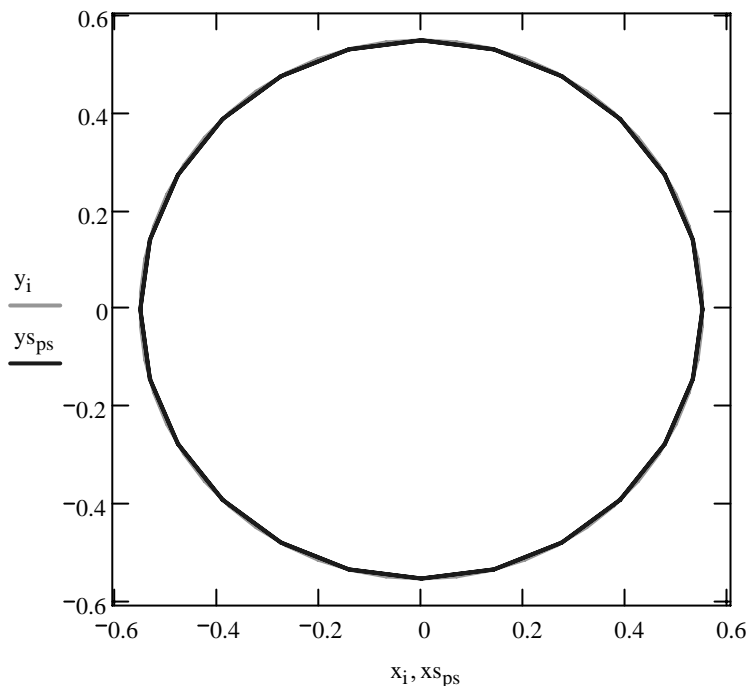
$$y_{ST} := \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{x_{ps+1}^{s} - x_{ps}^{s}}{8} \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + \frac{(y_{ps+1}^{s} - y_{ps}^{s})^2}{3} \right] \right] \quad y_{ST} = -0.011 \text{ m}$$

$$I_{xS} := \sum_{ps=1}^{ns} \left[ \left[ (x_{ps+1}^{s} - x_{ps}^{s}) \cdot \frac{y_{ps+1}^{s} + y_{ps}^{s}}{24} \right] \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + (y_{ps+1}^{s} - y_{ps}^{s})^2 \right] \right] \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := - \sum_{ps=1}^{ns} \left[ \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{24} \right] \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + (x_{ps+1}^{s} - x_{ps}^{s})^2 \right] \right] \quad I_{yS} = 0 \text{ m}^4$$

$$I_{xS} := I_{xS} - A_{ST} \cdot x_{ST}^2 \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := I_{yS} - A_{ST} \cdot y_{ST}^2 \quad I_{yS} = 0.00000 \text{ m}^4$$



**Rebar Data Layer 1 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	804	0	-474	51	0	0	0
2	804	-123	-458	52	0	0	0
3	804	-237	-410	53	0	0	0
4	804	-335	-335	54	0	0	0
5	804	-410	-237	55	0	0	0
6	804	-458	-123	56	0	0	0
7	804	-474	0	57	0	0	0
8	804	-458	123	58	0	0	0
9	804	-410	237	59	0	0	0
10	804	-335	335	60	0	0	0
11	804	-237	410	61	0	0	0
12	804	-123	458	62	0	0	0
13	804	0	474	63	0	0	0
14	804	123	458	64	0	0	0
15	804	237	410	65	0	0	0
16	804	335	335	66	0	0	0
17	804	410	237	67	0	0	0
18	804	458	123	68	0	0	0
19	804	474	0	69	0	0	0
20	804	458	-123	70	0	0	0
21	804	410	-237	71	0	0	0
22	804	335	-335	72	0	0	0
23	804	237	-410	73	0	0	0
24	804	123	-458	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

**Rebar Data Layer 2 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	0	0	0	51	0	0	0
2	0	0	0	52	0	0	0
3	0	0	0	53	0	0	0
4	0	0	0	54	0	0	0
5	0	0	0	55	0	0	0
6	0	0	0	56	0	0	0
7	0	0	0	57	0	0	0
8	0	0	0	58	0	0	0
9	0	0	0	59	0	0	0
10	0	0	0	60	0	0	0
11	0	0	0	61	0	0	0
12	0	0	0	62	0	0	0
13	0	0	0	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

$$A1 := A1 \cdot \text{mm}^2 \quad A2 := A2 \cdot \text{mm}^2 \quad A3 := A3 \cdot \text{mm}^2 \quad A4 := A4 \cdot \text{mm}^2$$

$$X1 := X1 \cdot \text{mm} \quad X2 := X2 \cdot \text{mm} \quad X3 := X3 \cdot \text{mm} \quad X4 := X4 \cdot \text{mm}$$

$$Y1 := Y1 \cdot \text{mm} \quad Y2 := Y2 \cdot \text{mm} \quad Y3 := Y3 \cdot \text{mm} \quad Y4 := Y4 \cdot \text{mm}$$

$$k := 1..50$$

$$A_{\text{bar}_k} := A1_k \quad x_{\text{bar}_k} := X1_k \quad y_{\text{bar}_k} := Y1_k$$

$$A_{\text{bar}_{k+50}} := A2_k \quad x_{\text{bar}_{k+50}} := X2_k \quad y_{\text{bar}_{k+50}} := Y2_k$$

$$A_{\text{bar}_{k+100}} := A3_k \quad x_{\text{bar}_{k+100}} := X3_k \quad y_{\text{bar}_{k+100}} := Y3_k$$

$$A_{\text{bar}_{k+150}} := A4_k \quad x_{\text{bar}_{k+150}} := X4_k \quad y_{\text{bar}_{k+150}} := Y4_k$$

### Calculate Section Properties of Reinforcement

$$A_{\text{BAR}} := \sum_{j=1}^{200} A_{\text{bar}_j} \quad A_{\text{BAR}} = 19302 \text{ mm}^2$$

$$\rho := \frac{A_{\text{BAR}}}{A_C} \quad \rho = 0.0204$$

$$x_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot x_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad x_b = 0 \text{ m}$$

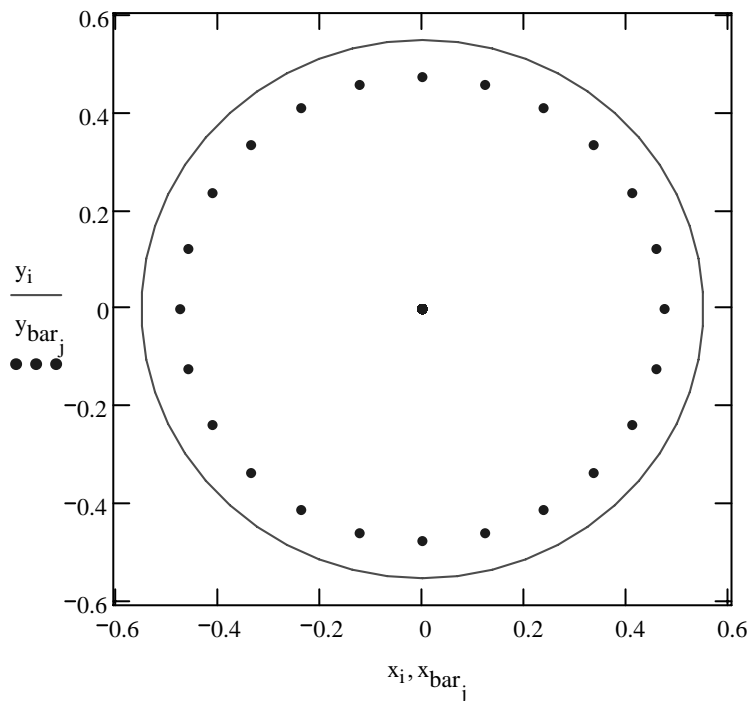
$$y_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot y_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad y_b = 0 \text{ m}$$

$$I_{x_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (x_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot x_b^2 \quad I_{x_b} = 0.00217 \text{ m}^4$$

$$I_{y_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (y_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot y_b^2 \quad I_{y_b} = 0.00217 \text{ m}^4$$



$j := 1 \dots 200$



**Calculate Composite Section Properties (before cracking)**

Effective area  $A_E := A_C \cdot [1 + \rho \cdot (\alpha - 1)] + A_{ST} \cdot \alpha$   $A_E = 1078490 \text{ mm}^2$

Effective centroid  $x_E := \frac{A_C \cdot [(1 - \rho) \cdot x_C + \rho \cdot x_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot x_{ST}}{A_E}$   $x_E = 0.000 \text{ m}$

$y_E := \frac{A_C \cdot [(1 - \rho) \cdot y_C + \rho \cdot y_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot y_{ST}}{A_E}$   $y_E = 0.000 \text{ m}$

Effective stiffness  $I_{EX} := I_{xC} + I_{xb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot x_C^2 + \rho \cdot x_b^2 \cdot \alpha] + (I_{xS} + A_{ST} \cdot x_{ST}^2) \cdot \alpha$   
 $I_{EX} = 0 \text{ m}^4$

$I_{EY} := I_{yC} + I_{yb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot y_C^2 + \rho \cdot y_b^2 \cdot \alpha] + (I_{yS} + A_{ST} \cdot y_{ST}^2) \cdot \alpha$   
 $I_{EY} = 0 \text{ m}^4$

Distance from extreme concrete fiber to centroid

$x_{F_{pos}} := \max(x - x_E)$   $x_{F_{neg}} := \min(x - x_E)$

$y_{F_{pos}} := \max(y - y_E)$   $y_{F_{neg}} := \min(y - y_E)$

Total depth of concrete section

$H_{CX} := x_{F_{pos}} - x_{F_{neg}}$   $H_{CX} = 1 \text{ m}$

$H_{CY} := y_{F_{pos}} - y_{F_{neg}}$   $H_{CY} = 1 \text{ m}$

Section modulus

$$Z_{Xpos} := \frac{I_{EX}}{xF_{pos}}$$

$$Z_{Xneg} := \frac{I_{EX}}{xF_{neg}}$$

$$Z_{Ypos} := \frac{I_{EY}}{yF_{pos}}$$

$$Z_{Yneg} := \frac{I_{EY}}{yF_{neg}}$$

Thickness of steel tube:

$$ts := y_1 - ys_1$$

$$ts = 0 \text{ mm}$$

**Establish Section Dimensions**

Positive case - determine coord of extreme concrete fiber

$$y_{Epos} := \max(y)$$

$$y_{Epos} = 550 \text{ mm}$$

Negative case - determine coord of extreme concrete fiber

$$y_{Eneg} := \min(y)$$

$$y_{Eneg} = -550 \text{ mm}$$

Offsets of rebar from extreme fiber

$$y_{Obar} := y_{Epos} - y_{bar}$$

Determine most extreme rebar (minimum offset)

$$y_{1bar} := \min(y_{Epos} - y_{bar})$$

$$y_{1bar} = 76 \text{ mm}$$

Determine most extreme rebar (maximum offset)

$$y_{nbar} := \max(y_{Epos} - y_{bar})$$

$$y_{nbar} = 1024 \text{ mm}$$

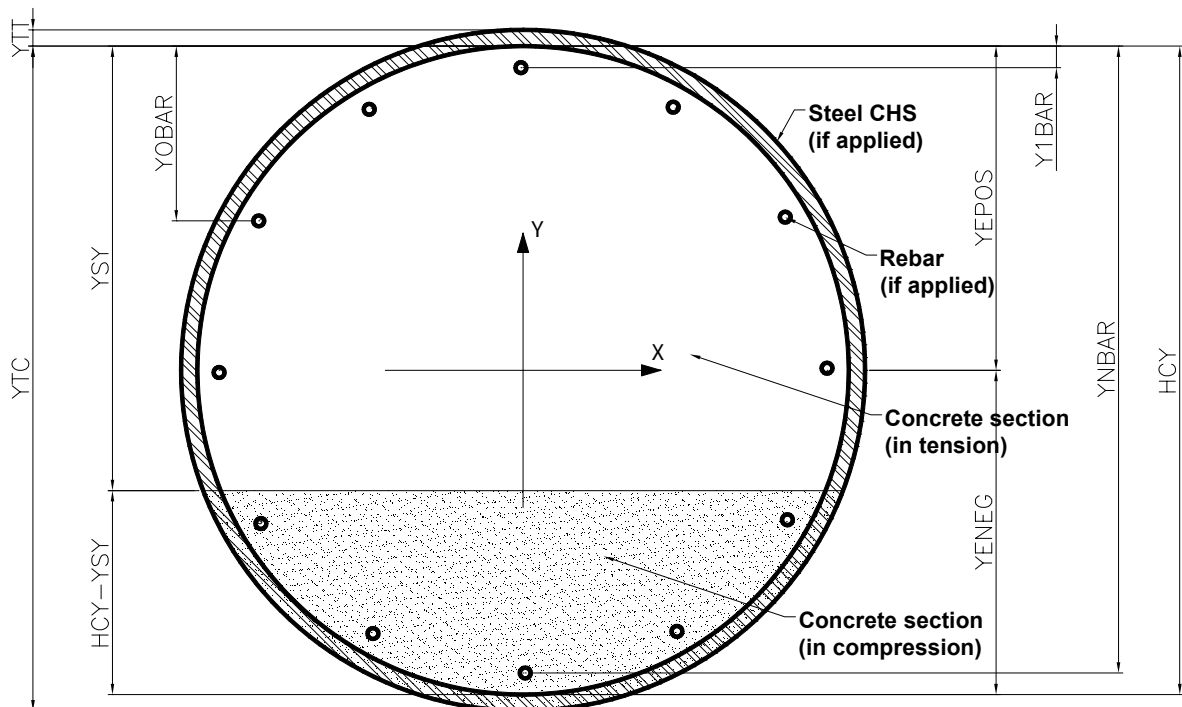
Offsets of extreme steel tube fiber from extreme concrete fiber

$$y_{tt} := ts$$

$$y_{tt} = 0 \text{ mm}$$

$$y_{tc} := H_{CY} + ts$$

$$y_{tc} = 1100 \text{ mm}$$



**ASSIGN NEUTRAL AXIS VALUES**

Number of sections to analysed                      ns := 500

q := 2 .. ns

Distance of neutral axis from extreme fiber in tension                       $y_{SY_q} := H_{CY} \cdot \frac{q}{ns + 1}$

**Calculate stresses and strains in reinforcement and concrete at extreme fibers**

Calculate strain at extreme compression fiber assuming max allowable stress in concrete:

Trial value of concrete strain

$$\epsilon_{cc} := \frac{\sigma_{cc}}{E_C} \cdot 2 \qquad \frac{\sigma_{cc}}{E_C} = 0.001165$$

Given

$$\sigma_{cc} = \epsilon_{cc} \cdot \left( 4700 \sqrt{\frac{f_c \cdot 2}{MPa}} - \frac{4700^2}{2.68} \cdot \epsilon_{cc} \right) \cdot MPa$$

$$\epsilon_{cc} := \text{Find}(\epsilon_{cc}) \qquad \epsilon_{cc} = 0.003321$$

$$\epsilon_{cc} := \begin{cases} \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \epsilon_{cc} & \text{otherwise} \end{cases} \qquad \epsilon_{cc} = 0.003321$$

Strain at other stresses taken to be linear:

$$\epsilon_{cc}(f_c, \sigma_{cd}) := \begin{cases} \frac{\sigma_{cd}}{\sigma_{tc}} \cdot \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \frac{\sigma_{cd}}{\sigma_{rc}} \cdot \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \frac{\sigma_{cd}}{\sigma_{cc}} \cdot \epsilon_{cc} & \text{otherwise} \end{cases}$$

Calculate strain in steel tube assuming max allowable stress in concrete:

In compression                       $\epsilon_{tcc_q} := \epsilon_{cc} \cdot \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}}$

In tension                               $\epsilon_{tct_q} := \epsilon_{cc} \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}}$

Calculate strain in rebar assuming max allowable stress in concrete:

$$\text{In compression} \quad \varepsilon_{rcc_q} := \varepsilon_{cc} \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

$$\text{In tension} \quad \varepsilon_{rct_q} := \varepsilon_{cc} \cdot \frac{y_{1bar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

Calculate design max stress in compression taking account of other limits:

$$\sigma_{cd}(\varepsilon_{tcc}, q) := \begin{cases} \sigma_{cd} \leftarrow \sigma_{cc} & \text{if } f_c > 0 \\ \sigma_{cd} \leftarrow \sigma_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \sigma_{cd} \leftarrow \sigma_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{tc}}{\varepsilon_{tcc}} & \text{if } (\varepsilon_{tcc} > \varepsilon_{tc}) \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rc}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}} & \text{if } \left( \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}} > \varepsilon_{rc} \right) \cdot (A_{BAR} > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{ts}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}}} & \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} < \varepsilon_{ts} \right] \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rs}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}}} & \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}} < \varepsilon_{rs} \right] \cdot (A_{BAR} > 0) \\ \sigma_{cc} & \text{otherwise} \end{cases}$$

$$\sigma_{cd_q} := \sigma_{cd}(\varepsilon_{tcc_q}, q)$$

**CALCULATE FORCES AND MOMENTS AT EACH NEUTRAL AXIS LOCATION**

Calculate force in concrete:

$$F_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from concrete about column centroid:

$$M_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] \cdot y dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in rebar assuming design max stress in concrete:

$$y_{SY_q} := \begin{cases} y_{nbar} \cdot \frac{q}{ns + 1} & \text{if } (f_c = 0) \cdot (A_{BAR} > 0) \\ y_{SY_q} & \text{otherwise} \end{cases}$$

$$\varepsilon_{S_{j,q}} := \begin{cases} \frac{y_{SY_q} - y_{Obar_j}}{y_{nbar} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{if } f_c = 0 \\ \frac{y_{SY_q} - y_{Obar_j}}{H_{CY} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{otherwise} \end{cases}$$

Calculate force in each rebar:

$$F_{S_{j,q}} := \begin{cases} \varepsilon_{S_{j,q}} \cdot E_S \cdot A_{bar_j} & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total force in reinforcement:

$$F_{R_q} := \sum_j F_{S_{j,q}}$$

Calculate moment from reinforcement about section centroid:

$$M_{R_q} := \begin{cases} \sum_j -(\varepsilon_{S_{j,q}} E_S A_{bar_j} y_{bar_j}) & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in steel tube at extreme tension fiber:

$$\varepsilon_{tds_q} := \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate strain in steel tube at extreme compression fiber:

$$\varepsilon_{tdc_q} := \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate tensile force in steel tube:

$$F_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS} := \begin{cases} F_{TS1} - F_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate compressive force in steel tube:

$$F_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TC2q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] dy$$

$$F_{TC} := \begin{cases} F_{TC1} - F_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from tensile force in steel tube:

$$M_{TS1q} := \int_{\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2} + y_{tt}} -2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS2q} := \int_{\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} -2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS} := \begin{cases} M_{TS1} - M_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from compressive force in steel tube:

$$M_{TC1q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC2q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC} := \begin{cases} M_{TC1} - M_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total axial response from section:

$$F_T := F_C + F_R + F_{TS} + F_{TC}$$

$$F_{TC} := F_C$$

Calculate total moment response from section:

$$M_T := M_C + M_R + M_{TS} + M_{TC}$$

$$M_{TC} := M_C$$



### CALCULATE MAXIMUM ALLOWABLE AXIAL FORCE IN SECTION

Limiting strain in axial  
compression:

$$\varepsilon_{cL} := \begin{cases} \min(\varepsilon_{cc}, \varepsilon_{tc}) & \text{if } (A_{BAR} = 0) \cdot (ts \neq 0) \cdot (f_c \neq 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}) & \text{if } (ts = 0) \cdot (A_{BAR} \neq 0) \cdot (f_c \neq 0) \\ \varepsilon_{tc} & \text{if } (A_{BAR} = 0) \cdot (f_c = 0) \\ \varepsilon_{rc} & \text{if } (ts = 0) \cdot (f_c = 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}, \varepsilon_{tc}) & \text{otherwise} \end{cases} \quad \varepsilon_{cL} = 0.001950$$

Limiting concrete stress in axial compression

$$\sigma_{cL} := \begin{cases} \sigma_{cd2} & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases} \quad \sigma_{cL} = 18.93 \text{ MPa}$$

$$P_{MAX} := \sigma_{cL} \cdot A_C (1 - \rho) + \varepsilon_{cL} \cdot E_S (A_{BAR} + A_{ST})$$

$$P_{MAX} = 25104 \text{ kN} \quad F_{T_1} := P_{MAX} \quad M_{T_1} := 0 \cdot \text{kN} \cdot \text{m}$$

$$P_{MAXC} := \sigma_{cL} \cdot A_C \cdot (1 - \rho)$$

$$P_{MAXC} = 17576.2 \text{ kN} \quad F_{TC_1} := P_{MAXC} \quad M_{TC_1} := 0 \cdot \text{kN} \cdot \text{m}$$

### CALCULATE MINIMUM ALLOWABLE AXIAL FORCE IN SECTION

$$P_{MIN} := \begin{cases} \varepsilon_{rs} \cdot E_S (A_{BAR}) & \text{if } ts = 0 \\ \varepsilon_{ts} \cdot E_S (A_{ST}) & \text{if } A_{BAR} = 0 \\ \max(\varepsilon_{ts}, \varepsilon_{rs}) \cdot E_S (A_{BAR} + A_{ST}) & \text{otherwise} \end{cases}$$

$$P_{MIN} = -3281.3 \text{ kN} \quad F_{T_{ns+1}} := P_{MIN} \quad M_{T_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

$$\text{Limit} := \begin{cases} \min(P, F_T) \cdot 0.75 & \text{if } \min(P) > 0 \\ \min(P, F_T) \cdot 1.25 & \text{otherwise} \end{cases}$$

$$P_{MINC} := 0 \text{ kN} \quad M_{TC_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

Diameter of Column  $D = 1100 \text{ mm}$

Percentage reinforcement  $\rho = 2.04 \%$

Thickness of CHS  $t_s = 0 \text{ mm}$

Characteristic strength of concrete

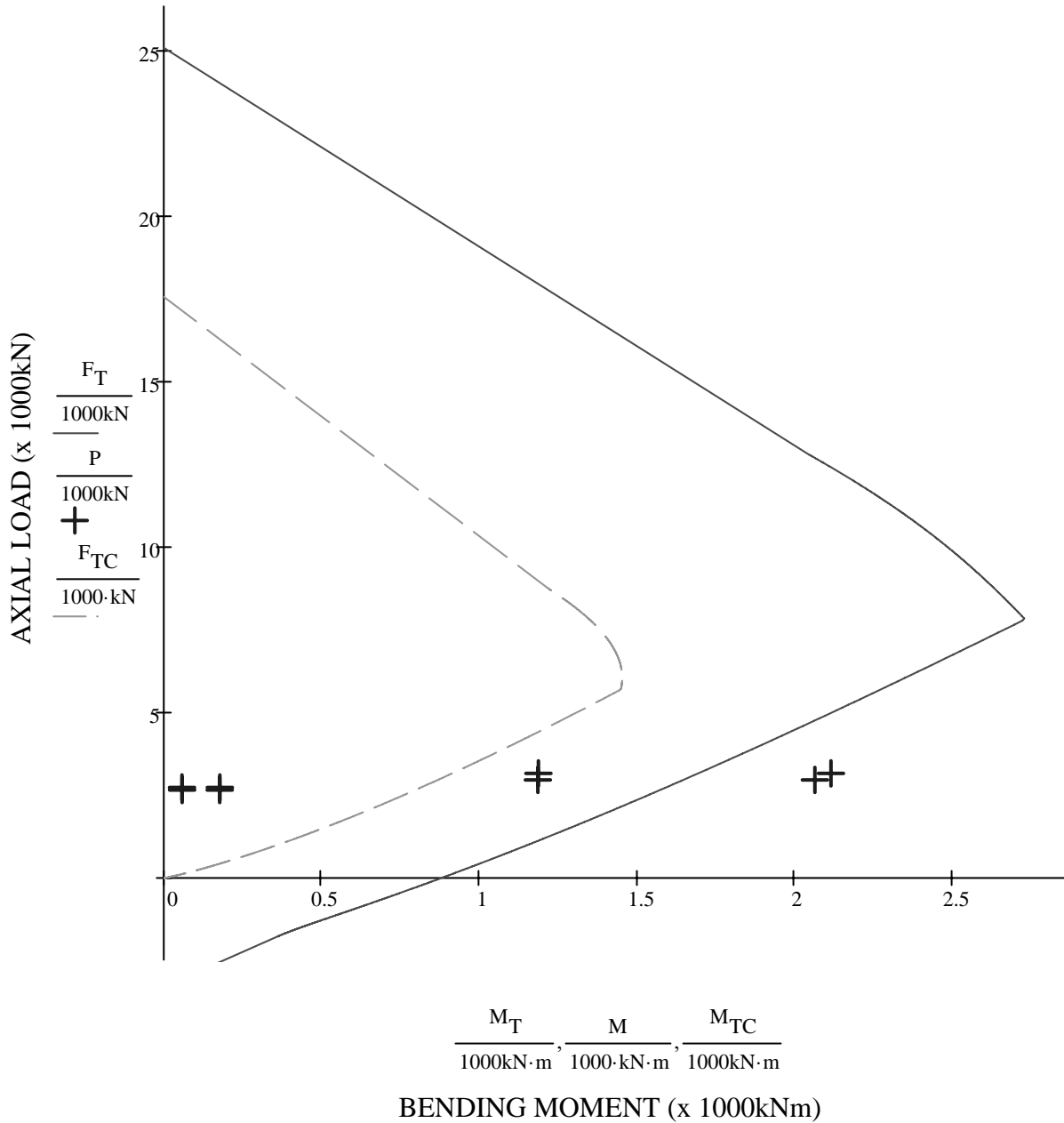
Yield Strength of Rebar

Yield Strength of CHS

$f_c = 30 \text{ MPa}$

$f_y = 390 \text{ MPa}$

$f_{ys} = 250 \text{ MPa}$



Equation of interaction line - upper region (between 1 and 2 calculation points)

$$m1 := \frac{M_{T_2} - M_{T_1}}{F_{T_2} - F_{T_1}} \quad c1 := F_{T_1}$$

Equation of interaction line - lower region (between ns and ns+1 calculation points)

$$m2 := \frac{M_{T_{ns}} - M_{T_{ns+1}}}{F_{T_{ns}} - F_{T_{ns+1}}} \quad c2 := F_{T_{ns+1}}$$

r := 1 .. 8

$$M_{SLS_r} := \begin{cases} 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r > F_{T_1} \\ 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r < F_{T_{ns+1}} \\ (P_r - c1) \cdot m1 & \text{if } (P_r > F_{T_2}) \cdot (P_r \leq F_{T_1}) \\ (P_r - c2) \cdot m2 & \text{if } (P_r \geq F_{T_{ns+1}}) \cdot (P_r < F_{T_{ns}}) \\ \text{otherwise} \\ \quad j \leftarrow 1 \\ \quad \text{while } F_{T_j} > P_r \\ \quad \quad j \leftarrow j + 1 \\ \quad M_{T_j} \end{cases}$$

$$\text{StressFactor}_r := \begin{cases} \text{"No Result"} & \text{if } M_{SLS_r} < 0.000000000000000001 \cdot \text{kN}\cdot\text{m} \\ \frac{M_r}{M_{SLS_r}} & \text{otherwise} \end{cases}$$

$$P = \begin{pmatrix} 2748 \\ 2748 \\ 2669 \\ 2669 \\ 2974 \\ 2974 \\ 3172 \\ 3172 \end{pmatrix} \text{ kN} \quad M = \begin{pmatrix} 178 \\ 58 \\ 178 \\ 58 \\ 2063 \\ 1186 \\ 2115 \\ 1187 \end{pmatrix} \text{ kN}\cdot\text{m} \quad M_{SLS} = \begin{pmatrix} 1589.0 \\ 1589.0 \\ 1564.4 \\ 1564.4 \\ 1639.7 \\ 1639.7 \\ 1692.4 \\ 1692.4 \end{pmatrix} \text{ kN}\cdot\text{m} \quad \text{StressFactor} = \begin{pmatrix} 0.112 \\ 0.037 \\ 0.113 \\ 0.037 \\ 1.258 \\ 0.723 \\ 1.250 \\ 0.702 \end{pmatrix}$$

**RESULTS SUMMARY**  
**SERVICEABILITY LIMIT STATE ANALYSIS OF CIRCULAR BEAM COLUMN**

Diameter of Column		1100	mm				
Percentage of rebar		2.04	%				
Load Case Ref	Pier	Applied Service Axial Load kN	Applied Service Bending Moment kNm	Service Limit State Bending Moment kNm	Allowable Stress Factor	Applied Stress Factor	Serviceability Limit State Design Result
1	P61	2748	178	1589.0	140%	11%	OK
2	P61	2748	58	1589.0	140%	4%	OK
3	P62	2669	178	1564.4	140%	11%	OK
4	P62	2669	58	1564.4	140%	4%	OK

**BASE**

## **Serviceability Check - Traffic Load Only**



**KATAHIRA & ENGINEERS  
INTERNATIONAL**

**Project:** Detailed Design Study of  
North Java Corridor Flyover Project

**Calculation:** Balaraja Flyover  
Serviceability Check - Traffic Load Only  
1100 mm Dia Circular RC Column - P6 Base Section

**Reference:** Project Specific Design Criteria

**Section Data**

MPa := 1000000·Pa

kN := 1000·N

Input Item		
Concrete Compressive Strength	fc	30 MPa
Structural Steel Yield Strength	fys	250 MPa
Rebar Yield Strength	fy	390 MPa
Diameter of reinforced concrete section	D	1100 mm
Thickness of CHS section	t	0 mm
Diameter of rebar - layer 1	dia1	32 mm
Diameter of rebar - layer 2	dia2	0 mm
Number bars - layer 1 (max 100)	n1	12
Number bars - layer 2 (max 100)	n2	0
Cover from face of section - layer 1	cov1	60 mm
Cover from face of section - layer 2	cov2	115 mm

**Load Data**

Ref	Pier	Load Case	P	M	Stress
			kN	kNm	Allowance
1	P61	Combination 1 - P + Traffic Load Only	2904.0	2.7	100%
2	P61	Combination 1 - P + Traffic Load Only	2904.0	54.8	100%
3	P62	Combination 1 - P + Traffic Load Only	2812.0	2.7	100%
4	P62	Combination 1 - P + Traffic Load Only	2812.0	54.8	100%

$$f_c := f_c \cdot \text{MPa} \quad f_{ys} := f_{ys} \cdot \text{MPa} \quad f_y := f_y \cdot \text{MPa} \quad D := D \cdot \text{mm} \quad ts := ts \cdot \text{mm}$$

$$\text{dia1} := \text{dia1} \cdot \text{mm} \quad \text{dia2} := \text{dia2} \cdot \text{mm} \quad \text{cov1} := \text{cov1} \cdot \text{mm} \quad \text{cov2} := \text{cov2} \cdot \text{mm}$$

$$P := P \cdot \text{kN} \quad M := M \cdot \text{kN} \cdot \text{m}$$

$$E_S := 200000 \cdot \text{MPa} \quad E_C := 4700 \sqrt{\frac{f_c}{\text{MPa}}} \cdot \text{MPa} \quad \text{Modular ratio} \quad \alpha := \begin{cases} \frac{E_S}{E_C} & \text{if } E_C > 0 \\ 1 & \text{otherwise} \end{cases} \quad \alpha = 7.77$$

$$E_C = 25743 \text{ MPa}$$

### Calculate Basic Allowable Stresses

Calculate rupture stress:

$$\sigma_{ct} := 0.5 \cdot \left( \frac{f_c}{\text{MPa}} \right)^{\frac{2}{3}} \cdot \text{MPa} \quad \sigma_{ct} = 4.8 \text{ MPa}$$

Calculate basic allowable stress of concrete

$$\sigma_{cc} := 1.0 \cdot f_c \quad \sigma_{cc} = 30.0 \text{ MPa}$$

Calculate basic allowable tensile stress of rebar

$$\sigma_{rs} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 170 \text{ MPa} \\ 170 \text{ MPa} & \text{otherwise} \end{cases} \quad \sigma_{rs} = 170 \text{ MPa}$$

Calculate basic allowable compressive stress of rebar

$$\sigma_{rc} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 110 \text{ MPa} \\ f_y & \text{otherwise} \end{cases} \quad \sigma_{rc} = 390 \text{ MPa}$$

Calculate basic allowable stress of structural steel

$$\sigma_{ts} := -0.6 f_{ys} \quad \sigma_{ts} = -150 \text{ MPa}$$

$$\sigma_{tc} := 1 f_{ys} \quad \sigma_{tc} = 250 \text{ MPa}$$

Limiting strain of rebar

$$\epsilon_{rs} := -\frac{\sigma_{rs}}{E_S} \quad \epsilon_{rs} = -0.000850$$

$$\epsilon_{rc} := \frac{\sigma_{rc}}{E_S} \quad \epsilon_{rc} = 0.001950$$

Limiting strain of structural steel

$$\epsilon_{ts} := \frac{\sigma_{ts}}{E_S} \quad \epsilon_{ts} = -0.000750$$

$$\epsilon_{tc} := \frac{\sigma_{tc}}{E_S} \quad \epsilon_{tc} = 0.001250$$



### Concrete Cross Section Data - generated

n := 50      Number of Points - 50 points maximum

i := 1 .. n + 1      Range from 1 to n+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	550
2	-69	-546	27	69	546
3	-137	-533	28	137	533
4	-202	-511	29	202	511
5	-265	-482	30	265	482
6	-323	-445	31	323	445
7	-377	-401	32	377	401
8	-424	-351	33	424	351
9	-464	-295	34	464	295
10	-498	-234	35	498	234
11	-523	-170	36	523	170
12	-540	-103	37	540	103
13	-549	-35	38	549	35
14	-549	35	39	549	-35
15	-540	103	40	540	-103
16	-523	170	41	523	-170
17	-498	234	42	498	-234
18	-464	295	43	464	-295
19	-424	351	44	424	-351
20	-377	401	45	377	-401
21	-323	445	46	323	-445
22	-265	482	47	265	-482
23	-202	511	48	202	-511
24	-137	533	49	137	-533
25	-69	546	50	69	-546

k := 1 .. 25      XS1 := XS1·mm    XS2 := XS2·mm      YS1 := YS1·mm    YS2 := YS2·mm

$x_k := XS1_k$        $y_k := YS1_k$        $x_{k+25} := XS2_k$        $y_{k+25} := YS2_k$        $x_{n+1} := XS1_1$        $y_{n+1} := YS1_1$

### Calculate Section Properties of Concrete Section

$$A_C := - \sum_{i=1}^n \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{2} \right] \quad A_C = 0.94783 \text{ m}^2$$

$$x_C := - \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{y_{i+1} - y_i}{8} \cdot \left[ (x_{i+1} + x_i)^2 + \frac{(x_{i+1} - x_i)^2}{3} \right] \right] \quad x_C = 0 \text{ m}$$

$$y_C := \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{x_{i+1} - x_i}{8} \cdot \left[ (y_{i+1} + y_i)^2 + \frac{(y_{i+1} - y_i)^2}{3} \right] \right] \quad y_C = 0 \text{ m}$$

$$I_x := \sum_{i=1}^n \left[ \left[ (x_{i+1} - x_i) \cdot \frac{y_{i+1} + y_i}{24} \right] \cdot \left[ (y_{i+1} + y_i)^2 + (y_{i+1} - y_i)^2 \right] \right] \quad I_x = 0.07149 \text{ m}^4$$

$$I_y := - \sum_{i=1}^n \left[ \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{24} \right] \cdot \left[ (x_{i+1} + x_i)^2 + (x_{i+1} - x_i)^2 \right] \right] \quad I_y = 0.07149 \text{ m}^4$$

$$I_{xC} := I_x - A_C \cdot x_C^2 \quad I_{xC} = 0.07149 \text{ m}^4$$

$$I_{yC} := I_y - A_C \cdot y_C^2 \quad I_{yC} = 0.07149 \text{ m}^4$$

### Steel Tube Cross Section Data - generated from input

ns := 50      Number of Points - 50 points maximum

ps := 1 .. ns + 1      Range from 1 to ns+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	-550
2	-142	-531	27	142	-531
3	-275	-476	28	275	-476
4	-389	-389	29	389	-389
5	-476	-275	30	476	-275
6	-531	-142	31	531	-142
7	-550	0	32	550	0
8	-531	142	33	531	142
9	-476	275	34	476	275
10	-389	389	35	389	389
11	-275	476	36	275	476
12	-142	531	37	142	531
13	0	550	38	0	550
14	142	531	39	-142	531
15	275	476	40	-275	476
16	389	389	41	-389	389
17	476	275	42	-476	275
18	531	142	43	-531	142
19	550	0	44	-550	0
20	531	-142	45	-531	-142
21	476	-275	46	-476	-275
22	389	-389	47	-389	-389
23	275	-476	48	-275	-476
24	142	-531	49	-142	-531
25	0	-550	50	0	-550

XSS1 := XSS1·mm      XSS2 := XSS2·mm      YSS1 := YSS1·mm      YSS2 := YSS2·mm

z := 1 .. 25       $xs_z := XSS1_z$        $ys_z := YSS1_z$

z := 26 .. 50       $xs_z := XSS2_{z-25}$        $ys_z := YSS2_{z-25}$

$xs_{ns+1} := XSS1_1$        $ys_{ns+1} := YSS1_1$

### Calculate Section Properties of Steel Tube Section

$$A_{ST} := - \sum_{ps=1}^{ns} \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{2} \right] \quad A_{ST} = 0 \text{ m}^2$$

$$x_{ST} := - \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{y_{ps+1}^{s} - y_{ps}^{s}}{8} \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + \frac{(x_{ps+1}^{s} - x_{ps}^{s})^2}{3} \right] \right] \quad x_{ST} = 0.2 \text{ m}$$

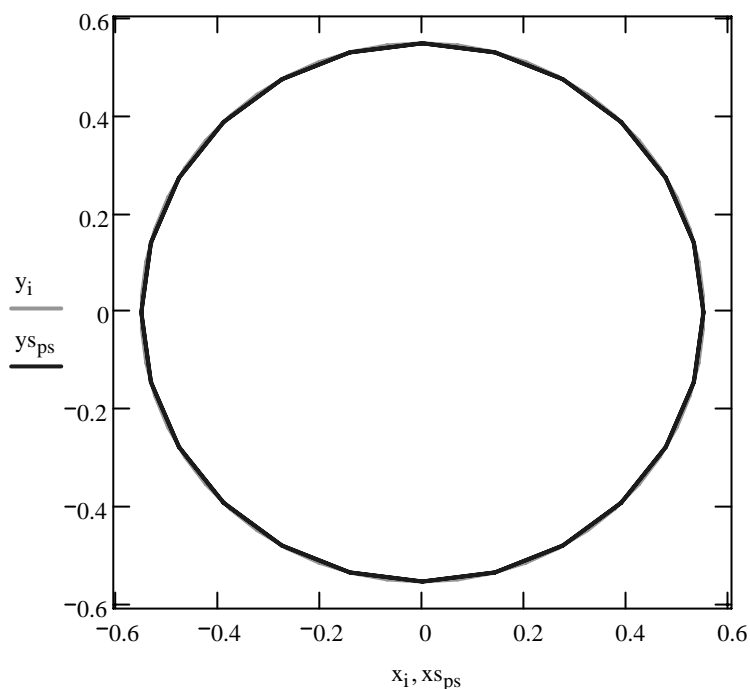
$$y_{ST} := \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{x_{ps+1}^{s} - x_{ps}^{s}}{8} \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + \frac{(y_{ps+1}^{s} - y_{ps}^{s})^2}{3} \right] \right] \quad y_{ST} = -0.011 \text{ m}$$

$$I_{xS} := \sum_{ps=1}^{ns} \left[ \left[ (x_{ps+1}^{s} - x_{ps}^{s}) \cdot \frac{y_{ps+1}^{s} + y_{ps}^{s}}{24} \right] \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + (y_{ps+1}^{s} - y_{ps}^{s})^2 \right] \right] \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := - \sum_{ps=1}^{ns} \left[ \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{24} \right] \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + (x_{ps+1}^{s} - x_{ps}^{s})^2 \right] \right] \quad I_{yS} = 0 \text{ m}^4$$

$$I_{xS} := I_{xS} - A_{ST} \cdot x_{ST}^2 \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := I_{yS} - A_{ST} \cdot y_{ST}^2 \quad I_{yS} = 0.00000 \text{ m}^4$$



**Rebar Data Layer 1 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	804	0	-474	51	0	0	0
2	804	-237	-410	52	0	0	0
3	804	-410	-237	53	0	0	0
4	804	-474	0	54	0	0	0
5	804	-410	237	55	0	0	0
6	804	-237	410	56	0	0	0
7	804	0	474	57	0	0	0
8	804	237	410	58	0	0	0
9	804	410	237	59	0	0	0
10	804	474	0	60	0	0	0
11	804	410	-237	61	0	0	0
12	804	237	-410	62	0	0	0
13	0	0	0	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

**Rebar Data Layer 2 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	0	0	0	51	0	0	0
2	0	0	0	52	0	0	0
3	0	0	0	53	0	0	0
4	0	0	0	54	0	0	0
5	0	0	0	55	0	0	0
6	0	0	0	56	0	0	0
7	0	0	0	57	0	0	0
8	0	0	0	58	0	0	0
9	0	0	0	59	0	0	0
10	0	0	0	60	0	0	0
11	0	0	0	61	0	0	0
12	0	0	0	62	0	0	0
13	0	0	0	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

$$A1 := A1 \cdot \text{mm}^2 \quad A2 := A2 \cdot \text{mm}^2 \quad A3 := A3 \cdot \text{mm}^2 \quad A4 := A4 \cdot \text{mm}^2$$

$$X1 := X1 \cdot \text{mm} \quad X2 := X2 \cdot \text{mm} \quad X3 := X3 \cdot \text{mm} \quad X4 := X4 \cdot \text{mm}$$

$$Y1 := Y1 \cdot \text{mm} \quad Y2 := Y2 \cdot \text{mm} \quad Y3 := Y3 \cdot \text{mm} \quad Y4 := Y4 \cdot \text{mm}$$

$$k := 1..50$$

$$A_{\text{bar}_k} := A1_k \quad x_{\text{bar}_k} := X1_k \quad y_{\text{bar}_k} := Y1_k$$

$$A_{\text{bar}_{k+50}} := A2_k \quad x_{\text{bar}_{k+50}} := X2_k \quad y_{\text{bar}_{k+50}} := Y2_k$$

$$A_{\text{bar}_{k+100}} := A3_k \quad x_{\text{bar}_{k+100}} := X3_k \quad y_{\text{bar}_{k+100}} := Y3_k$$

$$A_{\text{bar}_{k+150}} := A4_k \quad x_{\text{bar}_{k+150}} := X4_k \quad y_{\text{bar}_{k+150}} := Y4_k$$

### Calculate Section Properties of Reinforcement

$$A_{\text{BAR}} := \sum_{j=1}^{200} A_{\text{bar}_j} \quad A_{\text{BAR}} = 9651 \text{ mm}^2$$

$$\rho := \frac{A_{\text{BAR}}}{A_C} \quad \rho = 0.0102$$

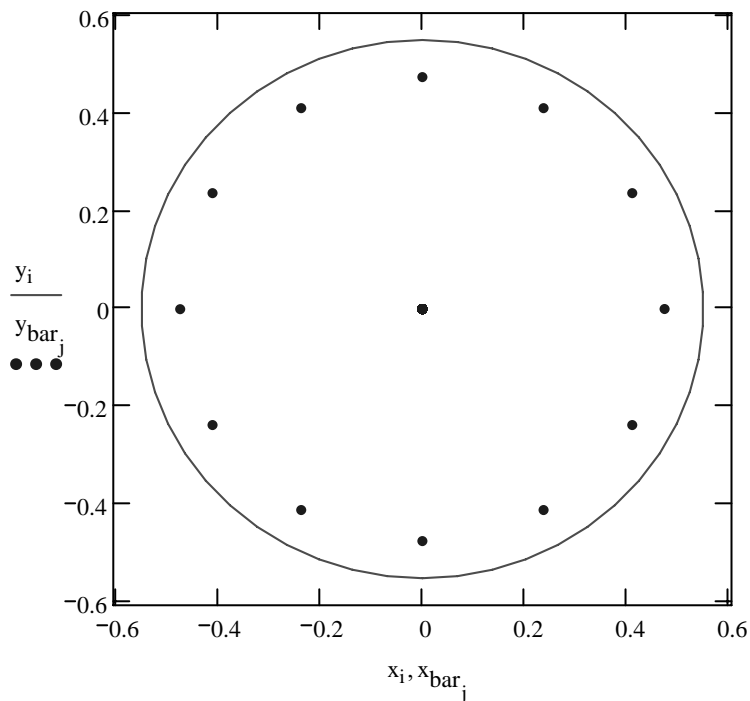
$$x_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot x_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad x_b = 0 \text{ m}$$

$$y_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot y_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad y_b = 0 \text{ m}$$

$$I_{x_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (x_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot x_b^2 \quad I_{x_b} = 0.00108 \text{ m}^4$$

$$I_{y_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (y_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot y_b^2 \quad I_{y_b} = 0.00108 \text{ m}^4$$

$j := 1 \dots 200$



**Calculate Composite Section Properties (before cracking)**

Effective area  $A_E := A_C \cdot [1 + \rho \cdot (\alpha - 1)] + A_{ST} \cdot \alpha$   $A_E = 1013161 \text{ mm}^2$

Effective centroid  $x_E := \frac{A_C \cdot [(1 - \rho) \cdot x_C + \rho \cdot x_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot x_{ST}}{A_E}$   $x_E = 0.000 \text{ m}$

$y_E := \frac{A_C \cdot [(1 - \rho) \cdot y_C + \rho \cdot y_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot y_{ST}}{A_E}$   $y_E = 0.000 \text{ m}$

Effective stiffness  $I_{EX} := I_{xC} + I_{xb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot x_C^2 + \rho \cdot x_b^2 \cdot \alpha] + (I_{xS} + A_{ST} \cdot x_{ST}^2) \cdot \alpha$   
 $I_{EX} = 0 \text{ m}^4$

$I_{EY} := I_{yC} + I_{yb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot y_C^2 + \rho \cdot y_b^2 \cdot \alpha] + (I_{yS} + A_{ST} \cdot y_{ST}^2) \cdot \alpha$   
 $I_{EY} = 0 \text{ m}^4$

Distance from extreme concrete fiber to centroid

$x_{F_{pos}} := \max(x - x_E)$   $x_{F_{neg}} := \min(x - x_E)$

$y_{F_{pos}} := \max(y - y_E)$   $y_{F_{neg}} := \min(y - y_E)$

Total depth of concrete section

$H_{CX} := x_{F_{pos}} - x_{F_{neg}}$   $H_{CX} = 1 \text{ m}$

$H_{CY} := y_{F_{pos}} - y_{F_{neg}}$   $H_{CY} = 1 \text{ m}$



Section modulus

$$Z_{Xpos} := \frac{I_{EX}}{xF_{pos}} \quad Z_{Xneg} := \frac{I_{EX}}{xF_{neg}}$$

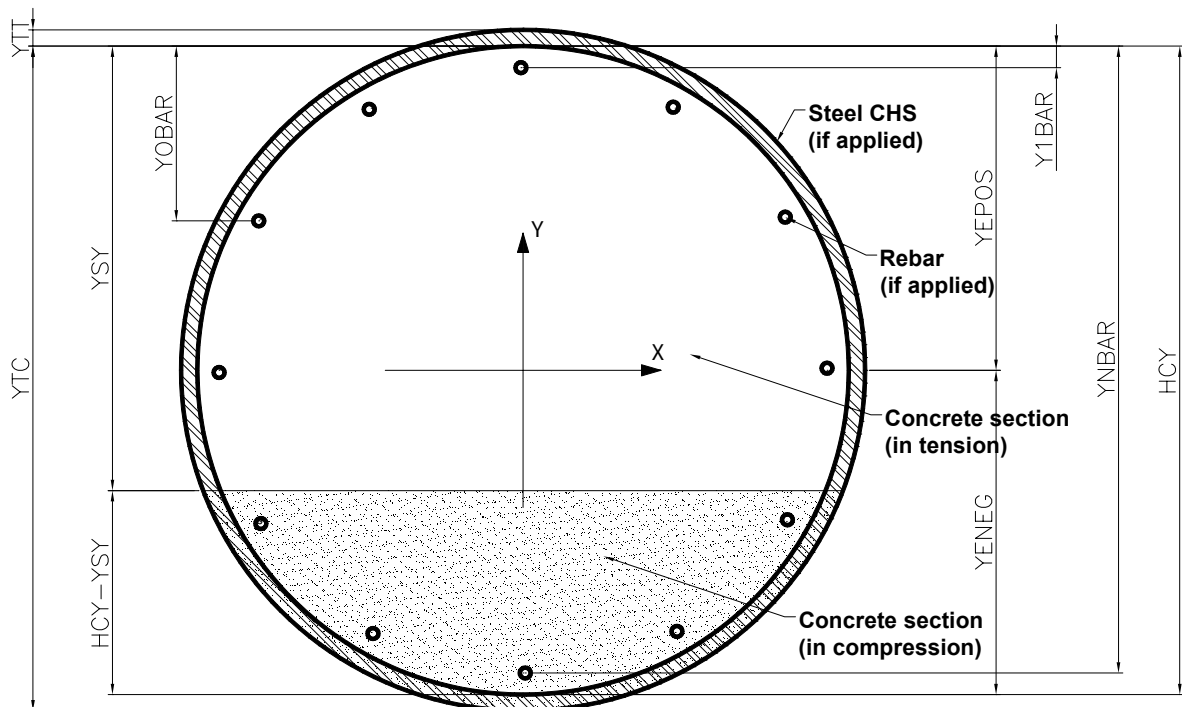
$$Z_{Ypos} := \frac{I_{EY}}{yF_{pos}} \quad Z_{Yneg} := \frac{I_{EY}}{yF_{neg}}$$

Thickness of steel tube:

$$ts := y_1 - ys_1 \quad ts = 0 \text{ mm}$$

**Establish Section Dimensions**

Positive case - determine coord of extreme concrete fiber	$y_{Epos} := \max(y)$	$y_{Epos} = 550 \text{ mm}$
Negative case - determine coord of extreme concrete fiber	$y_{Eneg} := \min(y)$	$y_{Eneg} = -550 \text{ mm}$
Offsets of rebar from extreme fiber	$y_{Obar} := y_{Epos} - y_{bar}$	
Determine most extreme rebar (minimum offset)	$y_{1bar} := \min(y_{Epos} - y_{bar})$	$y_{1bar} = 76 \text{ mm}$
Determine most extreme rebar (maximum offset)	$y_{nbar} := \max(y_{Epos} - y_{bar})$	$y_{nbar} = 1024 \text{ mm}$
Offsets of extreme steel tube fiber from extreme concrete fiber	$y_{tt} := ts$	$y_{tt} = 0 \text{ mm}$
	$y_{tc} := H_{CY} + ts$	$y_{tc} = 1100 \text{ mm}$



**ASSIGN NEUTRAL AXIS VALUES**

Number of sections to analysed                      ns := 500

q := 2 .. ns

Distance of neutral axis from extreme fiber in tension                       $y_{SY_q} := H_{CY} \cdot \frac{q}{ns + 1}$

**Calculate stresses and strains in reinforcement and concrete at extreme fibers**

Calculate strain at extreme compression fiber assuming max allowable stress in concrete:

Trial value of concrete strain

$$\epsilon_{cc} := \frac{\sigma_{cc}}{E_C} \cdot 2 \qquad \frac{\sigma_{cc}}{E_C} = 0.001165$$

Given

$$\sigma_{cc} = \epsilon_{cc} \cdot \left( 4700 \sqrt{\frac{f_c \cdot 2}{MPa}} - \frac{4700^2}{2.68} \cdot \epsilon_{cc} \right) \cdot MPa$$

$$\epsilon_{cc} := \text{Find}(\epsilon_{cc}) \qquad \epsilon_{cc} = 0.003321$$

$$\epsilon_{cc} := \begin{cases} \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \epsilon_{cc} & \text{otherwise} \end{cases} \qquad \epsilon_{cc} = 0.003321$$

Strain at other stresses taken to be linear:

$$\epsilon_{cc}(f_c, \sigma_{cd}) := \begin{cases} \frac{\sigma_{cd}}{\sigma_{tc}} \cdot \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \frac{\sigma_{cd}}{\sigma_{rc}} \cdot \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \frac{\sigma_{cd}}{\sigma_{cc}} \cdot \epsilon_{cc} & \text{otherwise} \end{cases}$$

Calculate strain in steel tube assuming max allowable stress in concrete:

$$\begin{aligned} \text{In compression} \quad \epsilon_{tcc_q} &:= \epsilon_{cc} \cdot \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \\ \text{In tension} \quad \epsilon_{tct_q} &:= \epsilon_{cc} \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \end{aligned}$$

Calculate strain in rebar assuming max allowable stress in concrete:

$$\begin{array}{l} \text{In} \\ \text{compression} \end{array} \quad \varepsilon_{rcq} := \varepsilon_{cc} \cdot \frac{y_{nbar} - y_{SYq}}{H_{CY} - y_{SYq}}$$

$$\begin{array}{l} \text{In} \\ \text{tension} \end{array} \quad \varepsilon_{rtq} := \varepsilon_{cc} \cdot \frac{y_{1bar} - y_{SYq}}{H_{CY} - y_{SYq}}$$

Calculate design max stress in compression taking account of other limits:

$$\sigma_{cd}(\varepsilon_{tcc}, q) := \left\{ \begin{array}{l} \sigma_{cd} \leftarrow \sigma_{cc} \quad \text{if } f_c > 0 \\ \sigma_{cd} \leftarrow \sigma_{tc} \quad \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \sigma_{cd} \leftarrow \sigma_{rc} \quad \text{if } (f_c = 0) \cdot (ts = 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{tc}}{\varepsilon_{tcc}} \quad \text{if } (\varepsilon_{tcc} > \varepsilon_{tc}) \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rc}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SYq}}{H_{CY} - y_{SYq}}} \quad \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SYq}}{H_{CY} - y_{SYq}} > \varepsilon_{rc} \right] \cdot (A_{BAR} > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{ts}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SYq} + y_{tt})}{H_{CY} - y_{SYq}}} \quad \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SYq} + y_{tt})}{H_{CY} - y_{SYq}} < \varepsilon_{ts} \right] \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rs}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SYq} - y_{1bar})}{H_{CY} - y_{SYq}}} \quad \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SYq} - y_{1bar})}{H_{CY} - y_{SYq}} < \varepsilon_{rs} \right] \cdot (A_{BAR} > 0) \\ \sigma_{cc} \quad \text{otherwise} \end{array} \right.$$

$$\sigma_{cdq} := \sigma_{cd}(\varepsilon_{tccq}, q)$$

**CALCULATE FORCES AND MOMENTS AT EACH NEUTRAL AXIS LOCATION**

Calculate force in concrete:

$$F_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from concrete about column centroid:

$$M_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] \cdot y dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in rebar assuming design max stress in concrete:

$$y_{SY_q} := \begin{cases} y_{nbar} \cdot \frac{q}{ns + 1} & \text{if } (f_c = 0) \cdot (A_{BAR} > 0) \\ y_{SY_q} & \text{otherwise} \end{cases}$$

$$\varepsilon_{S_{j,q}} := \begin{cases} \frac{y_{SY_q} - y_{Obar_j}}{y_{nbar} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{if } f_c = 0 \\ \frac{y_{SY_q} - y_{Obar_j}}{H_{CY} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{otherwise} \end{cases}$$

Calculate force in each rebar:

$$F_{S_{j,q}} := \begin{cases} \varepsilon_{S_{j,q}} \cdot E_S \cdot A_{bar_j} & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total force in reinforcement:

$$F_{R_q} := \sum_j F_{S_{j,q}}$$

Calculate moment from reinforcement about section centroid:

$$M_{R_q} := \begin{cases} \sum_j -(\varepsilon_{S_{j,q}} E_S A_{bar_j} y_{bar_j}) & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in steel tube at extreme tension fiber:

$$\varepsilon_{tds_q} := \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate strain in steel tube at extreme compression fiber:

$$\varepsilon_{tdc_q} := \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate tensile force in steel tube:

$$F_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS} := \begin{cases} F_{TS1} - F_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate compressive force in steel tube:

$$F_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TC2_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TC} := \begin{cases} F_{TC1} - F_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from tensile force in steel tube:

$$M_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} -2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} -2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS} := \begin{cases} M_{TS1} - M_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from compressive force in steel tube:

$$M_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC2_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC} := \begin{cases} M_{TC1} - M_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total axial response from section:

$$F_T := F_C + F_R + F_{TS} + F_{TC}$$

$$F_{TC} := F_C$$

Calculate total moment response from section:

$$M_T := M_C + M_R + M_{TS} + M_{TC}$$

$$M_{TC} := M_C$$

**CALCULATE MAXIMUM ALLOWABLE AXIAL FORCE IN SECTION**

Limiting strain in axial  
compression:

$$\varepsilon_{cL} := \begin{cases} \min(\varepsilon_{cc}, \varepsilon_{tc}) & \text{if } (A_{BAR} = 0) \cdot (ts \neq 0) \cdot (f_c \neq 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}) & \text{if } (ts = 0) \cdot (A_{BAR} \neq 0) \cdot (f_c \neq 0) \\ \varepsilon_{tc} & \text{if } (A_{BAR} = 0) \cdot (f_c = 0) \\ \varepsilon_{rc} & \text{if } (ts = 0) \cdot (f_c = 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}, \varepsilon_{tc}) & \text{otherwise} \end{cases} \quad \varepsilon_{cL} = 0.001950$$

Limiting concrete stress in axial compression

$$\sigma_{cL} := \begin{cases} \sigma_{cd2} & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases} \quad \sigma_{cL} = 18.93 \text{ MPa}$$

$$P_{MAX} := \sigma_{cL} \cdot A_C (1 - \rho) + \varepsilon_{cL} \cdot E_S (A_{BAR} + A_{ST})$$

$$P_{MAX} = 21522.8 \text{ kN} \quad F_{T_1} := P_{MAX} \quad M_{T_1} := 0 \cdot \text{kN} \cdot \text{m}$$

$$P_{MAXC} := \sigma_{cL} \cdot A_C \cdot (1 - \rho)$$

$$P_{MAXC} = 17758.9 \text{ kN} \quad F_{TC_1} := P_{MAXC} \quad M_{TC_1} := 0 \cdot \text{kN} \cdot \text{m}$$

**CALCULATE MINIMUM ALLOWABLE AXIAL FORCE IN SECTION**

$$P_{MIN} := \begin{cases} \varepsilon_{rs} \cdot E_S (A_{BAR}) & \text{if } ts = 0 \\ \varepsilon_{ts} \cdot E_S (A_{ST}) & \text{if } A_{BAR} = 0 \\ \max(\varepsilon_{ts}, \varepsilon_{rs}) \cdot E_S (A_{BAR} + A_{ST}) & \text{otherwise} \end{cases}$$

$$P_{MIN} = -1640.7 \text{ kN} \quad F_{T_{ns+1}} := P_{MIN} \quad M_{T_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

$$\text{Limit} := \begin{cases} \min(P, F_T) \cdot 0.75 & \text{if } \min(P) > 0 \\ \min(P, F_T) \cdot 1.25 & \text{otherwise} \end{cases}$$

$$P_{MINC} := 0 \text{ kN} \quad M_{TC_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$



Diameter of Column  $D = 1100 \text{ mm}$

Percentage reinforcement  $\rho = 1.02 \%$

Thickness of CHS  $t_s = 0 \text{ mm}$

Characteristic strength of concrete

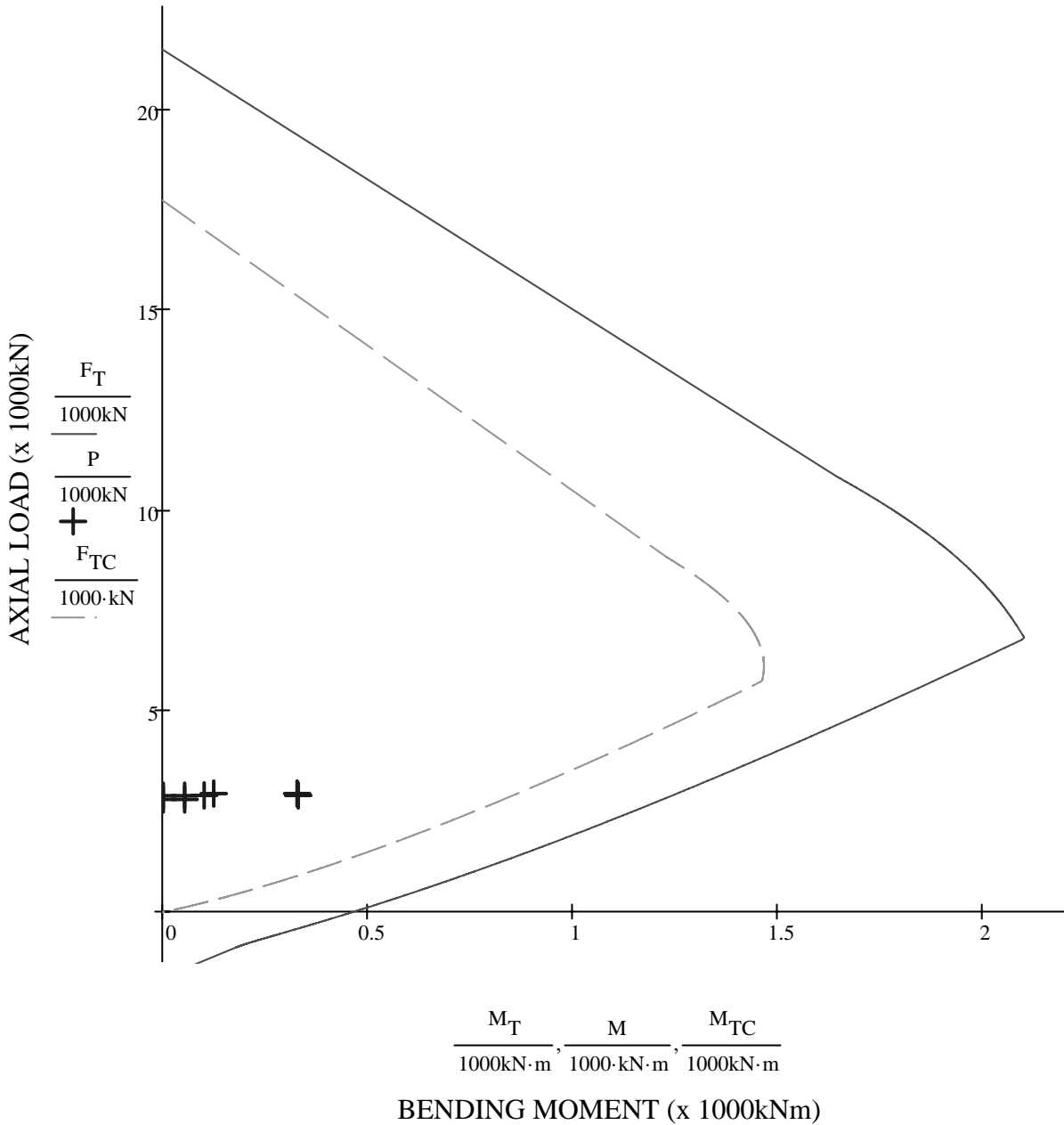
Yield Strength of Rebar

Yield Strength of CHS

$f_c = 30 \text{ MPa}$

$f_y = 390 \text{ MPa}$

$f_{ys} = 250 \text{ MPa}$



Equation of interaction line - upper region (between 1 and 2 calculation points)

$$m1 := \frac{M_{T_2} - M_{T_1}}{F_{T_2} - F_{T_1}} \quad c1 := F_{T_1}$$

Equation of interaction line - lower region (between ns and ns+1 calculation points)

$$m2 := \frac{M_{T_{ns}} - M_{T_{ns+1}}}{F_{T_{ns}} - F_{T_{ns+1}}} \quad c2 := F_{T_{ns+1}}$$

r := 1 .. 8

$$M_{SLS_r} := \begin{cases} 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r > F_{T_1} \\ 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r < F_{T_{ns+1}} \\ (P_r - c1) \cdot m1 & \text{if } (P_r > F_{T_2}) \cdot (P_r \leq F_{T_1}) \\ (P_r - c2) \cdot m2 & \text{if } (P_r \geq F_{T_{ns+1}}) \cdot (P_r < F_{T_{ns}}) \\ \text{otherwise} \\ \quad \begin{cases} j \leftarrow 1 \\ \text{while } F_{T_j} > P_r \\ \quad j \leftarrow j + 1 \\ \quad M_{T_j} \end{cases} \end{cases}$$

$$\text{StressFactor}_r := \begin{cases} \text{"No Result"} & \text{if } M_{SLS_r} < 0.000000000000000001 \cdot \text{kN}\cdot\text{m} \\ \frac{M_r}{M_{SLS_r}} & \text{otherwise} \end{cases}$$

$$P = \begin{pmatrix} 2904 \\ 2904 \\ 2812 \\ 2812 \\ 2912 \\ 2912 \\ 2959 \\ 2959 \end{pmatrix} \text{ kN} \quad M = \begin{pmatrix} 3 \\ 55 \\ 3 \\ 55 \\ 332 \\ 102 \\ 329 \\ 126 \end{pmatrix} \text{ kN}\cdot\text{m} \quad M_{SLS} = \begin{pmatrix} 1239.2 \\ 1239.2 \\ 1217.4 \\ 1217.4 \\ 1239.2 \\ 1239.2 \\ 1250.3 \\ 1250.3 \end{pmatrix} \text{ kN}\cdot\text{m} \quad \text{StressFactor} = \begin{pmatrix} 0.002 \\ 0.044 \\ 0.002 \\ 0.045 \\ 0.268 \\ 0.083 \\ 0.263 \\ 0.101 \end{pmatrix}$$

**RESULTS SUMMARY**  
**SERVICEABILITY LIMIT STATE ANALYSIS OF CIRCULAR BEAM COLUMN**

Diameter of Column		1100	mm				
Percentage of rebar		1.02	%				
Load Case Ref	Pier	Applied Service Axial Load kN	Applied Service Bending Moment kNm	Service Limit State Bending Moment kNm	Allowable Stress Factor	Applied Stress Factor	Serviceability Limit State Design Result
1	P61	2904	3	1239.2	100%	0%	OK
2	P61	2904	55	1239.2	100%	4%	OK
3	P62	2812	3	1217.4	100%	0%	OK
4	P62	2812	55	1217.4	100%	5%	OK

## **Serviceability Check - Full Live Load**



**KATAHIRA & ENGINEERS  
INTERNATIONAL**

**Project:** Detailed Design Study of  
North Java Corridor Flyover Project

**Calculation:** Balaraja Flyover  
Serviceability Check - Full Live Load  
1100 mm Dia Circular RC Column - P6 Base Section

**Reference:** Project Specific Design Criteria

**Section Data**

MPa := 1000000·Pa

kN := 1000·N

Input Item		
Concrete Compressive Strength	fc	30 MPa
Structural Steel Yield Strength	fys	250 MPa
Rebar Yield Strength	fy	390 MPa
Diameter of reinforced concrete section	D	1100 mm
Thickness of CHS section	t	0 mm
Diameter of rebar - layer 1	dia1	32 mm
Diameter of rebar - layer 2	dia2	0 mm
Number bars - layer 1 (max 100)	n1	12
Number bars - layer 2 (max 100)	n2	0
Cover from face of section - layer 1	cov1	60 mm
Cover from face of section - layer 2	cov2	115 mm

**Load Data**

Ref	Pier	Load Case	P	M	Stress
			kN	kNm	Allowance
1	P61	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+SCSH	2893.4	25.5	140%
2	P61	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+SCSH	2893.4	73.2	140%
3	P62	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+SCSH	2815.1	25.5	140%
4	P62	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+SCSH	2815.1	73.2	140%

$$f_c := f_c \cdot \text{MPa} \quad f_{ys} := f_{ys} \cdot \text{MPa} \quad f_y := f_y \cdot \text{MPa} \quad D := D \cdot \text{mm} \quad ts := ts \cdot \text{mm}$$

$$\text{dia1} := \text{dia1} \cdot \text{mm} \quad \text{dia2} := \text{dia2} \cdot \text{mm} \quad \text{cov1} := \text{cov1} \cdot \text{mm} \quad \text{cov2} := \text{cov2} \cdot \text{mm}$$

$$P := P \cdot \text{kN} \quad M := M \cdot \text{kN} \cdot \text{m}$$

$$E_S := 200000 \cdot \text{MPa} \quad E_C := 4700 \sqrt{\frac{f_c}{\text{MPa}}} \cdot \text{MPa} \quad \text{Modular ratio} \quad \alpha := \begin{cases} \frac{E_S}{E_C} & \text{if } E_C > 0 \\ 1 & \text{otherwise} \end{cases} \quad \alpha = 7.77$$

$$E_C = 25743 \text{ MPa}$$

### Calculate Basic Allowable Stresses

Calculate rupture stress:

$$\sigma_{ct} := 0.5 \cdot \left( \frac{f_c}{\text{MPa}} \right)^{\frac{2}{3}} \cdot \text{MPa} \quad \sigma_{ct} = 4.8 \text{ MPa}$$

Calculate basic allowable stress of concrete

$$\sigma_{cc} := 1.0 \cdot f_c \quad \sigma_{cc} = 30.0 \text{ MPa}$$

Calculate basic allowable tensile stress of rebar

$$\sigma_{rs} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 170 \text{ MPa} \\ 170 \text{ MPa} & \text{otherwise} \end{cases} \quad \sigma_{rs} = 170 \text{ MPa}$$

Calculate basic allowable compressive stress of rebar

$$\sigma_{rc} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 110 \text{ MPa} \\ f_y & \text{otherwise} \end{cases} \quad \sigma_{rc} = 390 \text{ MPa}$$

Calculate basic allowable stress of structural steel

$$\sigma_{ts} := -0.6 f_{ys} \quad \sigma_{ts} = -150 \text{ MPa}$$

$$\sigma_{tc} := 1 f_{ys} \quad \sigma_{tc} = 250 \text{ MPa}$$

Limiting strain of rebar

$$\epsilon_{rs} := -\frac{\sigma_{rs}}{E_S} \quad \epsilon_{rs} = -0.000850$$

$$\epsilon_{rc} := \frac{\sigma_{rc}}{E_S} \quad \epsilon_{rc} = 0.001950$$

Limiting strain of structural steel

$$\epsilon_{ts} := \frac{\sigma_{ts}}{E_S} \quad \epsilon_{ts} = -0.000750$$

$$\epsilon_{tc} := \frac{\sigma_{tc}}{E_S} \quad \epsilon_{tc} = 0.001250$$

### Concrete Cross Section Data - generated

n := 50      Number of Points - 50 points maximum

i := 1 .. n + 1      Range from 1 to n+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	550
2	-69	-546	27	69	546
3	-137	-533	28	137	533
4	-202	-511	29	202	511
5	-265	-482	30	265	482
6	-323	-445	31	323	445
7	-377	-401	32	377	401
8	-424	-351	33	424	351
9	-464	-295	34	464	295
10	-498	-234	35	498	234
11	-523	-170	36	523	170
12	-540	-103	37	540	103
13	-549	-35	38	549	35
14	-549	35	39	549	-35
15	-540	103	40	540	-103
16	-523	170	41	523	-170
17	-498	234	42	498	-234
18	-464	295	43	464	-295
19	-424	351	44	424	-351
20	-377	401	45	377	-401
21	-323	445	46	323	-445
22	-265	482	47	265	-482
23	-202	511	48	202	-511
24	-137	533	49	137	-533
25	-69	546	50	69	-546

k := 1 .. 25      XS1 := XS1·mm    XS2 := XS2·mm    YS1 := YS1·mm    YS2 := YS2·mm

$x_k := XS1_k$        $y_k := YS1_k$        $x_{k+25} := XS2_k$        $y_{k+25} := YS2_k$        $x_{n+1} := XS1_1$        $y_{n+1} := YS1_1$

### Calculate Section Properties of Concrete Section

$$A_C := - \sum_{i=1}^n \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{2} \right] \quad A_C = 0.94783 \text{ m}^2$$

$$x_C := - \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{y_{i+1} - y_i}{8} \cdot \left[ (x_{i+1} + x_i)^2 + \frac{(x_{i+1} - x_i)^2}{3} \right] \right] \quad x_C = 0 \text{ m}$$

$$y_C := \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{x_{i+1} - x_i}{8} \cdot \left[ (y_{i+1} + y_i)^2 + \frac{(y_{i+1} - y_i)^2}{3} \right] \right] \quad y_C = 0 \text{ m}$$

$$I_x := \sum_{i=1}^n \left[ \left[ (x_{i+1} - x_i) \cdot \frac{y_{i+1} + y_i}{24} \right] \cdot \left[ (y_{i+1} + y_i)^2 + (y_{i+1} - y_i)^2 \right] \right] \quad I_x = 0.07149 \text{ m}^4$$

$$I_y := - \sum_{i=1}^n \left[ \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{24} \right] \cdot \left[ (x_{i+1} + x_i)^2 + (x_{i+1} - x_i)^2 \right] \right] \quad I_y = 0.07149 \text{ m}^4$$

$$I_{xC} := I_x - A_C \cdot x_C^2 \quad I_{xC} = 0.07149 \text{ m}^4$$

$$I_{yC} := I_y - A_C \cdot y_C^2 \quad I_{yC} = 0.07149 \text{ m}^4$$



### Steel Tube Cross Section Data - generated from input

ns := 50      Number of Points - 50 points maximum

ps := 1 .. ns + 1      Range from 1 to ns+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	-550
2	-142	-531	27	142	-531
3	-275	-476	28	275	-476
4	-389	-389	29	389	-389
5	-476	-275	30	476	-275
6	-531	-142	31	531	-142
7	-550	0	32	550	0
8	-531	142	33	531	142
9	-476	275	34	476	275
10	-389	389	35	389	389
11	-275	476	36	275	476
12	-142	531	37	142	531
13	0	550	38	0	550
14	142	531	39	-142	531
15	275	476	40	-275	476
16	389	389	41	-389	389
17	476	275	42	-476	275
18	531	142	43	-531	142
19	550	0	44	-550	0
20	531	-142	45	-531	-142
21	476	-275	46	-476	-275
22	389	-389	47	-389	-389
23	275	-476	48	-275	-476
24	142	-531	49	-142	-531
25	0	-550	50	0	-550

$$XSS1 := XSS1 \cdot \text{mm}$$

$$XSS2 := XSS2 \cdot \text{mm}$$

$$YSS1 := YSS1 \cdot \text{mm}$$

$$YSS2 := YSS2 \cdot \text{mm}$$

$$z := 1 .. 25$$

$$xs_z := XSS1_z$$

$$ys_z := YSS1_z$$

$$z := 26 .. 50$$

$$xs_z := XSS2_{z-25}$$

$$ys_z := YSS2_{z-25}$$

$$xs_{ns+1} := XSS1_1$$

$$ys_{ns+1} := YSS1_1$$

### Calculate Section Properties of Steel Tube Section

$$A_{ST} := - \sum_{ps=1}^{ns} \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{2} \right] \quad A_{ST} = 0 \text{ m}^2$$

$$x_{ST} := - \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{y_{ps+1}^{s} - y_{ps}^{s}}{8} \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + \frac{(x_{ps+1}^{s} - x_{ps}^{s})^2}{3} \right] \right] \quad x_{ST} = 0.2 \text{ m}$$

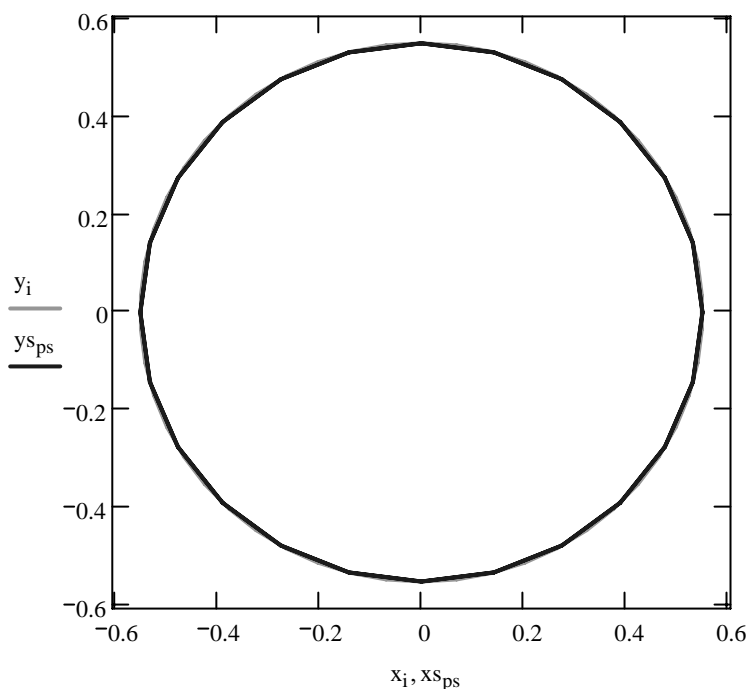
$$y_{ST} := \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{x_{ps+1}^{s} - x_{ps}^{s}}{8} \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + \frac{(y_{ps+1}^{s} - y_{ps}^{s})^2}{3} \right] \right] \quad y_{ST} = -0.011 \text{ m}$$

$$I_{xS} := \sum_{ps=1}^{ns} \left[ \left[ (x_{ps+1}^{s} - x_{ps}^{s}) \cdot \frac{y_{ps+1}^{s} + y_{ps}^{s}}{24} \right] \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + (y_{ps+1}^{s} - y_{ps}^{s})^2 \right] \right] \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := - \sum_{ps=1}^{ns} \left[ \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{24} \right] \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + (x_{ps+1}^{s} - x_{ps}^{s})^2 \right] \right] \quad I_{yS} = 0 \text{ m}^4$$

$$I_{xS} := I_{xS} - A_{ST} \cdot x_{ST}^2 \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := I_{yS} - A_{ST} \cdot y_{ST}^2 \quad I_{yS} = 0.00000 \text{ m}^4$$



**Rebar Data Layer 1 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	804	0	-474	51	0	0	0
2	804	-237	-410	52	0	0	0
3	804	-410	-237	53	0	0	0
4	804	-474	0	54	0	0	0
5	804	-410	237	55	0	0	0
6	804	-237	410	56	0	0	0
7	804	0	474	57	0	0	0
8	804	237	410	58	0	0	0
9	804	410	237	59	0	0	0
10	804	474	0	60	0	0	0
11	804	410	-237	61	0	0	0
12	804	237	-410	62	0	0	0
13	0	0	0	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

**Rebar Data Layer 2 - generated from input**

Ref	Area mm2	X mm	Y mm	Ref	Area mm2	X mm	Y mm
1	0	0	0	51	0	0	0
2	0	0	0	52	0	0	0
3	0	0	0	53	0	0	0
4	0	0	0	54	0	0	0
5	0	0	0	55	0	0	0
6	0	0	0	56	0	0	0
7	0	0	0	57	0	0	0
8	0	0	0	58	0	0	0
9	0	0	0	59	0	0	0
10	0	0	0	60	0	0	0
11	0	0	0	61	0	0	0
12	0	0	0	62	0	0	0
13	0	0	0	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

$$A1 := A1 \cdot \text{mm}^2 \quad A2 := A2 \cdot \text{mm}^2 \quad A3 := A3 \cdot \text{mm}^2 \quad A4 := A4 \cdot \text{mm}^2$$

$$X1 := X1 \cdot \text{mm} \quad X2 := X2 \cdot \text{mm} \quad X3 := X3 \cdot \text{mm} \quad X4 := X4 \cdot \text{mm}$$

$$Y1 := Y1 \cdot \text{mm} \quad Y2 := Y2 \cdot \text{mm} \quad Y3 := Y3 \cdot \text{mm} \quad Y4 := Y4 \cdot \text{mm}$$

$$k := 1..50$$

$$A_{\text{bar}_k} := A1_k \quad x_{\text{bar}_k} := X1_k \quad y_{\text{bar}_k} := Y1_k$$

$$A_{\text{bar}_{k+50}} := A2_k \quad x_{\text{bar}_{k+50}} := X2_k \quad y_{\text{bar}_{k+50}} := Y2_k$$

$$A_{\text{bar}_{k+100}} := A3_k \quad x_{\text{bar}_{k+100}} := X3_k \quad y_{\text{bar}_{k+100}} := Y3_k$$

$$A_{\text{bar}_{k+150}} := A4_k \quad x_{\text{bar}_{k+150}} := X4_k \quad y_{\text{bar}_{k+150}} := Y4_k$$

### Calculate Section Properties of Reinforcement

$$A_{\text{BAR}} := \sum_{j=1}^{200} A_{\text{bar}_j} \quad A_{\text{BAR}} = 9651 \text{ mm}^2$$

$$\rho := \frac{A_{\text{BAR}}}{A_C} \quad \rho = 0.0102$$

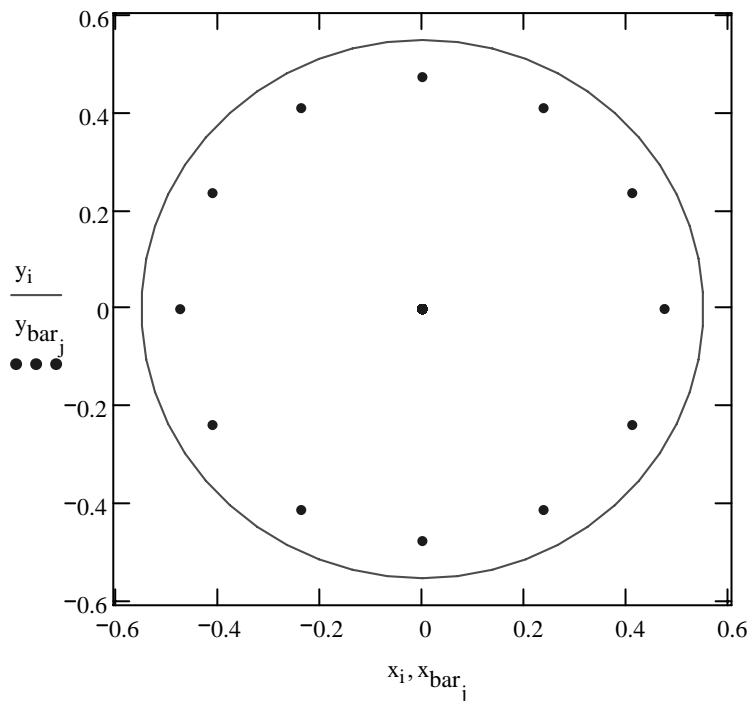
$$x_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot x_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad x_b = 0 \text{ m}$$

$$y_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot y_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad y_b = 0 \text{ m}$$

$$I_{x_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (x_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot x_b^2 \quad I_{x_b} = 0.00108 \text{ m}^4$$

$$I_{y_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (y_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot y_b^2 \quad I_{y_b} = 0.00108 \text{ m}^4$$

$j := 1 .. 200$



**Calculate Composite Section Properties (before cracking)**

Effective area  $A_E := A_C \cdot [1 + \rho \cdot (\alpha - 1)] + A_{ST} \cdot \alpha$   $A_E = 1013161 \text{ mm}^2$

Effective centroid  $x_E := \frac{A_C \cdot [(1 - \rho) \cdot x_C + \rho \cdot x_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot x_{ST}}{A_E}$   $x_E = 0.000 \text{ m}$

$y_E := \frac{A_C \cdot [(1 - \rho) \cdot y_C + \rho \cdot y_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot y_{ST}}{A_E}$   $y_E = 0.000 \text{ m}$

Effective stiffness  $I_{EX} := I_{xC} + I_{xb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot x_C^2 + \rho \cdot x_b^2 \cdot \alpha] + (I_{xS} + A_{ST} \cdot x_{ST}^2) \cdot \alpha$   
 $I_{EX} = 0 \text{ m}^4$

$I_{EY} := I_{yC} + I_{yb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot y_C^2 + \rho \cdot y_b^2 \cdot \alpha] + (I_{yS} + A_{ST} \cdot y_{ST}^2) \cdot \alpha$   
 $I_{EY} = 0 \text{ m}^4$

Distance from extreme concrete fiber to centroid

$x_{F_{pos}} := \max(x - x_E)$   $x_{F_{neg}} := \min(x - x_E)$

$y_{F_{pos}} := \max(y - y_E)$   $y_{F_{neg}} := \min(y - y_E)$

Total depth of concrete section

$H_{CX} := x_{F_{pos}} - x_{F_{neg}}$   $H_{CX} = 1 \text{ m}$

$H_{CY} := y_{F_{pos}} - y_{F_{neg}}$   $H_{CY} = 1 \text{ m}$

Section modulus

$$Z_{Xpos} := \frac{I_{EX}}{xF_{pos}}$$

$$Z_{Xneg} := \frac{I_{EX}}{xF_{neg}}$$

$$Z_{Ypos} := \frac{I_{EY}}{yF_{pos}}$$

$$Z_{Yneg} := \frac{I_{EY}}{yF_{neg}}$$

Thickness of steel tube:

$$ts := y_1 - ys_1$$

$$ts = 0 \text{ mm}$$

**Establish Section Dimensions**

Positive case - determine coord of extreme concrete fiber

$$y_{Epos} := \max(y)$$

$$y_{Epos} = 550 \text{ mm}$$

Negative case - determine coord of extreme concrete fiber

$$y_{Eneg} := \min(y)$$

$$y_{Eneg} = -550 \text{ mm}$$

Offsets of rebar from extreme fiber

$$y_{Obar} := y_{Epos} - y_{bar}$$

Determine most extreme rebar (minimum offset)

$$y_{1bar} := \min(y_{Epos} - y_{bar})$$

$$y_{1bar} = 76 \text{ mm}$$

Determine most extreme rebar (maximum offset)

$$y_{nbar} := \max(y_{Epos} - y_{bar})$$

$$y_{nbar} = 1024 \text{ mm}$$

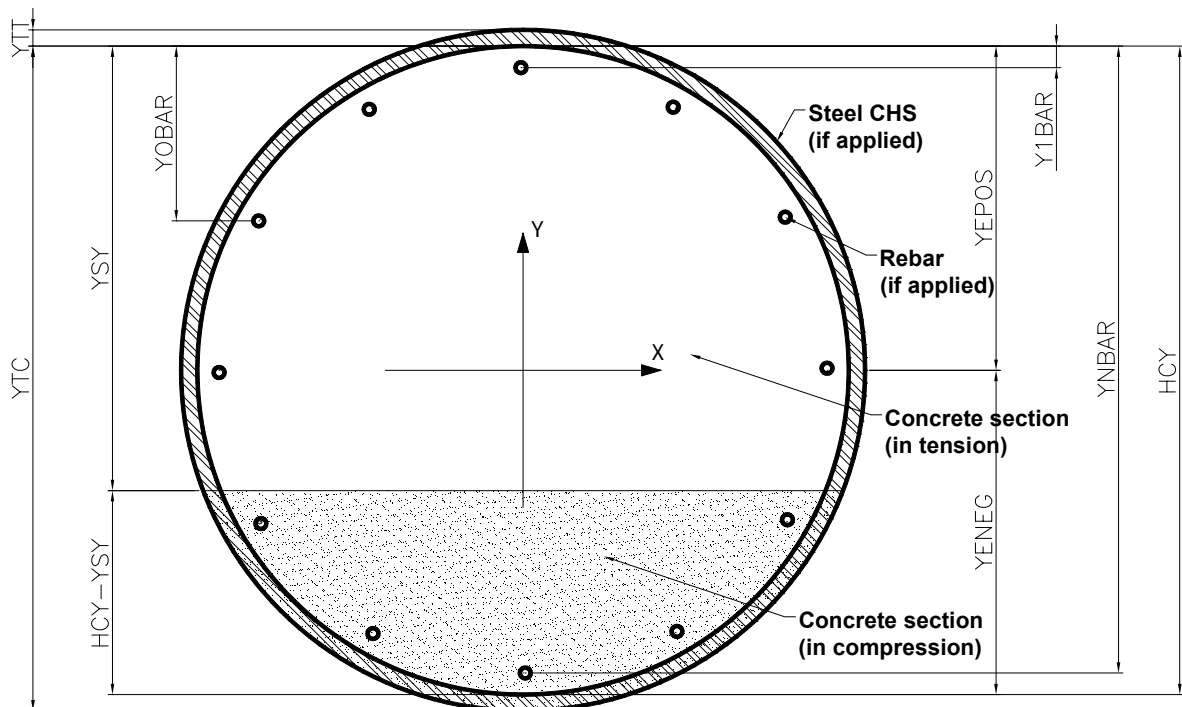
Offsets of extreme steel tube fiber from extreme concrete fiber

$$y_{tt} := ts$$

$$y_{tt} = 0 \text{ mm}$$

$$y_{tc} := H_{CY} + ts$$

$$y_{tc} = 1100 \text{ mm}$$



**ASSIGN NEUTRAL AXIS VALUES**

Number of sections to analysed                      ns := 500

q := 2 .. ns

Distance of neutral axis from extreme fiber in tension                       $y_{SY_q} := H_{CY} \cdot \frac{q}{ns + 1}$

**Calculate stresses and strains in reinforcement and concrete at extreme fibers**

Calculate strain at extreme compression fiber assuming max allowable stress in concrete:

Trial value of concrete strain

$$\epsilon_{cc} := \frac{\sigma_{cc}}{E_C} \cdot 2 \qquad \frac{\sigma_{cc}}{E_C} = 0.001165$$

Given

$$\sigma_{cc} = \epsilon_{cc} \cdot \left( 4700 \sqrt{\frac{f_c \cdot 2}{MPa}} - \frac{4700^2}{2.68} \cdot \epsilon_{cc} \right) \cdot MPa$$

$$\epsilon_{cc} := \text{Find}(\epsilon_{cc}) \qquad \epsilon_{cc} = 0.003321$$

$$\epsilon_{cc} := \begin{cases} \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \epsilon_{cc} & \text{otherwise} \end{cases} \qquad \epsilon_{cc} = 0.003321$$

Strain at other stresses taken to be linear:

$$\epsilon_{cc}(f_c, \sigma_{cd}) := \begin{cases} \frac{\sigma_{cd}}{\sigma_{tc}} \cdot \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \frac{\sigma_{cd}}{\sigma_{rc}} \cdot \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \frac{\sigma_{cd}}{\sigma_{cc}} \cdot \epsilon_{cc} & \text{otherwise} \end{cases}$$

Calculate strain in steel tube assuming max allowable stress in concrete:

In compression                       $\epsilon_{tcc_q} := \epsilon_{cc} \cdot \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}}$

In tension                               $\epsilon_{tct_q} := \epsilon_{cc} \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}}$



Calculate strain in rebar assuming max allowable stress in concrete:

$$\text{In compression} \quad \varepsilon_{rcc_q} := \varepsilon_{cc} \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

$$\text{In tension} \quad \varepsilon_{rct_q} := \varepsilon_{cc} \cdot \frac{y_{1bar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

Calculate design max stress in compression taking account of other limits:

$$\sigma_{cd}(\varepsilon_{tcc}, q) := \begin{cases} \sigma_{cd} \leftarrow \sigma_{cc} & \text{if } f_c > 0 \\ \sigma_{cd} \leftarrow \sigma_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \sigma_{cd} \leftarrow \sigma_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{tc}}{\varepsilon_{tcc}} & \text{if } (\varepsilon_{tcc} > \varepsilon_{tc}) \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rc}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}} & \text{if } \left( \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}} > \varepsilon_{rc} \right) \cdot (A_{BAR} > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{ts}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}}} & \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} < \varepsilon_{ts} \right] \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rs}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}}} & \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}} < \varepsilon_{rs} \right] \cdot (A_{BAR} > 0) \\ \sigma_{cc} & \text{otherwise} \end{cases}$$

$$\sigma_{cd_q} := \sigma_{cd}(\varepsilon_{tcc_q}, q)$$

**CALCULATE FORCES AND MOMENTS AT EACH NEUTRAL AXIS LOCATION**

Calculate force in concrete:

$$F_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from concrete about column centroid:

$$M_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] \cdot y dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in rebar assuming design max stress in concrete:

$$y_{SY_q} := \begin{cases} y_{nbar} \cdot \frac{q}{ns + 1} & \text{if } (f_c = 0) \cdot (A_{BAR} > 0) \\ y_{SY_q} & \text{otherwise} \end{cases}$$

$$\varepsilon_{S_{j,q}} := \begin{cases} \frac{y_{SY_q} - y_{Obar_j}}{y_{nbar} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{if } f_c = 0 \\ \frac{y_{SY_q} - y_{Obar_j}}{H_{CY} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{otherwise} \end{cases}$$

Calculate force in each rebar:

$$F_{S_{j,q}} := \begin{cases} \varepsilon_{S_{j,q}} \cdot E_S \cdot A_{bar_j} & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total force in reinforcement:

$$F_{R_q} := \sum_j F_{S_{j,q}}$$

Calculate moment from reinforcement about section centroid:

$$M_{R_q} := \begin{cases} \sum_j -(\varepsilon_{S_{j,q}} E_S A_{bar_j} y_{bar_j}) & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in steel tube at extreme tension fiber:

$$\varepsilon_{tds_q} := \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate strain in steel tube at extreme compression fiber:

$$\varepsilon_{tdc_q} := \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate tensile force in steel tube:

$$F_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS} := \begin{cases} F_{TS1} - F_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate compressive force in steel tube:

$$F_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TC2q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] dy$$

$$F_{TC} := \begin{cases} F_{TC1} - F_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from tensile force in steel tube:

$$M_{TS1q} := \int_{\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2} + y_{tt}} -2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS2q} := \int_{\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} -2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS} := \begin{cases} M_{TS1} - M_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from compressive force in steel tube:

$$M_{TC1q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC2q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC} := \begin{cases} M_{TC1} - M_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total axial response from section:

$$F_T := F_C + F_R + F_{TS} + F_{TC}$$

$$F_{TC} := F_C$$

Calculate total moment response from section:

$$M_T := M_C + M_R + M_{TS} + M_{TC}$$

$$M_{TC} := M_C$$

**CALCULATE MAXIMUM ALLOWABLE AXIAL FORCE IN SECTION**

Limiting strain in axial  
compression:

$$\varepsilon_{cL} := \begin{cases} \min(\varepsilon_{cc}, \varepsilon_{tc}) & \text{if } (A_{BAR} = 0) \cdot (ts \neq 0) \cdot (f_c \neq 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}) & \text{if } (ts = 0) \cdot (A_{BAR} \neq 0) \cdot (f_c \neq 0) \\ \varepsilon_{tc} & \text{if } (A_{BAR} = 0) \cdot (f_c = 0) \\ \varepsilon_{rc} & \text{if } (ts = 0) \cdot (f_c = 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}, \varepsilon_{tc}) & \text{otherwise} \end{cases} \quad \varepsilon_{cL} = 0.001950$$

Limiting concrete stress in axial compression

$$\sigma_{cL} := \begin{cases} \sigma_{cd2} & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases} \quad \sigma_{cL} = 18.93 \text{ MPa}$$

$$P_{MAX} := \sigma_{cL} \cdot A_C (1 - \rho) + \varepsilon_{cL} \cdot E_S (A_{BAR} + A_{ST})$$

$$P_{MAX} = 21522.8 \text{ kN} \quad F_{T_1} := P_{MAX} \quad M_{T_1} := 0 \cdot \text{kN} \cdot \text{m}$$

$$P_{MAXC} := \sigma_{cL} \cdot A_C \cdot (1 - \rho)$$

$$P_{MAXC} = 17758.9 \text{ kN} \quad F_{TC_1} := P_{MAXC} \quad M_{TC_1} := 0 \cdot \text{kN} \cdot \text{m}$$

**CALCULATE MINIMUM ALLOWABLE AXIAL FORCE IN SECTION**

$$P_{MIN} := \begin{cases} \varepsilon_{rs} \cdot E_S (A_{BAR}) & \text{if } ts = 0 \\ \varepsilon_{ts} \cdot E_S (A_{ST}) & \text{if } A_{BAR} = 0 \\ \max(\varepsilon_{ts}, \varepsilon_{rs}) \cdot E_S (A_{BAR} + A_{ST}) & \text{otherwise} \end{cases}$$

$$P_{MIN} = -1640.7 \text{ kN} \quad F_{T_{ns+1}} := P_{MIN} \quad M_{T_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

$$\text{Limit} := \begin{cases} \min(P, F_T) \cdot 0.75 & \text{if } \min(P) > 0 \\ \min(P, F_T) \cdot 1.25 & \text{otherwise} \end{cases}$$

$$P_{MINC} := 0 \text{ kN} \quad M_{TC_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

Diameter of Column  $D = 1100 \text{ mm}$

Percentage reinforcement  $\rho = 1.02 \%$

Thickness of CHS  $t_s = 0 \text{ mm}$

Characteristic strength of concrete

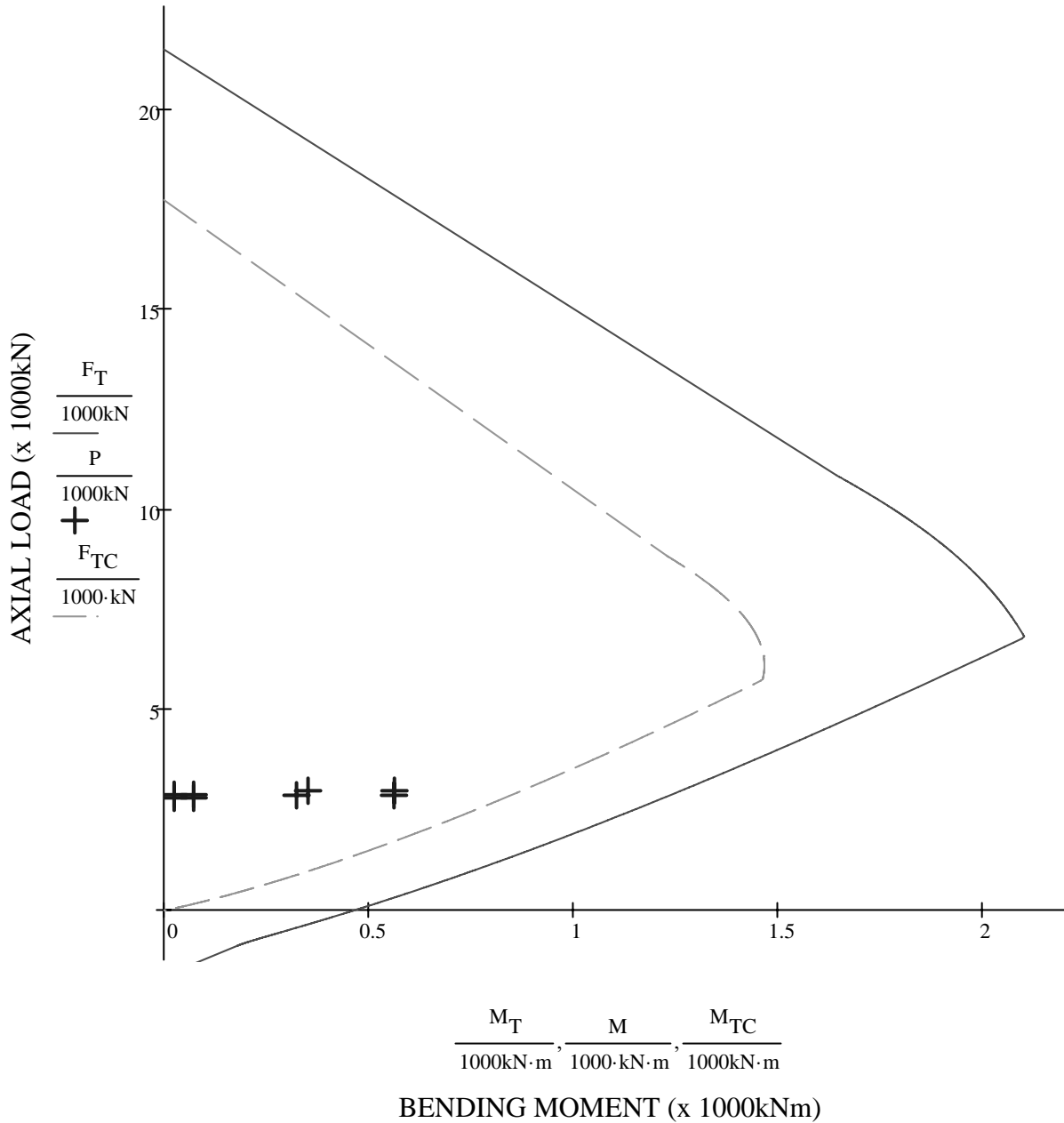
Yield Strength of Rebar

Yield Strength of CHS

$f_c = 30 \text{ MPa}$

$f_y = 390 \text{ MPa}$

$f_{ys} = 250 \text{ MPa}$



INTERACTION CURVE AT SERVICEABILITY LIMIT STATE

Equation of interaction line - upper region (between 1 and 2 calculation points)

$$m1 := \frac{M_{T_2} - M_{T_1}}{F_{T_2} - F_{T_1}} \quad c1 := F_{T_1}$$

Equation of interaction line - lower region (between ns and ns+1 calculation points)

$$m2 := \frac{M_{T_{ns}} - M_{T_{ns+1}}}{F_{T_{ns}} - F_{T_{ns+1}}} \quad c2 := F_{T_{ns+1}}$$

r := 1 .. 8

$$M_{SLS_r} := \begin{cases} 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r > F_{T_1} \\ 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r < F_{T_{ns+1}} \\ (P_r - c1) \cdot m1 & \text{if } (P_r > F_{T_2}) \cdot (P_r \leq F_{T_1}) \\ (P_r - c2) \cdot m2 & \text{if } (P_r \geq F_{T_{ns+1}}) \cdot (P_r < F_{T_{ns}}) \\ \text{otherwise} \\ \quad j \leftarrow 1 \\ \quad \text{while } F_{T_j} > P_r \\ \quad \quad j \leftarrow j + 1 \\ \quad M_{T_j} \end{cases}$$

$$\text{StressFactor}_r := \begin{cases} \text{"No Result"} & \text{if } M_{SLS_r} < 0.000000000000000001 \cdot \text{kN}\cdot\text{m} \\ \frac{M_r}{M_{SLS_r}} & \text{otherwise} \end{cases}$$

$$P = \begin{pmatrix} 2893 \\ 2893 \\ 2815 \\ 2815 \\ 2881 \\ 2881 \\ 2994 \\ 2994 \end{pmatrix} \text{ kN} \quad M = \begin{pmatrix} 26 \\ 73 \\ 26 \\ 73 \\ 563 \\ 325 \\ 564 \\ 353 \end{pmatrix} \text{ kN}\cdot\text{m} \quad M_{SLS} = \begin{pmatrix} 1239.2 \\ 1239.2 \\ 1217.4 \\ 1217.4 \\ 1228.2 \\ 1228.2 \\ 1261.5 \\ 1261.5 \end{pmatrix} \text{ kN}\cdot\text{m} \quad \text{StressFactor} = \begin{pmatrix} 0.021 \\ 0.059 \\ 0.021 \\ 0.060 \\ 0.458 \\ 0.264 \\ 0.447 \\ 0.280 \end{pmatrix}$$



**RESULTS SUMMARY**  
**SERVICEABILITY LIMIT STATE ANALYSIS OF CIRCULAR BEAM COLUMN**

Diameter of Column		1100	mm				
Percentage of rebar		1.02	%				
Load Case Ref	Pier	Applied Service Axial Load kN	Applied Service Bending Moment kNm	Service Limit State Bending Moment kNm	Allowable Stress Factor	Applied Stress Factor	Serviceability Limit State Design Result
1	P61	2893	26	1239.2	140%	2%	OK
2	P61	2893	73	1239.2	140%	6%	OK
3	P62	2815	26	1217.4	140%	2%	OK
4	P62	2815	73	1217.4	140%	6%	OK

**P7 PORTAL COLUMN 1.1 M DIAMETER**

**TOP**

## **Serviceability Check - Traffic Load Only**



**KATAHIRA & ENGINEERS  
INTERNATIONAL**

**Project:** Detailed Design Study of  
North Java Corridor Flyover Project

**Calculation:** Balaraja Flyover  
Serviceability Check - Traffic Load Only  
1100 mm Dia Circular RC Column - P7 Top Section

**Reference:** Project Specific Design Criteria

**Section Data**

MPa := 1000000·Pa

kN := 1000·N

Input Item		
Concrete Compressive Strength	fc	30 MPa
Structural Steel Yield Strength	fys	250 MPa
Rebar Yield Strength	fy	390 MPa
Diameter of reinforced concrete section	D	1100 mm
Thickness of CHS section	t	0 mm
Diameter of rebar - layer 1	dia1	32 mm
Diameter of rebar - layer 2	dia2	0 mm
Number bars - layer 1 (max 100)	n1	39
Number bars - layer 2 (max 100)	n2	0
Cover from face of section - layer 1	cov1	60 mm
Cover from face of section - layer 2	cov2	115 mm

**Load Data**

Ref	Pier	Load Case	P	M	Stress
			kN	kNm	Allowance
1	P71	Combination 1 - P + Traffic Load Only	3181.8	486.6	100%
2	P71	Combination 1 - P + Traffic Load Only	3181.8	2143.0	100%
3	P72	Combination 1 - P + Traffic Load Only	3161.5	496.5	100%
4	P72	Combination 1 - P + Traffic Load Only	3161.5	2127.7	100%

$$f_c := f_c \cdot \text{MPa} \quad f_{ys} := f_{ys} \cdot \text{MPa} \quad f_y := f_y \cdot \text{MPa} \quad D := D \cdot \text{mm} \quad ts := ts \cdot \text{mm}$$

$$\text{dia1} := \text{dia1} \cdot \text{mm} \quad \text{dia2} := \text{dia2} \cdot \text{mm} \quad \text{cov1} := \text{cov1} \cdot \text{mm} \quad \text{cov2} := \text{cov2} \cdot \text{mm}$$

$$P := P \cdot \text{kN} \quad M := M \cdot \text{kN} \cdot \text{m}$$

$$E_S := 200000 \cdot \text{MPa} \quad E_C := 4700 \sqrt{\frac{f_c}{\text{MPa}}} \cdot \text{MPa} \quad \text{Modular ratio} \quad \alpha := \begin{cases} \frac{E_S}{E_C} & \text{if } E_C > 0 \\ 1 & \text{otherwise} \end{cases} \quad \alpha = 7.77$$

$$E_C = 25743 \text{ MPa}$$

### Calculate Basic Allowable Stresses

Calculate rupture stress:

$$\sigma_{ct} := 0.5 \cdot \left( \frac{f_c}{\text{MPa}} \right)^{\frac{2}{3}} \cdot \text{MPa} \quad \sigma_{ct} = 4.8 \text{ MPa}$$

Calculate basic allowable stress of concrete

$$\sigma_{cc} := 1.0 \cdot f_c \quad \sigma_{cc} = 30.0 \text{ MPa}$$

Calculate basic allowable tensile stress of rebar

$$\sigma_{rs} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 170 \text{ MPa} \\ 170 \text{ MPa} & \text{otherwise} \end{cases} \quad \sigma_{rs} = 170 \text{ MPa}$$

Calculate basic allowable compressive stress of rebar

$$\sigma_{rc} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 110 \text{ MPa} \\ f_y & \text{otherwise} \end{cases} \quad \sigma_{rc} = 390 \text{ MPa}$$

Calculate basic allowable stress of structural steel

$$\sigma_{ts} := -0.6 f_{ys} \quad \sigma_{ts} = -150 \text{ MPa}$$

$$\sigma_{tc} := 1 f_{ys} \quad \sigma_{tc} = 250 \text{ MPa}$$

Limiting strain of rebar

$$\epsilon_{rs} := -\frac{\sigma_{rs}}{E_S} \quad \epsilon_{rs} = -0.000850$$

$$\epsilon_{rc} := \frac{\sigma_{rc}}{E_S} \quad \epsilon_{rc} = 0.001950$$

Limiting strain of structural steel

$$\epsilon_{ts} := \frac{\sigma_{ts}}{E_S} \quad \epsilon_{ts} = -0.000750$$

$$\epsilon_{tc} := \frac{\sigma_{tc}}{E_S} \quad \epsilon_{tc} = 0.001250$$

### Concrete Cross Section Data - generated

n := 50      Number of Points - 50 points maximum

i := 1 .. n + 1      Range from 1 to n+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	550
2	-69	-546	27	69	546
3	-137	-533	28	137	533
4	-202	-511	29	202	511
5	-265	-482	30	265	482
6	-323	-445	31	323	445
7	-377	-401	32	377	401
8	-424	-351	33	424	351
9	-464	-295	34	464	295
10	-498	-234	35	498	234
11	-523	-170	36	523	170
12	-540	-103	37	540	103
13	-549	-35	38	549	35
14	-549	35	39	549	-35
15	-540	103	40	540	-103
16	-523	170	41	523	-170
17	-498	234	42	498	-234
18	-464	295	43	464	-295
19	-424	351	44	424	-351
20	-377	401	45	377	-401
21	-323	445	46	323	-445
22	-265	482	47	265	-482
23	-202	511	48	202	-511
24	-137	533	49	137	-533
25	-69	546	50	69	-546

k := 1 .. 25      XS1 := XS1·mm    XS2 := XS2·mm    YS1 := YS1·mm    YS2 := YS2·mm

$x_k := XS1_k$        $y_k := YS1_k$        $x_{k+25} := XS2_k$        $y_{k+25} := YS2_k$        $x_{n+1} := XS1_1$        $y_{n+1} := YS1_1$

### Calculate Section Properties of Concrete Section

$$A_C := - \sum_{i=1}^n \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{2} \right] \quad A_C = 0.94783 \text{ m}^2$$

$$x_C := - \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{y_{i+1} - y_i}{8} \cdot \left[ (x_{i+1} + x_i)^2 + \frac{(x_{i+1} - x_i)^2}{3} \right] \right] \quad x_C = 0 \text{ m}$$

$$y_C := \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{x_{i+1} - x_i}{8} \cdot \left[ (y_{i+1} + y_i)^2 + \frac{(y_{i+1} - y_i)^2}{3} \right] \right] \quad y_C = 0 \text{ m}$$

$$I_x := \sum_{i=1}^n \left[ \left[ (x_{i+1} - x_i) \cdot \frac{y_{i+1} + y_i}{24} \right] \cdot \left[ (y_{i+1} + y_i)^2 + (y_{i+1} - y_i)^2 \right] \right] \quad I_x = 0.07149 \text{ m}^4$$

$$I_y := - \sum_{i=1}^n \left[ \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{24} \right] \cdot \left[ (x_{i+1} + x_i)^2 + (x_{i+1} - x_i)^2 \right] \right] \quad I_y = 0.07149 \text{ m}^4$$

$$I_{xC} := I_x - A_C \cdot x_C^2 \quad I_{xC} = 0.07149 \text{ m}^4$$

$$I_{yC} := I_y - A_C \cdot y_C^2 \quad I_{yC} = 0.07149 \text{ m}^4$$



### Steel Tube Cross Section Data - generated from input

ns := 50      Number of Points - 50 points maximum

ps := 1 .. ns + 1      Range from 1 to ns+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	-550
2	-142	-531	27	142	-531
3	-275	-476	28	275	-476
4	-389	-389	29	389	-389
5	-476	-275	30	476	-275
6	-531	-142	31	531	-142
7	-550	0	32	550	0
8	-531	142	33	531	142
9	-476	275	34	476	275
10	-389	389	35	389	389
11	-275	476	36	275	476
12	-142	531	37	142	531
13	0	550	38	0	550
14	142	531	39	-142	531
15	275	476	40	-275	476
16	389	389	41	-389	389
17	476	275	42	-476	275
18	531	142	43	-531	142
19	550	0	44	-550	0
20	531	-142	45	-531	-142
21	476	-275	46	-476	-275
22	389	-389	47	-389	-389
23	275	-476	48	-275	-476
24	142	-531	49	-142	-531
25	0	-550	50	0	-550

$$XSS1 := XSS1 \cdot \text{mm}$$

$$XSS2 := XSS2 \cdot \text{mm}$$

$$YSS1 := YSS1 \cdot \text{mm}$$

$$YSS2 := YSS2 \cdot \text{mm}$$

$$z := 1 .. 25$$

$$xs_z := XSS1_z$$

$$ys_z := YSS1_z$$

$$z := 26 .. 50$$

$$xs_z := XSS2_{z-25}$$

$$ys_z := YSS2_{z-25}$$

$$xs_{ns+1} := XSS1_1$$

$$ys_{ns+1} := YSS1_1$$

**Calculate Section Properties of Steel Tube Section**

$$A_{ST} := - \sum_{ps=1}^{ns} \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{2} \right] \quad A_{ST} = 0 \text{ m}^2$$

$$x_{ST} := - \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{y_{ps+1}^{s} - y_{ps}^{s}}{8} \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + \frac{(x_{ps+1}^{s} - x_{ps}^{s})^2}{3} \right] \right] \quad x_{ST} = 0.2 \text{ m}$$

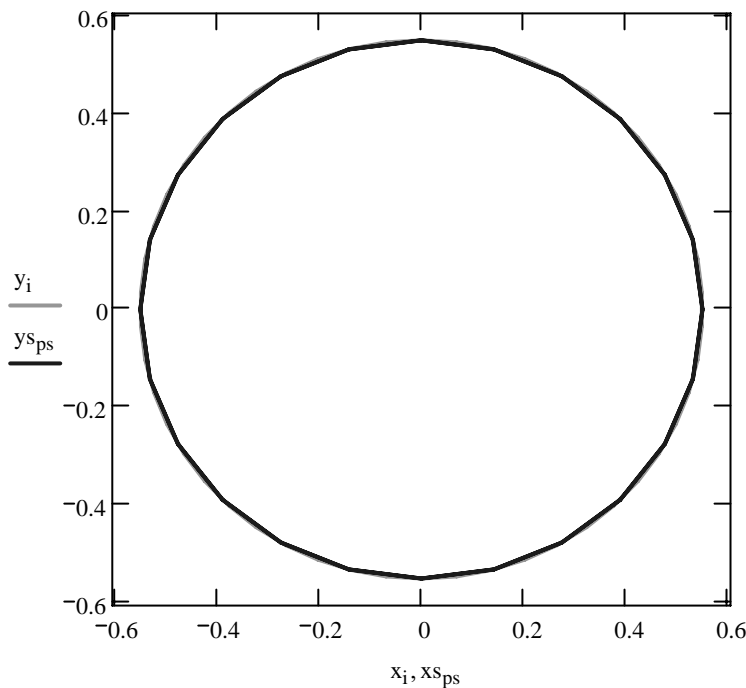
$$y_{ST} := \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{x_{ps+1}^{s} - x_{ps}^{s}}{8} \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + \frac{(y_{ps+1}^{s} - y_{ps}^{s})^2}{3} \right] \right] \quad y_{ST} = -0.011 \text{ m}$$

$$I_{xS} := \sum_{ps=1}^{ns} \left[ \left[ (x_{ps+1}^{s} - x_{ps}^{s}) \cdot \frac{y_{ps+1}^{s} + y_{ps}^{s}}{24} \right] \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + (y_{ps+1}^{s} - y_{ps}^{s})^2 \right] \right] \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := - \sum_{ps=1}^{ns} \left[ \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{24} \right] \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + (x_{ps+1}^{s} - x_{ps}^{s})^2 \right] \right] \quad I_{yS} = 0 \text{ m}^4$$

$$I_{xS} := I_{xS} - A_{ST} \cdot x_{ST}^2 \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := I_{yS} - A_{ST} \cdot y_{ST}^2 \quad I_{yS} = 0.00000 \text{ m}^4$$



**Rebar Data Layer 1 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	804	0	-474	51	0	0	0
2	804	-76	-468	52	0	0	0
3	804	-150	-450	53	0	0	0
4	804	-220	-420	54	0	0	0
5	804	-285	-379	55	0	0	0
6	804	-342	-328	56	0	0	0
7	804	-390	-269	57	0	0	0
8	804	-428	-203	58	0	0	0
9	804	-455	-132	59	0	0	0
10	804	-471	-57	60	0	0	0
11	804	-474	19	61	0	0	0
12	804	-464	95	62	0	0	0
13	804	-443	168	63	0	0	0
14	804	-410	237	64	0	0	0
15	804	-367	300	65	0	0	0
16	804	-314	355	66	0	0	0
17	804	-253	401	67	0	0	0
18	804	-186	436	68	0	0	0
19	804	-113	460	69	0	0	0
20	804	-38	472	70	0	0	0
21	804	38	472	71	0	0	0
22	804	113	460	72	0	0	0
23	804	186	436	73	0	0	0
24	804	253	401	74	0	0	0
25	804	314	355	75	0	0	0
26	804	367	300	76	0	0	0
27	804	410	237	77	0	0	0
28	804	443	168	78	0	0	0
29	804	464	95	79	0	0	0
30	804	474	19	80	0	0	0
31	804	471	-57	81	0	0	0
32	804	455	-132	82	0	0	0
33	804	428	-203	83	0	0	0
34	804	390	-269	84	0	0	0
35	804	342	-328	85	0	0	0
36	804	285	-379	86	0	0	0
37	804	220	-420	87	0	0	0
38	804	150	-450	88	0	0	0
39	804	76	-468	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

**Rebar Data Layer 2 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	0	0	0	51	0	0	0
2	0	0	0	52	0	0	0
3	0	0	0	53	0	0	0
4	0	0	0	54	0	0	0
5	0	0	0	55	0	0	0
6	0	0	0	56	0	0	0
7	0	0	0	57	0	0	0
8	0	0	0	58	0	0	0
9	0	0	0	59	0	0	0
10	0	0	0	60	0	0	0
11	0	0	0	61	0	0	0
12	0	0	0	62	0	0	0
13	0	0	0	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

$$A1 := A1 \cdot \text{mm}^2 \quad A2 := A2 \cdot \text{mm}^2 \quad A3 := A3 \cdot \text{mm}^2 \quad A4 := A4 \cdot \text{mm}^2$$

$$X1 := X1 \cdot \text{mm} \quad X2 := X2 \cdot \text{mm} \quad X3 := X3 \cdot \text{mm} \quad X4 := X4 \cdot \text{mm}$$

$$Y1 := Y1 \cdot \text{mm} \quad Y2 := Y2 \cdot \text{mm} \quad Y3 := Y3 \cdot \text{mm} \quad Y4 := Y4 \cdot \text{mm}$$

$$k := 1..50$$

$$A_{\text{bar}_k} := A1_k \quad x_{\text{bar}_k} := X1_k \quad y_{\text{bar}_k} := Y1_k$$

$$A_{\text{bar}_{k+50}} := A2_k \quad x_{\text{bar}_{k+50}} := X2_k \quad y_{\text{bar}_{k+50}} := Y2_k$$

$$A_{\text{bar}_{k+100}} := A3_k \quad x_{\text{bar}_{k+100}} := X3_k \quad y_{\text{bar}_{k+100}} := Y3_k$$

$$A_{\text{bar}_{k+150}} := A4_k \quad x_{\text{bar}_{k+150}} := X4_k \quad y_{\text{bar}_{k+150}} := Y4_k$$

### Calculate Section Properties of Reinforcement

$$A_{\text{BAR}} := \sum_{j=1}^{200} A_{\text{bar}_j} \quad A_{\text{BAR}} = 31366 \text{ mm}^2$$

$$\rho := \frac{A_{\text{BAR}}}{A_C} \quad \rho = 0.0331$$

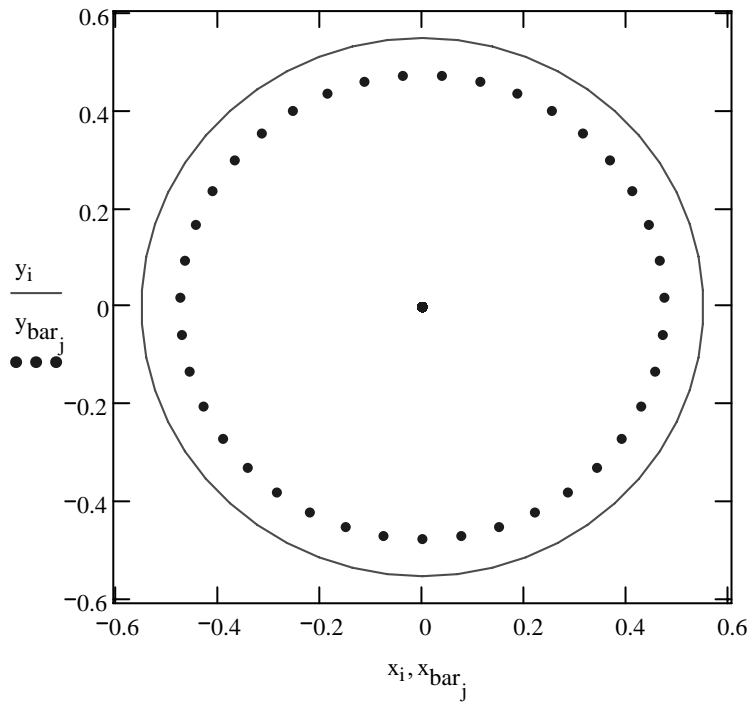
$$x_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot x_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad x_b = 0 \text{ m}$$

$$y_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot y_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad y_b = 0 \text{ m}$$

$$I_{x_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (x_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot x_b^2 \quad I_{x_b} = 0.00352 \text{ m}^4$$

$$I_{y_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (y_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot y_b^2 \quad I_{y_b} = 0.00352 \text{ m}^4$$

$j := 1 \dots 200$



**Calculate Composite Section Properties (before cracking)**

Effective area  $A_E := A_C \cdot [1 + \rho \cdot (\alpha - 1)] + A_{ST} \cdot \alpha$   $A_E = 1160150 \text{ mm}^2$

Effective centroid  $x_E := \frac{A_C \cdot [(1 - \rho) \cdot x_C + \rho \cdot x_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot x_{ST}}{A_E}$   $x_E = 0.000 \text{ m}$

$y_E := \frac{A_C \cdot [(1 - \rho) \cdot y_C + \rho \cdot y_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot y_{ST}}{A_E}$   $y_E = 0.000 \text{ m}$

Effective stiffness  $I_{EX} := I_{xC} + I_{xb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot x_C^2 + \rho \cdot x_b^2 \cdot \alpha] + (I_{xS} + A_{ST} \cdot x_{ST}^2) \cdot \alpha$   
 $I_{EX} = 0 \text{ m}^4$

$I_{EY} := I_{yC} + I_{yb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot y_C^2 + \rho \cdot y_b^2 \cdot \alpha] + (I_{yS} + A_{ST} \cdot y_{ST}^2) \cdot \alpha$   
 $I_{EY} = 0 \text{ m}^4$

Distance from extreme concrete fiber to centroid

$x_{F_{pos}} := \max(x - x_E)$   $x_{F_{neg}} := \min(x - x_E)$

$y_{F_{pos}} := \max(y - y_E)$   $y_{F_{neg}} := \min(y - y_E)$

Total depth of concrete section

$H_{CX} := x_{F_{pos}} - x_{F_{neg}}$   $H_{CX} = 1 \text{ m}$

$H_{CY} := y_{F_{pos}} - y_{F_{neg}}$   $H_{CY} = 1 \text{ m}$

Section modulus

$$Z_{Xpos} := \frac{I_{EX}}{xF_{pos}}$$

$$Z_{Xneg} := \frac{I_{EX}}{xF_{neg}}$$

$$Z_{Ypos} := \frac{I_{EY}}{yF_{pos}}$$

$$Z_{Yneg} := \frac{I_{EY}}{yF_{neg}}$$

Thickness of steel tube:

$$ts := y_1 - ys_1$$

$$ts = 0 \text{ mm}$$

**Establish Section Dimensions**

Positive case - determine coord of extreme concrete fiber

$$y_{Epos} := \max(y)$$

$$y_{Epos} = 550 \text{ mm}$$

Negative case - determine coord of extreme concrete fiber

$$y_{Eneg} := \min(y)$$

$$y_{Eneg} = -550 \text{ mm}$$

Offsets of rebar from extreme fiber

$$y_{Obar} := y_{Epos} - y_{bar}$$

Determine most extreme rebar (minimum offset)

$$y_{1bar} := \min(y_{Epos} - y_{bar})$$

$$y_{1bar} = 78 \text{ mm}$$

Determine most extreme rebar (maximum offset)

$$y_{nbar} := \max(y_{Epos} - y_{bar})$$

$$y_{nbar} = 1024 \text{ mm}$$

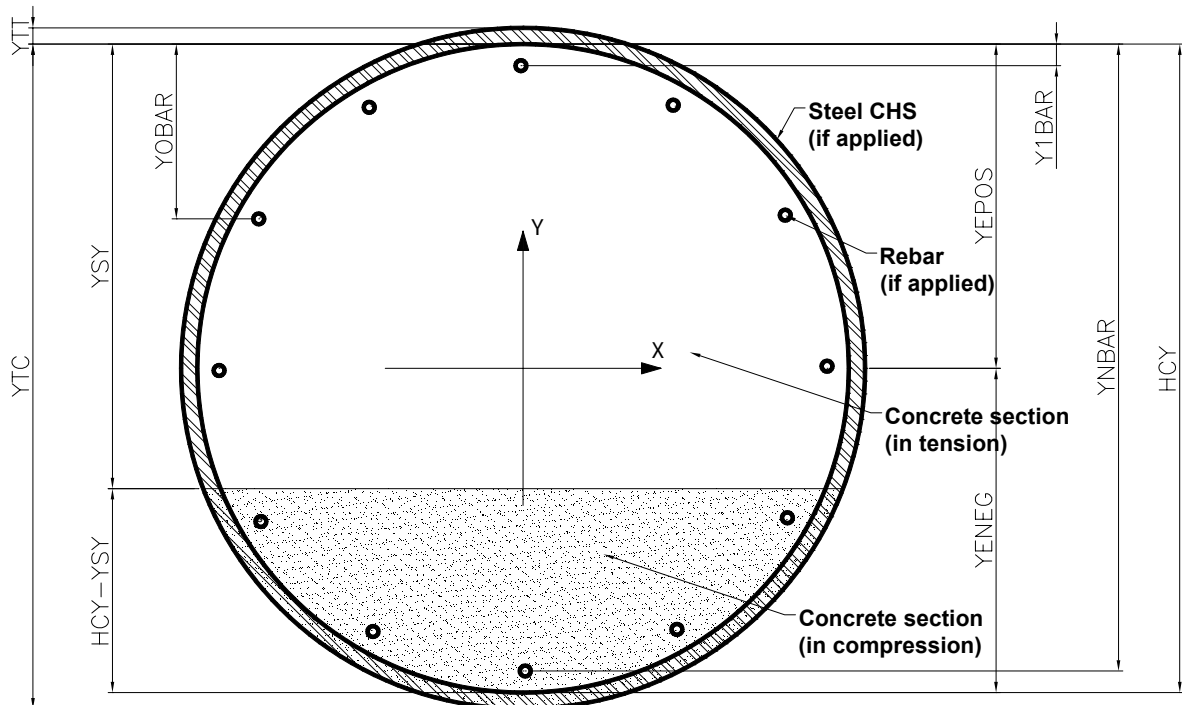
Offsets of extreme steel tube fiber from extreme concrete fiber

$$y_{tt} := ts$$

$$y_{tt} = 0 \text{ mm}$$

$$y_{tc} := H_{CY} + ts$$

$$y_{tc} = 1100 \text{ mm}$$



**ASSIGN NEUTRAL AXIS VALUES**

Number of sections to analysed                      ns := 500

q := 2 .. ns

Distance of neutral axis from extreme fiber in tension                       $y_{SY_q} := H_{CY} \cdot \frac{q}{ns + 1}$

**Calculate stresses and strains in reinforcement and concrete at extreme fibers**

Calculate strain at extreme compression fiber assuming max allowable stress in concrete:

Trial value of concrete strain

$$\epsilon_{cc} := \frac{\sigma_{cc}}{E_C} \cdot 2 \qquad \frac{\sigma_{cc}}{E_C} = 0.001165$$

Given

$$\sigma_{cc} = \epsilon_{cc} \cdot \left( 4700 \sqrt{\frac{f_c \cdot 2}{MPa}} - \frac{4700^2}{2.68} \cdot \epsilon_{cc} \right) \cdot MPa$$

$$\epsilon_{cc} := \text{Find}(\epsilon_{cc}) \qquad \epsilon_{cc} = 0.003321$$

$$\epsilon_{cc} := \begin{cases} \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \epsilon_{cc} & \text{otherwise} \end{cases} \qquad \epsilon_{cc} = 0.003321$$

Strain at other stresses taken to be linear:

$$\epsilon_{cc}(f_c, \sigma_{cd}) := \begin{cases} \frac{\sigma_{cd}}{\sigma_{tc}} \cdot \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \frac{\sigma_{cd}}{\sigma_{rc}} \cdot \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \frac{\sigma_{cd}}{\sigma_{cc}} \cdot \epsilon_{cc} & \text{otherwise} \end{cases}$$

Calculate strain in steel tube assuming max allowable stress in concrete:

$$\begin{aligned} \text{In compression} \quad \epsilon_{tcc_q} &:= \epsilon_{cc} \cdot \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \\ \text{In tension} \quad \epsilon_{tct_q} &:= \epsilon_{cc} \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \end{aligned}$$



Calculate strain in rebar assuming max allowable stress in concrete:

$$\text{In compression} \quad \varepsilon_{rcc_q} := \varepsilon_{cc} \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

$$\text{In tension} \quad \varepsilon_{rct_q} := \varepsilon_{cc} \cdot \frac{y_{1bar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

Calculate design max stress in compression taking account of other limits:

$$\sigma_{cd}(\varepsilon_{tcc}, q) := \begin{cases} \sigma_{cd} \leftarrow \sigma_{cc} & \text{if } f_c > 0 \\ \sigma_{cd} \leftarrow \sigma_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \sigma_{cd} \leftarrow \sigma_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{tc}}{\varepsilon_{tcc}} & \text{if } (\varepsilon_{tcc} > \varepsilon_{tc}) \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rc}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}} & \text{if } \left( \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}} > \varepsilon_{rc} \right) \cdot (A_{BAR} > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{ts}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}}} & \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} < \varepsilon_{ts} \right] \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rs}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}}} & \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}} < \varepsilon_{rs} \right] \cdot (A_{BAR} > 0) \\ \sigma_{cc} & \text{otherwise} \end{cases}$$

$$\sigma_{cd_q} := \sigma_{cd}(\varepsilon_{tcc_q}, q)$$

**CALCULATE FORCES AND MOMENTS AT EACH NEUTRAL AXIS LOCATION**

Calculate force in concrete:

$$F_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from concrete about column centroid:

$$M_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] \cdot y dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in rebar assuming design max stress in concrete:

$$y_{SY_q} := \begin{cases} y_{nbar} \cdot \frac{q}{ns + 1} & \text{if } (f_c = 0) \cdot (A_{BAR} > 0) \\ y_{SY_q} & \text{otherwise} \end{cases}$$

$$\varepsilon_{S_{j,q}} := \begin{cases} \frac{y_{SY_q} - y_{Obar_j}}{y_{nbar} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{if } f_c = 0 \\ \frac{y_{SY_q} - y_{Obar_j}}{H_{CY} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{otherwise} \end{cases}$$

Calculate force in each rebar:

$$F_{S_{j,q}} := \begin{cases} \varepsilon_{S_{j,q}} \cdot E_S \cdot A_{bar_j} & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total force in reinforcement:

$$F_{R_q} := \sum_j F_{S_{j,q}}$$

Calculate moment from reinforcement about section centroid:

$$M_{R_q} := \begin{cases} \sum_j -(\varepsilon_{S_{j,q}} E_S A_{bar_j} y_{bar_j}) & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in steel tube at extreme tension fiber:

$$\varepsilon_{tds_q} := \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate strain in steel tube at extreme compression fiber:

$$\varepsilon_{tdc_q} := \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate tensile force in steel tube:

$$F_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS} := \begin{cases} F_{TS1} - F_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate compressive force in steel tube:

$$F_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TC2_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TC} := \begin{cases} F_{TC1} - F_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from tensile force in steel tube:

$$M_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} -2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} -2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS} := \begin{cases} M_{TS1} - M_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from compressive force in steel tube:

$$M_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC2_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC} := \begin{cases} M_{TC1} - M_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total axial response from section:

$$F_T := F_C + F_R + F_{TS} + F_{TC}$$

$$F_{TC} := F_C$$

Calculate total moment response from section:

$$M_T := M_C + M_R + M_{TS} + M_{TC}$$

$$M_{TC} := M_C$$

**CALCULATE MAXIMUM ALLOWABLE AXIAL FORCE IN SECTION**

Limiting strain in axial  
compression:

$$\varepsilon_{cL} := \begin{cases} \min(\varepsilon_{cc}, \varepsilon_{tc}) & \text{if } (A_{BAR} = 0) \cdot (ts \neq 0) \cdot (f_c \neq 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}) & \text{if } (ts = 0) \cdot (A_{BAR} \neq 0) \cdot (f_c \neq 0) \\ \varepsilon_{tc} & \text{if } (A_{BAR} = 0) \cdot (f_c = 0) \\ \varepsilon_{rc} & \text{if } (ts = 0) \cdot (f_c = 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}, \varepsilon_{tc}) & \text{otherwise} \end{cases} \quad \varepsilon_{cL} = 0.001950$$

Limiting concrete stress in axial compression

$$\sigma_{cL} := \begin{cases} \sigma_{cd2} & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases} \quad \sigma_{cL} = 18.93 \text{ MPa}$$

$$P_{MAX} := \sigma_{cL} \cdot A_C (1 - \rho) + \varepsilon_{cL} \cdot E_S (A_{BAR} + A_{ST})$$

$$P_{MAX} = 29580.5 \text{ kN} \quad F_{T_1} := P_{MAX} \quad M_{T_1} := 0 \cdot \text{kN} \cdot \text{m}$$

$$P_{MAXC} := \sigma_{cL} \cdot A_C \cdot (1 - \rho)$$

$$P_{MAXC} = 17347.9 \text{ kN} \quad F_{TC_1} := P_{MAXC} \quad M_{TC_1} := 0 \cdot \text{kN} \cdot \text{m}$$

**CALCULATE MINIMUM ALLOWABLE AXIAL FORCE IN SECTION**

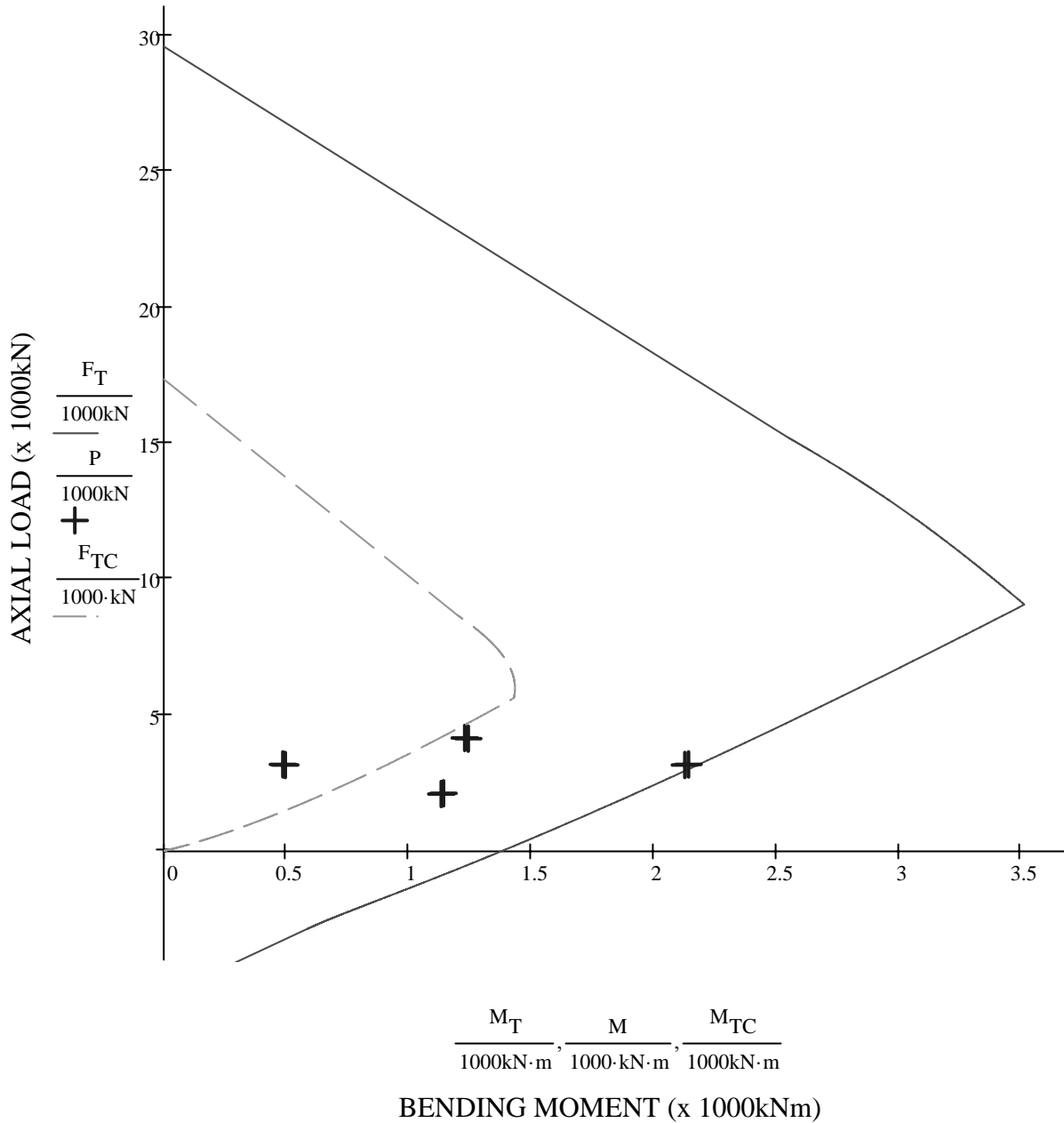
$$P_{MIN} := \begin{cases} \varepsilon_{rs} \cdot E_S (A_{BAR}) & \text{if } ts = 0 \\ \varepsilon_{ts} \cdot E_S (A_{ST}) & \text{if } A_{BAR} = 0 \\ \max(\varepsilon_{ts}, \varepsilon_{rs}) \cdot E_S (A_{BAR} + A_{ST}) & \text{otherwise} \end{cases}$$

$$P_{MIN} = -5332.2 \text{ kN} \quad F_{T_{ns+1}} := P_{MIN} \quad M_{T_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

$$\text{Limit} := \begin{cases} \min(P, F_T) \cdot 0.75 & \text{if } \min(P) > 0 \\ \min(P, F_T) \cdot 1.25 & \text{otherwise} \end{cases}$$

$$P_{MINC} := 0 \text{ kN} \quad M_{TC_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

Diameter of Column	D = 1100 mm	Characteristic strength of concrete	$f_c = 30 \text{ MPa}$
Percentage reinforcement	$\rho = 3.31 \%$	Yield Strength of Rebar	$f_y = 390 \text{ MPa}$
Thickness of CHS	$t_s = 0 \text{ mm}$	Yield Strength of CHS	$f_{ys} = 250 \text{ MPa}$



Equation of interaction line - upper region (between 1 and 2 calculation points)

$$m1 := \frac{M_{T_2} - M_{T_1}}{F_{T_2} - F_{T_1}} \quad c1 := F_{T_1}$$

Equation of interaction line - lower region (between ns and ns+1 calculation points)

$$m2 := \frac{M_{T_{ns}} - M_{T_{ns+1}}}{F_{T_{ns}} - F_{T_{ns+1}}} \quad c2 := F_{T_{ns+1}}$$

r := 1 .. 8

$$M_{SLS_r} := \begin{cases} 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r > F_{T_1} \\ 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r < F_{T_{ns+1}} \\ (P_r - c1) \cdot m1 & \text{if } (P_r > F_{T_2}) \cdot (P_r \leq F_{T_1}) \\ (P_r - c2) \cdot m2 & \text{if } (P_r \geq F_{T_{ns+1}}) \cdot (P_r < F_{T_{ns}}) \\ \text{otherwise} \\ \begin{cases} j \leftarrow 1 \\ \text{while } F_{T_j} > P_r \\ j \leftarrow j + 1 \\ M_{T_j} \end{cases} \end{cases}$$

$$\text{StressFactor}_r := \begin{cases} \text{"No Result"} & \text{if } M_{SLS_r} < 0.000000000000000001 \cdot \text{kN}\cdot\text{m} \\ \frac{M_r}{M_{SLS_r}} & \text{otherwise} \end{cases}$$

$$P = \begin{pmatrix} 3182 \\ 3182 \\ 3162 \\ 3162 \\ 2096 \\ 4131 \\ 2119 \\ 4157 \end{pmatrix} \text{ kN} \quad M = \begin{pmatrix} 487 \\ 2143 \\ 497 \\ 2128 \\ 1133 \\ 1243 \\ 1143 \\ 1229 \end{pmatrix} \text{ kN}\cdot\text{m} \quad M_{SLS} = \begin{pmatrix} 2173.3 \\ 2173.3 \\ 2173.3 \\ 2173.3 \\ 1915.3 \\ 2409.2 \\ 1915.3 \\ 2409.2 \end{pmatrix} \text{ kN}\cdot\text{m} \quad \text{StressFactor} = \begin{pmatrix} 0.224 \\ 0.986 \\ 0.228 \\ 0.979 \\ 0.592 \\ 0.516 \\ 0.597 \\ 0.510 \end{pmatrix}$$



**RESULTS SUMMARY**  
**SERVICEABILITY LIMIT STATE ANALYSIS OF CIRCULAR BEAM COLUMN**

Diameter of Column		1100	mm				
Percentage of rebar		3.31	%				
Load Case Ref	Pier	Applied Service Axial Load kN	Applied Service Bending Moment kNm	Service Limit State Bending Moment kNm	Allowable Stress Factor	Applied Stress Factor	Serviceability Limit State Design Result
1	P71	3182	487	2173.3	100%	22%	OK
2	P71	3182	2143	2173.3	100%	99%	OK
3	P72	3162	497	2173.3	100%	23%	OK
4	P72	3162	2128	2173.3	100%	98%	OK

## **Serviceability Check - Full Live Load**



**KATAHIRA & ENGINEERS  
INTERNATIONAL**

**Project:** Detailed Design Study of  
North Java Corridor Flyover Project

**Calculation:** Balaraja Flyover  
Serviceability Check - Full Live Load  
1100 mm Dia Circular RC Column - P7 Top Section

**Reference:** Project Specific Design Criteria

**Section Data**

MPa := 1000000·Pa

kN := 1000·N

Input Item		
Concrete Compressive Strength	fc	30 MPa
Structural Steel Yield Strength	fys	250 MPa
Rebar Yield Strength	fy	390 MPa
Diameter of reinforced concrete section	D	1100 mm
Thickness of CHS section	t	0 mm
Diameter of rebar - layer 1	dia1	32 mm
Diameter of rebar - layer 2	dia2	0 mm
Number bars - layer 1 (max 100)	n1	39
Number bars - layer 2 (max 100)	n2	0
Cover from face of section - layer 1	cov1	60 mm
Cover from face of section - layer 2	cov2	115 mm

**Load Data**

Ref	Pier	Load Case	P	M	Stress
			kN	kNm	Allowance
1	P71	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp	3172.9	986.0	140%
2	P71	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp	3172.9	2646.7	140%
3	P72	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp	3171.2	1004.2	140%
4	P72	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp	3171.2	2639.7	140%

$$f_c := f_c \cdot \text{MPa} \quad f_{ys} := f_{ys} \cdot \text{MPa} \quad f_y := f_y \cdot \text{MPa} \quad D := D \cdot \text{mm} \quad ts := ts \cdot \text{mm}$$

$$\text{dia1} := \text{dia1} \cdot \text{mm} \quad \text{dia2} := \text{dia2} \cdot \text{mm} \quad \text{cov1} := \text{cov1} \cdot \text{mm} \quad \text{cov2} := \text{cov2} \cdot \text{mm}$$

$$P := P \cdot \text{kN} \quad M := M \cdot \text{kN} \cdot \text{m}$$

$$E_S := 200000 \cdot \text{MPa} \quad E_C := 4700 \sqrt{\frac{f_c}{\text{MPa}}} \cdot \text{MPa} \quad \text{Modular ratio} \quad \alpha := \begin{cases} \frac{E_S}{E_C} & \text{if } E_C > 0 \\ 1 & \text{otherwise} \end{cases} \quad \alpha = 7.77$$

$$E_C = 25743 \text{ MPa}$$

### Calculate Basic Allowable Stresses

Calculate rupture stress:

$$\sigma_{ct} := 0.5 \cdot \left( \frac{f_c}{\text{MPa}} \right)^{\frac{2}{3}} \cdot \text{MPa} \quad \sigma_{ct} = 4.8 \text{ MPa}$$

Calculate basic allowable stress of concrete

$$\sigma_{cc} := 1.0 \cdot f_c \quad \sigma_{cc} = 30.0 \text{ MPa}$$

Calculate basic allowable tensile stress of rebar

$$\sigma_{rs} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 170 \text{ MPa} \\ 170 \text{ MPa} & \text{otherwise} \end{cases} \quad \sigma_{rs} = 170 \text{ MPa}$$

Calculate basic allowable compressive stress of rebar

$$\sigma_{rc} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 110 \text{ MPa} \\ f_y & \text{otherwise} \end{cases} \quad \sigma_{rc} = 390 \text{ MPa}$$

Calculate basic allowable stress of structural steel

$$\sigma_{ts} := -0.6 f_{ys} \quad \sigma_{ts} = -150 \text{ MPa}$$

$$\sigma_{tc} := 1 f_{ys} \quad \sigma_{tc} = 250 \text{ MPa}$$

Limiting strain of rebar

$$\epsilon_{rs} := -\frac{\sigma_{rs}}{E_S} \quad \epsilon_{rs} = -0.000850$$

$$\epsilon_{rc} := \frac{\sigma_{rc}}{E_S} \quad \epsilon_{rc} = 0.001950$$

Limiting strain of structural steel

$$\epsilon_{ts} := \frac{\sigma_{ts}}{E_S} \quad \epsilon_{ts} = -0.000750$$

$$\epsilon_{tc} := \frac{\sigma_{tc}}{E_S} \quad \epsilon_{tc} = 0.001250$$

### Concrete Cross Section Data - generated

n := 50      Number of Points - 50 points maximum

i := 1 .. n + 1      Range from 1 to n+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	550
2	-69	-546	27	69	546
3	-137	-533	28	137	533
4	-202	-511	29	202	511
5	-265	-482	30	265	482
6	-323	-445	31	323	445
7	-377	-401	32	377	401
8	-424	-351	33	424	351
9	-464	-295	34	464	295
10	-498	-234	35	498	234
11	-523	-170	36	523	170
12	-540	-103	37	540	103
13	-549	-35	38	549	35
14	-549	35	39	549	-35
15	-540	103	40	540	-103
16	-523	170	41	523	-170
17	-498	234	42	498	-234
18	-464	295	43	464	-295
19	-424	351	44	424	-351
20	-377	401	45	377	-401
21	-323	445	46	323	-445
22	-265	482	47	265	-482
23	-202	511	48	202	-511
24	-137	533	49	137	-533
25	-69	546	50	69	-546

k := 1 .. 25      XS1 := XS1·mm    XS2 := XS2·mm    YS1 := YS1·mm    YS2 := YS2·mm

$x_k := XS1_k$        $y_k := YS1_k$        $x_{k+25} := XS2_k$        $y_{k+25} := YS2_k$        $x_{n+1} := XS1_1$        $y_{n+1} := YS1_1$

### Calculate Section Properties of Concrete Section

$$A_C := - \sum_{i=1}^n \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{2} \right] \quad A_C = 0.94783 \text{ m}^2$$

$$x_C := - \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{y_{i+1} - y_i}{8} \cdot \left[ (x_{i+1} + x_i)^2 + \frac{(x_{i+1} - x_i)^2}{3} \right] \right] \quad x_C = 0 \text{ m}$$

$$y_C := \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{x_{i+1} - x_i}{8} \cdot \left[ (y_{i+1} + y_i)^2 + \frac{(y_{i+1} - y_i)^2}{3} \right] \right] \quad y_C = 0 \text{ m}$$

$$I_x := \sum_{i=1}^n \left[ \left[ (x_{i+1} - x_i) \cdot \frac{y_{i+1} + y_i}{24} \right] \cdot \left[ (y_{i+1} + y_i)^2 + (y_{i+1} - y_i)^2 \right] \right] \quad I_x = 0.07149 \text{ m}^4$$

$$I_y := - \sum_{i=1}^n \left[ \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{24} \right] \cdot \left[ (x_{i+1} + x_i)^2 + (x_{i+1} - x_i)^2 \right] \right] \quad I_y = 0.07149 \text{ m}^4$$

$$I_{xC} := I_x - A_C \cdot x_C^2 \quad I_{xC} = 0.07149 \text{ m}^4$$

$$I_{yC} := I_y - A_C \cdot y_C^2 \quad I_{yC} = 0.07149 \text{ m}^4$$

### Steel Tube Cross Section Data - generated from input

ns := 50      Number of Points - 50 points maximum

ps := 1 .. ns + 1      Range from 1 to ns+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	-550
2	-142	-531	27	142	-531
3	-275	-476	28	275	-476
4	-389	-389	29	389	-389
5	-476	-275	30	476	-275
6	-531	-142	31	531	-142
7	-550	0	32	550	0
8	-531	142	33	531	142
9	-476	275	34	476	275
10	-389	389	35	389	389
11	-275	476	36	275	476
12	-142	531	37	142	531
13	0	550	38	0	550
14	142	531	39	-142	531
15	275	476	40	-275	476
16	389	389	41	-389	389
17	476	275	42	-476	275
18	531	142	43	-531	142
19	550	0	44	-550	0
20	531	-142	45	-531	-142
21	476	-275	46	-476	-275
22	389	-389	47	-389	-389
23	275	-476	48	-275	-476
24	142	-531	49	-142	-531
25	0	-550	50	0	-550

$$XSS1 := XSS1 \cdot \text{mm}$$

$$XSS2 := XSS2 \cdot \text{mm}$$

$$YSS1 := YSS1 \cdot \text{mm}$$

$$YSS2 := YSS2 \cdot \text{mm}$$

$$z := 1 .. 25$$

$$xs_z := XSS1_z$$

$$ys_z := YSS1_z$$

$$z := 26 .. 50$$

$$xs_z := XSS2_{z-25}$$

$$ys_z := YSS2_{z-25}$$

$$xs_{ns+1} := XSS1_1$$

$$ys_{ns+1} := YSS1_1$$

### Calculate Section Properties of Steel Tube Section

$$A_{ST} := - \sum_{ps=1}^{ns} \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{2} \right] \quad A_{ST} = 0 \text{ m}^2$$

$$x_{ST} := - \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{y_{ps+1}^{s} - y_{ps}^{s}}{8} \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + \frac{(x_{ps+1}^{s} - x_{ps}^{s})^2}{3} \right] \right] \quad x_{ST} = 0.2 \text{ m}$$

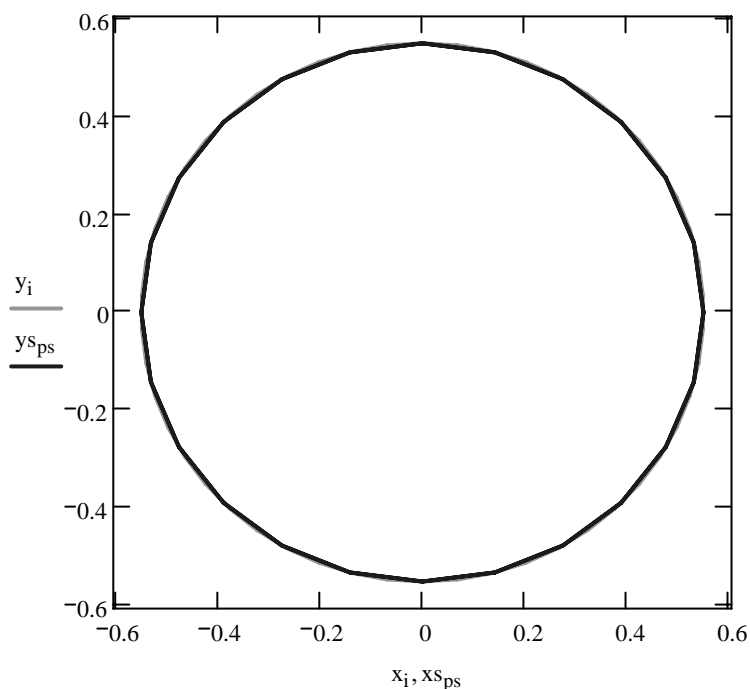
$$y_{ST} := \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{x_{ps+1}^{s} - x_{ps}^{s}}{8} \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + \frac{(y_{ps+1}^{s} - y_{ps}^{s})^2}{3} \right] \right] \quad y_{ST} = -0.011 \text{ m}$$

$$I_{xS} := \sum_{ps=1}^{ns} \left[ \left[ (x_{ps+1}^{s} - x_{ps}^{s}) \cdot \frac{y_{ps+1}^{s} + y_{ps}^{s}}{24} \right] \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + (y_{ps+1}^{s} - y_{ps}^{s})^2 \right] \right] \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := - \sum_{ps=1}^{ns} \left[ \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{24} \right] \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + (x_{ps+1}^{s} - x_{ps}^{s})^2 \right] \right] \quad I_{yS} = 0 \text{ m}^4$$

$$I_{xS} := I_{xS} - A_{ST} \cdot x_{ST}^2 \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := I_{yS} - A_{ST} \cdot y_{ST}^2 \quad I_{yS} = 0.00000 \text{ m}^4$$





**Rebar Data Layer 1 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	804	0	-474	51	0	0	0
2	804	-76	-468	52	0	0	0
3	804	-150	-450	53	0	0	0
4	804	-220	-420	54	0	0	0
5	804	-285	-379	55	0	0	0
6	804	-342	-328	56	0	0	0
7	804	-390	-269	57	0	0	0
8	804	-428	-203	58	0	0	0
9	804	-455	-132	59	0	0	0
10	804	-471	-57	60	0	0	0
11	804	-474	19	61	0	0	0
12	804	-464	95	62	0	0	0
13	804	-443	168	63	0	0	0
14	804	-410	237	64	0	0	0
15	804	-367	300	65	0	0	0
16	804	-314	355	66	0	0	0
17	804	-253	401	67	0	0	0
18	804	-186	436	68	0	0	0
19	804	-113	460	69	0	0	0
20	804	-38	472	70	0	0	0
21	804	38	472	71	0	0	0
22	804	113	460	72	0	0	0
23	804	186	436	73	0	0	0
24	804	253	401	74	0	0	0
25	804	314	355	75	0	0	0
26	804	367	300	76	0	0	0
27	804	410	237	77	0	0	0
28	804	443	168	78	0	0	0
29	804	464	95	79	0	0	0
30	804	474	19	80	0	0	0
31	804	471	-57	81	0	0	0
32	804	455	-132	82	0	0	0
33	804	428	-203	83	0	0	0
34	804	390	-269	84	0	0	0
35	804	342	-328	85	0	0	0
36	804	285	-379	86	0	0	0
37	804	220	-420	87	0	0	0
38	804	150	-450	88	0	0	0
39	804	76	-468	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

**Rebar Data Layer 2 - generated from input**

Ref	Area mm2	X mm	Y mm	Ref	Area mm2	X mm	Y mm
1	0	0	0	51	0	0	0
2	0	0	0	52	0	0	0
3	0	0	0	53	0	0	0
4	0	0	0	54	0	0	0
5	0	0	0	55	0	0	0
6	0	0	0	56	0	0	0
7	0	0	0	57	0	0	0
8	0	0	0	58	0	0	0
9	0	0	0	59	0	0	0
10	0	0	0	60	0	0	0
11	0	0	0	61	0	0	0
12	0	0	0	62	0	0	0
13	0	0	0	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

$$A1 := A1 \cdot \text{mm}^2 \quad A2 := A2 \cdot \text{mm}^2 \quad A3 := A3 \cdot \text{mm}^2 \quad A4 := A4 \cdot \text{mm}^2$$

$$X1 := X1 \cdot \text{mm} \quad X2 := X2 \cdot \text{mm} \quad X3 := X3 \cdot \text{mm} \quad X4 := X4 \cdot \text{mm}$$

$$Y1 := Y1 \cdot \text{mm} \quad Y2 := Y2 \cdot \text{mm} \quad Y3 := Y3 \cdot \text{mm} \quad Y4 := Y4 \cdot \text{mm}$$

$$k := 1..50$$

$$A_{\text{bar}_k} := A1_k \quad x_{\text{bar}_k} := X1_k \quad y_{\text{bar}_k} := Y1_k$$

$$A_{\text{bar}_{k+50}} := A2_k \quad x_{\text{bar}_{k+50}} := X2_k \quad y_{\text{bar}_{k+50}} := Y2_k$$

$$A_{\text{bar}_{k+100}} := A3_k \quad x_{\text{bar}_{k+100}} := X3_k \quad y_{\text{bar}_{k+100}} := Y3_k$$

$$A_{\text{bar}_{k+150}} := A4_k \quad x_{\text{bar}_{k+150}} := X4_k \quad y_{\text{bar}_{k+150}} := Y4_k$$

### Calculate Section Properties of Reinforcement

$$A_{\text{BAR}} := \sum_{j=1}^{200} A_{\text{bar}_j} \quad A_{\text{BAR}} = 31366 \text{ mm}^2$$

$$\rho := \frac{A_{\text{BAR}}}{A_C} \quad \rho = 0.0331$$

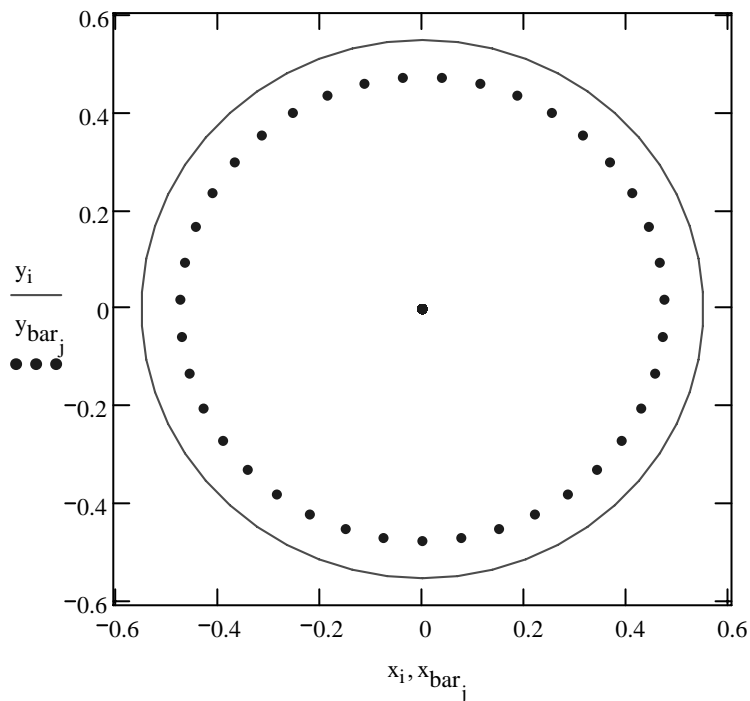
$$x_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot x_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad x_b = 0 \text{ m}$$

$$y_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot y_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad y_b = 0 \text{ m}$$

$$I_{x_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (x_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot x_b^2 \quad I_{x_b} = 0.00352 \text{ m}^4$$

$$I_{y_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (y_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot y_b^2 \quad I_{y_b} = 0.00352 \text{ m}^4$$

$j := 1 \dots 200$



**Calculate Composite Section Properties (before cracking)**

Effective area  $A_E := A_C \cdot [1 + \rho \cdot (\alpha - 1)] + A_{ST} \cdot \alpha$   $A_E = 1160150 \text{ mm}^2$

Effective centroid  $x_E := \frac{A_C \cdot [(1 - \rho) \cdot x_C + \rho \cdot x_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot x_{ST}}{A_E}$   $x_E = 0.000 \text{ m}$

$y_E := \frac{A_C \cdot [(1 - \rho) \cdot y_C + \rho \cdot y_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot y_{ST}}{A_E}$   $y_E = 0.000 \text{ m}$

Effective stiffness  $I_{EX} := I_{xC} + I_{xb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot x_C^2 + \rho \cdot x_b^2 \cdot \alpha] + (I_{xS} + A_{ST} \cdot x_{ST}^2) \cdot \alpha$   
 $I_{EX} = 0 \text{ m}^4$

$I_{EY} := I_{yC} + I_{yb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot y_C^2 + \rho \cdot y_b^2 \cdot \alpha] + (I_{yS} + A_{ST} \cdot y_{ST}^2) \cdot \alpha$   
 $I_{EY} = 0 \text{ m}^4$

Distance from extreme concrete fiber to centroid

$x_{F_{pos}} := \max(x - x_E)$   $x_{F_{neg}} := \min(x - x_E)$

$y_{F_{pos}} := \max(y - y_E)$   $y_{F_{neg}} := \min(y - y_E)$

Total depth of concrete section

$H_{CX} := x_{F_{pos}} - x_{F_{neg}}$   $H_{CX} = 1 \text{ m}$

$H_{CY} := y_{F_{pos}} - y_{F_{neg}}$   $H_{CY} = 1 \text{ m}$

Section modulus

$$Z_{Xpos} := \frac{I_{EX}}{xF_{pos}}$$

$$Z_{Xneg} := \frac{I_{EX}}{xF_{neg}}$$

$$Z_{Ypos} := \frac{I_{EY}}{yF_{pos}}$$

$$Z_{Yneg} := \frac{I_{EY}}{yF_{neg}}$$

Thickness of steel tube:

$$ts := y_1 - ys_1$$

$$ts = 0 \text{ mm}$$

**Establish Section Dimensions**

Positive case - determine coord of extreme concrete fiber

$$y_{Epos} := \max(y)$$

$$y_{Epos} = 550 \text{ mm}$$

Negative case - determine coord of extreme concrete fiber

$$y_{Eneg} := \min(y)$$

$$y_{Eneg} = -550 \text{ mm}$$

Offsets of rebar from extreme fiber

$$y_{Obar} := y_{Epos} - y_{bar}$$

Determine most extreme rebar (minimum offset)

$$y_{1bar} := \min(y_{Epos} - y_{bar})$$

$$y_{1bar} = 78 \text{ mm}$$

Determine most extreme rebar (maximum offset)

$$y_{nbar} := \max(y_{Epos} - y_{bar})$$

$$y_{nbar} = 1024 \text{ mm}$$

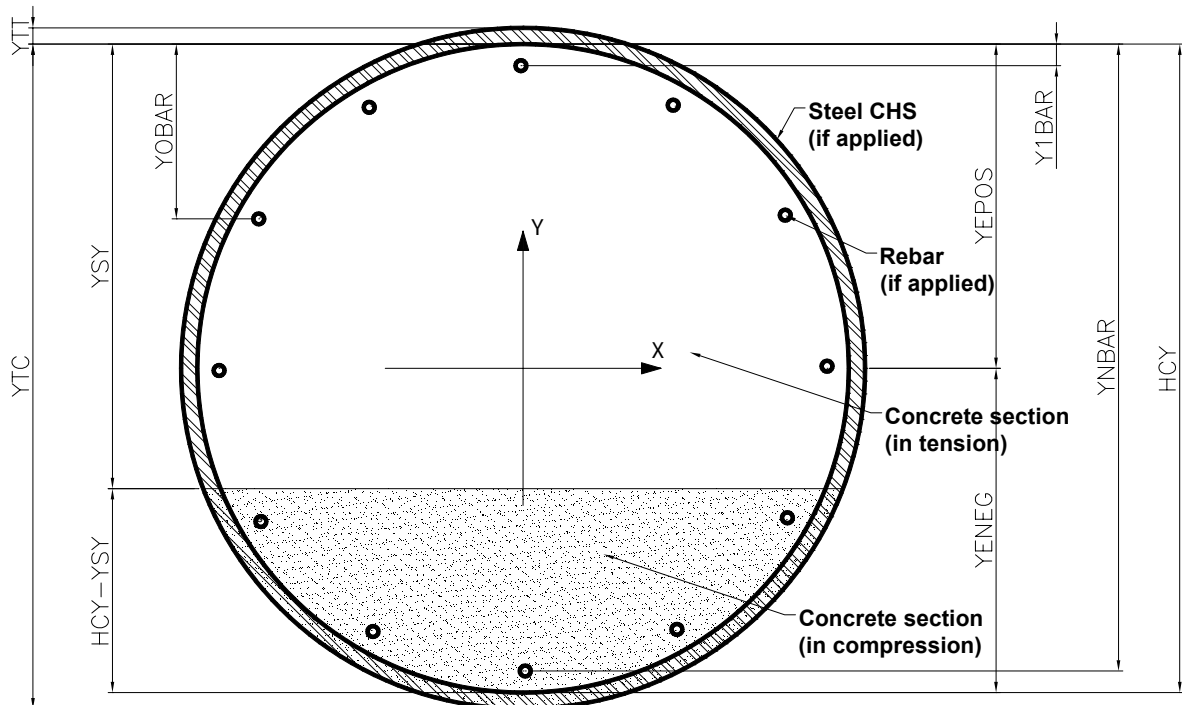
Offsets of extreme steel tube fiber from extreme concrete fiber

$$y_{tt} := ts$$

$$y_{tt} = 0 \text{ mm}$$

$$y_{tc} := H_{CY} + ts$$

$$y_{tc} = 1100 \text{ mm}$$



**ASSIGN NEUTRAL AXIS VALUES**

Number of sections to analysed                      ns := 500

q := 2 .. ns

Distance of neutral axis from extreme fiber in tension                       $y_{SY_q} := H_{CY} \cdot \frac{q}{ns + 1}$

**Calculate stresses and strains in reinforcement and concrete at extreme fibers**

Calculate strain at extreme compression fiber assuming max allowable stress in concrete:

Trial value of concrete strain

$$\epsilon_{cc} := \frac{\sigma_{cc}}{E_C} \cdot 2 \qquad \frac{\sigma_{cc}}{E_C} = 0.001165$$

Given

$$\sigma_{cc} = \epsilon_{cc} \cdot \left( 4700 \sqrt{\frac{f_c \cdot 2}{MPa}} - \frac{4700^2}{2.68} \cdot \epsilon_{cc} \right) \cdot MPa$$

$$\epsilon_{cc} := \text{Find}(\epsilon_{cc}) \qquad \epsilon_{cc} = 0.003321$$

$$\epsilon_{cc} := \begin{cases} \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \epsilon_{cc} & \text{otherwise} \end{cases} \qquad \epsilon_{cc} = 0.003321$$

Strain at other stresses taken to be linear:

$$\epsilon_{cc}(f_c, \sigma_{cd}) := \begin{cases} \frac{\sigma_{cd}}{\sigma_{tc}} \cdot \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \frac{\sigma_{cd}}{\sigma_{rc}} \cdot \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \frac{\sigma_{cd}}{\sigma_{cc}} \cdot \epsilon_{cc} & \text{otherwise} \end{cases}$$

Calculate strain in steel tube assuming max allowable stress in concrete:

$$\begin{aligned} \text{In compression} \quad \epsilon_{tcc_q} &:= \epsilon_{cc} \cdot \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \\ \text{In tension} \quad \epsilon_{tct_q} &:= \epsilon_{cc} \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \end{aligned}$$

Calculate strain in rebar assuming max allowable stress in concrete:

$$\text{In compression} \quad \varepsilon_{rcc_q} := \varepsilon_{cc} \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

$$\text{In tension} \quad \varepsilon_{rct_q} := \varepsilon_{cc} \cdot \frac{y_{1bar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

Calculate design max stress in compression taking account of other limits:

$$\sigma_{cd}(\varepsilon_{tcc}, q) := \begin{cases} \sigma_{cd} \leftarrow \sigma_{cc} & \text{if } f_c > 0 \\ \sigma_{cd} \leftarrow \sigma_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \sigma_{cd} \leftarrow \sigma_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{tc}}{\varepsilon_{tcc}} & \text{if } (\varepsilon_{tcc} > \varepsilon_{tc}) \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rc}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}} & \text{if } \left( \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}} > \varepsilon_{rc} \right) \cdot (A_{BAR} > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{ts}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}}} & \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} < \varepsilon_{ts} \right] \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rs}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}}} & \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}} < \varepsilon_{rs} \right] \cdot (A_{BAR} > 0) \\ \sigma_{cc} & \text{otherwise} \end{cases}$$

$$\sigma_{cd_q} := \sigma_{cd}(\varepsilon_{tcc_q}, q)$$

**CALCULATE FORCES AND MOMENTS AT EACH NEUTRAL AXIS LOCATION**

Calculate force in concrete:

$$F_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q}} \right] dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from concrete about column centroid:

$$M_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q}} \right] \cdot y dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in rebar assuming design max stress in concrete:

$$y_{SY_q} := \begin{cases} y_{nbar} \cdot \frac{q}{ns + 1} & \text{if } (f_c = 0) \cdot (A_{BAR} > 0) \\ y_{SY_q} & \text{otherwise} \end{cases}$$

$$\varepsilon_{S_{j,q}} := \begin{cases} \frac{y_{SY_q} - y_{Obar_j}}{y_{nbar} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{if } f_c = 0 \\ \frac{y_{SY_q} - y_{Obar_j}}{H_{CY} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{otherwise} \end{cases}$$

Calculate force in each rebar:

$$F_{S_{j,q}} := \begin{cases} \varepsilon_{S_{j,q}} \cdot E_S \cdot A_{bar_j} & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total force in reinforcement:



$$F_{R_q} := \sum_j F_{S_{j,q}}$$

Calculate moment from reinforcement about section centroid:

$$M_{R_q} := \begin{cases} \sum_j -(\varepsilon_{S_{j,q}} E_S A_{bar_j} y_{bar_j}) & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in steel tube at extreme tension fiber:

$$\varepsilon_{tds_q} := \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate strain in steel tube at extreme compression fiber:

$$\varepsilon_{tdc_q} := \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate tensile force in steel tube:

$$F_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS} := \begin{cases} F_{TS1} - F_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate compressive force in steel tube:

$$F_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TC2q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] dy$$

$$F_{TC} := \begin{cases} F_{TC1} - F_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from tensile force in steel tube:

$$M_{TS1q} := \int_{\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2} + y_{tt}} -2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS2q} := \int_{\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} -2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS} := \begin{cases} M_{TS1} - M_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from compressive force in steel tube:

$$M_{TC1q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC2q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC} := \begin{cases} M_{TC1} - M_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total axial response from section:

$$F_T := F_C + F_R + F_{TS} + F_{TC}$$

$$F_{TC} := F_C$$

Calculate total moment response from section:

$$M_T := M_C + M_R + M_{TS} + M_{TC}$$

$$M_{TC} := M_C$$

**CALCULATE MAXIMUM ALLOWABLE AXIAL FORCE IN SECTION**

Limiting strain in axial  
compression:

$$\varepsilon_{cL} := \begin{cases} \min(\varepsilon_{cc}, \varepsilon_{tc}) & \text{if } (A_{BAR} = 0) \cdot (ts \neq 0) \cdot (f_c \neq 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}) & \text{if } (ts = 0) \cdot (A_{BAR} \neq 0) \cdot (f_c \neq 0) \\ \varepsilon_{tc} & \text{if } (A_{BAR} = 0) \cdot (f_c = 0) \\ \varepsilon_{rc} & \text{if } (ts = 0) \cdot (f_c = 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}, \varepsilon_{tc}) & \text{otherwise} \end{cases} \quad \varepsilon_{cL} = 0.001950$$

Limiting concrete stress in axial compression

$$\sigma_{cL} := \begin{cases} \sigma_{cd2} & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases} \quad \sigma_{cL} = 18.93 \text{ MPa}$$

$$P_{MAX} := \sigma_{cL} \cdot A_C (1 - \rho) + \varepsilon_{cL} \cdot E_S (A_{BAR} + A_{ST})$$

$$P_{MAX} = 29580.5 \text{ kN} \quad F_{T_1} := P_{MAX} \quad M_{T_1} := 0 \cdot \text{kN} \cdot \text{m}$$

$$P_{MAXC} := \sigma_{cL} \cdot A_C \cdot (1 - \rho)$$

$$P_{MAXC} = 17347.9 \text{ kN} \quad F_{TC_1} := P_{MAXC} \quad M_{TC_1} := 0 \cdot \text{kN} \cdot \text{m}$$

**CALCULATE MINIMUM ALLOWABLE AXIAL FORCE IN SECTION**

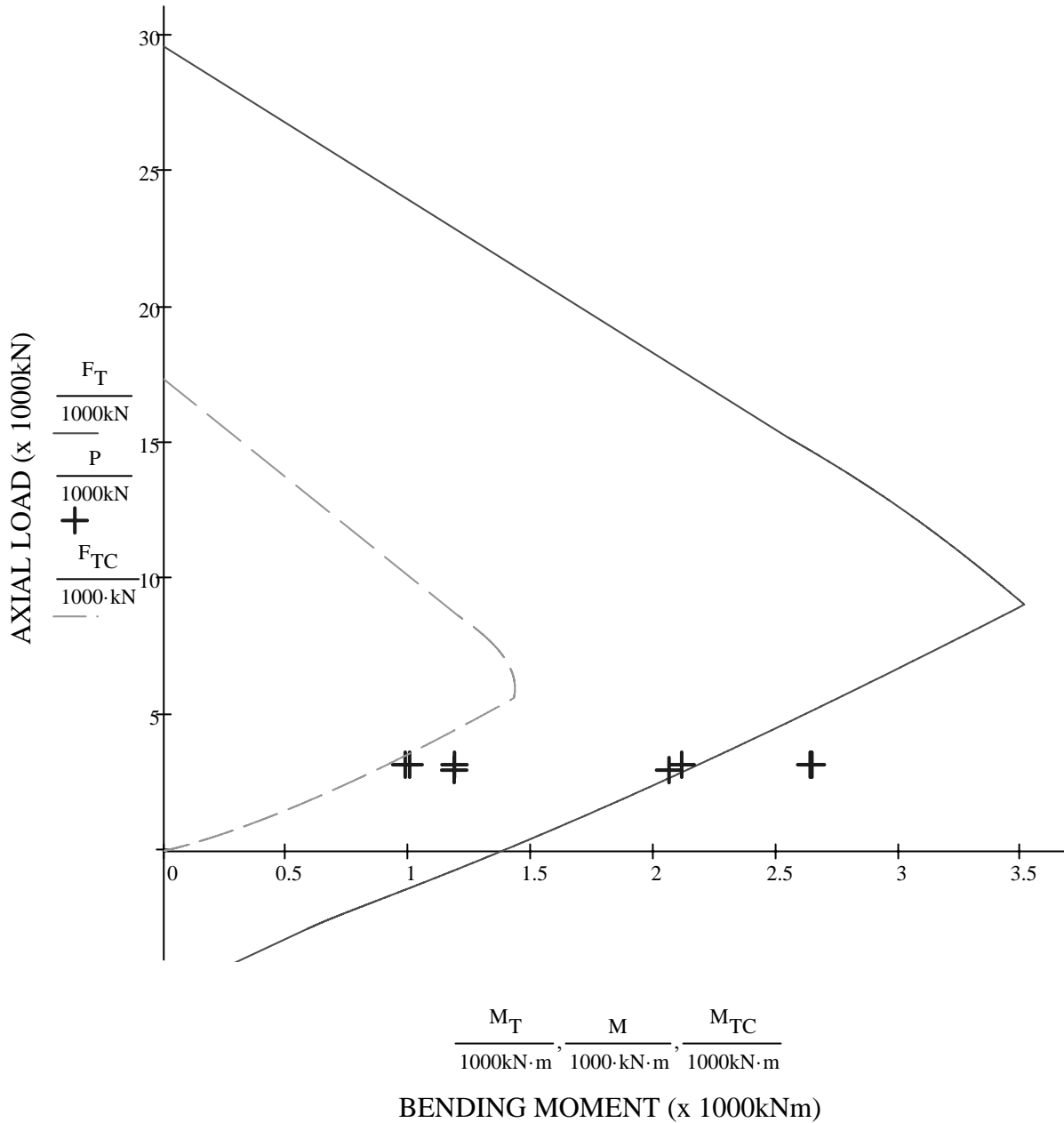
$$P_{MIN} := \begin{cases} \varepsilon_{rs} \cdot E_S (A_{BAR}) & \text{if } ts = 0 \\ \varepsilon_{ts} \cdot E_S (A_{ST}) & \text{if } A_{BAR} = 0 \\ \max(\varepsilon_{ts}, \varepsilon_{rs}) \cdot E_S (A_{BAR} + A_{ST}) & \text{otherwise} \end{cases}$$

$$P_{MIN} = -5332.2 \text{ kN} \quad F_{T_{ns+1}} := P_{MIN} \quad M_{T_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

$$\text{Limit} := \begin{cases} \min(P, F_T) \cdot 0.75 & \text{if } \min(P) > 0 \\ \min(P, F_T) \cdot 1.25 & \text{otherwise} \end{cases}$$

$$P_{MINC} := 0 \text{ kN} \quad M_{TC_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

Diameter of Column	D = 1100 mm	Characteristic strength of concrete	$f_c = 30 \text{ MPa}$
Percentage reinforcement	$\rho = 3.31 \%$	Yield Strength of Rebar	$f_y = 390 \text{ MPa}$
Thickness of CHS	$t_s = 0 \text{ mm}$	Yield Strength of CHS	$f_{ys} = 250 \text{ MPa}$



INTERACTION CURVE AT SERVICEABILITY LIMIT STATE

Equation of interaction line - upper region (between 1 and 2 calculation points)

$$m1 := \frac{M_{T_2} - M_{T_1}}{F_{T_2} - F_{T_1}} \quad c1 := F_{T_1}$$

Equation of interaction line - lower region (between ns and ns+1 calculation points)

$$m2 := \frac{M_{T_{ns}} - M_{T_{ns+1}}}{F_{T_{ns}} - F_{T_{ns+1}}} \quad c2 := F_{T_{ns+1}}$$

r := 1 .. 8

$$M_{SLS_r} := \begin{cases} 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r > F_{T_1} \\ 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r < F_{T_{ns+1}} \\ (P_r - c1) \cdot m1 & \text{if } (P_r > F_{T_2}) \cdot (P_r \leq F_{T_1}) \\ (P_r - c2) \cdot m2 & \text{if } (P_r \geq F_{T_{ns+1}}) \cdot (P_r < F_{T_{ns}}) \\ \text{otherwise} \\ \quad \begin{cases} j \leftarrow 1 \\ \text{while } F_{T_j} > P_r \\ \quad j \leftarrow j + 1 \\ M_{T_j} \end{cases} \end{cases}$$

$$\text{StressFactor}_r := \begin{cases} \text{"No Result"} & \text{if } M_{SLS_r} < 0.000000000000000001 \cdot \text{kN}\cdot\text{m} \\ \frac{M_r}{M_{SLS_r}} & \text{otherwise} \end{cases}$$

$$P = \begin{pmatrix} 3173 \\ 3173 \\ 3171 \\ 3171 \\ 2974 \\ 2974 \\ 3172 \\ 3172 \end{pmatrix} \text{ kN} \quad M = \begin{pmatrix} 986 \\ 2647 \\ 1004 \\ 2640 \\ 2063 \\ 1186 \\ 2115 \\ 1187 \end{pmatrix} \text{ kN}\cdot\text{m} \quad M_{SLS} = \begin{pmatrix} 2173.3 \\ 2173.3 \\ 2173.3 \\ 2173.3 \\ 2127.0 \\ 2127.0 \\ 2173.3 \\ 2173.3 \end{pmatrix} \text{ kN}\cdot\text{m} \quad \text{StressFactor} = \begin{pmatrix} 0.454 \\ 1.218 \\ 0.462 \\ 1.215 \\ 0.970 \\ 0.558 \\ 0.973 \\ 0.546 \end{pmatrix}$$

**RESULTS SUMMARY**  
**SERVICEABILITY LIMIT STATE ANALYSIS OF CIRCULAR BEAM COLUMN**

Diameter of Column		1100	mm				
Percentage of rebar		3.31	%				
Load Case Ref	Pier	Applied Service Axial Load kN	Applied Service Bending Moment kNm	Service Limit State Bending Moment kNm	Allowable Stress Factor	Applied Stress Factor	Serviceability Limit State Design Result
1	P71	3173	986	2173.3	140%	45%	OK
2	P71	3173	2647	2173.3	140%	122%	OK
3	P72	3171	1004	2173.3	140%	46%	OK
4	P72	3171	2640	2173.3	140%	121%	OK

**BASE**



## **Serviceability Check - Traffic Load Only**



**KATAHIRA & ENGINEERS  
INTERNATIONAL**

**Project:** Detailed Design Study of  
North Java Corridor Flyover Project

**Calculation:** Balaraja Flyover  
Serviceability Check - Traffic Load Only  
1100 mm Dia Circular RC Column - P7 Base Section

**Reference:** Project Specific Design Criteria

**Section Data**

MPa := 1000000·Pa

kN := 1000·N

Input Item		
Concrete Compressive Strength	fc	30 MPa
Structural Steel Yield Strength	fys	250 MPa
Rebar Yield Strength	fy	390 MPa
Diameter of reinforced concrete section	D	1100 mm
Thickness of CHS section	t	0 mm
Diameter of rebar - layer 1	dia1	32 mm
Diameter of rebar - layer 2	dia2	0 mm
Number bars - layer 1 (max 100)	n1	13
Number bars - layer 2 (max 100)	n2	0
Cover from face of section - layer 1	cov1	60 mm
Cover from face of section - layer 2	cov2	115 mm

**Load Data**

Ref	Pier	Load Case	P	M	Stress
			kN	kNm	Allowance
1	P71	Combination 1 - P + Traffic Load Only	3368.0	655.1	100%
2	P71	Combination 1 - P + Traffic Load Only	3368.0	263.9	100%
3	P72	Combination 1 - P + Traffic Load Only	3347.8	653.3	100%
4	P72	Combination 1 - P + Traffic Load Only	3347.8	248.9	100%

$$f_c := f_c \cdot \text{MPa} \quad f_{ys} := f_{ys} \cdot \text{MPa} \quad f_y := f_y \cdot \text{MPa} \quad D := D \cdot \text{mm} \quad ts := ts \cdot \text{mm}$$

$$\text{dia1} := \text{dia1} \cdot \text{mm} \quad \text{dia2} := \text{dia2} \cdot \text{mm} \quad \text{cov1} := \text{cov1} \cdot \text{mm} \quad \text{cov2} := \text{cov2} \cdot \text{mm}$$

$$P := P \cdot \text{kN} \quad M := M \cdot \text{kN} \cdot \text{m}$$

$$E_S := 200000 \cdot \text{MPa} \quad E_C := 4700 \sqrt{\frac{f_c}{\text{MPa}}} \cdot \text{MPa} \quad \text{Modular ratio} \quad \alpha := \begin{cases} \frac{E_S}{E_C} & \text{if } E_C > 0 \\ 1 & \text{otherwise} \end{cases} \quad \alpha = 7.77$$

$$E_C = 25743 \text{ MPa}$$

### Calculate Basic Allowable Stresses

Calculate rupture stress:

$$\sigma_{ct} := 0.5 \cdot \left( \frac{f_c}{\text{MPa}} \right)^{\frac{2}{3}} \cdot \text{MPa} \quad \sigma_{ct} = 4.8 \text{ MPa}$$

Calculate basic allowable stress of concrete

$$\sigma_{cc} := 1.0 \cdot f_c \quad \sigma_{cc} = 30.0 \text{ MPa}$$

Calculate basic allowable tensile stress of rebar

$$\sigma_{rs} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 170 \text{ MPa} \\ 170 \text{ MPa} & \text{otherwise} \end{cases} \quad \sigma_{rs} = 170 \text{ MPa}$$

Calculate basic allowable compressive stress of rebar

$$\sigma_{rc} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 110 \text{ MPa} \\ f_y & \text{otherwise} \end{cases} \quad \sigma_{rc} = 390 \text{ MPa}$$

Calculate basic allowable stress of structural steel

$$\sigma_{ts} := -0.6 f_{ys} \quad \sigma_{ts} = -150 \text{ MPa}$$

$$\sigma_{tc} := 1 f_{ys} \quad \sigma_{tc} = 250 \text{ MPa}$$

Limiting strain of rebar

$$\epsilon_{rs} := -\frac{\sigma_{rs}}{E_S} \quad \epsilon_{rs} = -0.000850$$

$$\epsilon_{rc} := \frac{\sigma_{rc}}{E_S} \quad \epsilon_{rc} = 0.001950$$

Limiting strain of structural steel

$$\epsilon_{ts} := \frac{\sigma_{ts}}{E_S} \quad \epsilon_{ts} = -0.000750$$

$$\epsilon_{tc} := \frac{\sigma_{tc}}{E_S} \quad \epsilon_{tc} = 0.001250$$

### Concrete Cross Section Data - generated

n := 50      Number of Points - 50 points maximum

i := 1 .. n + 1      Range from 1 to n+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	550
2	-69	-546	27	69	546
3	-137	-533	28	137	533
4	-202	-511	29	202	511
5	-265	-482	30	265	482
6	-323	-445	31	323	445
7	-377	-401	32	377	401
8	-424	-351	33	424	351
9	-464	-295	34	464	295
10	-498	-234	35	498	234
11	-523	-170	36	523	170
12	-540	-103	37	540	103
13	-549	-35	38	549	35
14	-549	35	39	549	-35
15	-540	103	40	540	-103
16	-523	170	41	523	-170
17	-498	234	42	498	-234
18	-464	295	43	464	-295
19	-424	351	44	424	-351
20	-377	401	45	377	-401
21	-323	445	46	323	-445
22	-265	482	47	265	-482
23	-202	511	48	202	-511
24	-137	533	49	137	-533
25	-69	546	50	69	-546

k := 1 .. 25      XS1 := XS1·mm    XS2 := XS2·mm      YS1 := YS1·mm    YS2 := YS2·mm

$x_k := XS1_k$        $y_k := YS1_k$        $x_{k+25} := XS2_k$        $y_{k+25} := YS2_k$        $x_{n+1} := XS1_1$        $y_{n+1} := YS1_1$

### Calculate Section Properties of Concrete Section

$$A_C := - \sum_{i=1}^n \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{2} \right] \quad A_C = 0.94783 \text{ m}^2$$

$$x_C := - \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{y_{i+1} - y_i}{8} \cdot \left[ (x_{i+1} + x_i)^2 + \frac{(x_{i+1} - x_i)^2}{3} \right] \right] \quad x_C = 0 \text{ m}$$

$$y_C := \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{x_{i+1} - x_i}{8} \cdot \left[ (y_{i+1} + y_i)^2 + \frac{(y_{i+1} - y_i)^2}{3} \right] \right] \quad y_C = 0 \text{ m}$$

$$I_x := \sum_{i=1}^n \left[ \left[ (x_{i+1} - x_i) \cdot \frac{y_{i+1} + y_i}{24} \right] \cdot \left[ (y_{i+1} + y_i)^2 + (y_{i+1} - y_i)^2 \right] \right] \quad I_x = 0.07149 \text{ m}^4$$

$$I_y := - \sum_{i=1}^n \left[ \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{24} \right] \cdot \left[ (x_{i+1} + x_i)^2 + (x_{i+1} - x_i)^2 \right] \right] \quad I_y = 0.07149 \text{ m}^4$$

$$I_{xC} := I_x - A_C \cdot x_C^2 \quad I_{xC} = 0.07149 \text{ m}^4$$

$$I_{yC} := I_y - A_C \cdot y_C^2 \quad I_{yC} = 0.07149 \text{ m}^4$$

### Steel Tube Cross Section Data - generated from input

ns := 50      Number of Points - 50 points maximum

ps := 1 .. ns + 1      Range from 1 to ns+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	-550
2	-142	-531	27	142	-531
3	-275	-476	28	275	-476
4	-389	-389	29	389	-389
5	-476	-275	30	476	-275
6	-531	-142	31	531	-142
7	-550	0	32	550	0
8	-531	142	33	531	142
9	-476	275	34	476	275
10	-389	389	35	389	389
11	-275	476	36	275	476
12	-142	531	37	142	531
13	0	550	38	0	550
14	142	531	39	-142	531
15	275	476	40	-275	476
16	389	389	41	-389	389
17	476	275	42	-476	275
18	531	142	43	-531	142
19	550	0	44	-550	0
20	531	-142	45	-531	-142
21	476	-275	46	-476	-275
22	389	-389	47	-389	-389
23	275	-476	48	-275	-476
24	142	-531	49	-142	-531
25	0	-550	50	0	-550

$$XSS1 := XSS1 \cdot \text{mm}$$

$$XSS2 := XSS2 \cdot \text{mm}$$

$$YSS1 := YSS1 \cdot \text{mm}$$

$$YSS2 := YSS2 \cdot \text{mm}$$

$$z := 1 .. 25$$

$$xs_z := XSS1_z$$

$$ys_z := YSS1_z$$

$$z := 26 .. 50$$

$$xs_z := XSS2_{z-25}$$

$$ys_z := YSS2_{z-25}$$

$$xs_{ns+1} := XSS1_1$$

$$ys_{ns+1} := YSS1_1$$

**Calculate Section Properties of Steel Tube Section**

$$A_{ST} := - \sum_{ps=1}^{ns} \left[ (y_{ps+1}^s - y_{ps}^s) \cdot \frac{x_{ps+1}^s + x_{ps}^s}{2} \right] \quad A_{ST} = 0 \text{ m}^2$$

$$x_{ST} := - \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{y_{ps+1}^s - y_{ps}^s}{8} \cdot \left[ (x_{ps+1}^s + x_{ps}^s)^2 + \frac{(x_{ps+1}^s - x_{ps}^s)^2}{3} \right] \right] \quad x_{ST} = 0.2 \text{ m}$$

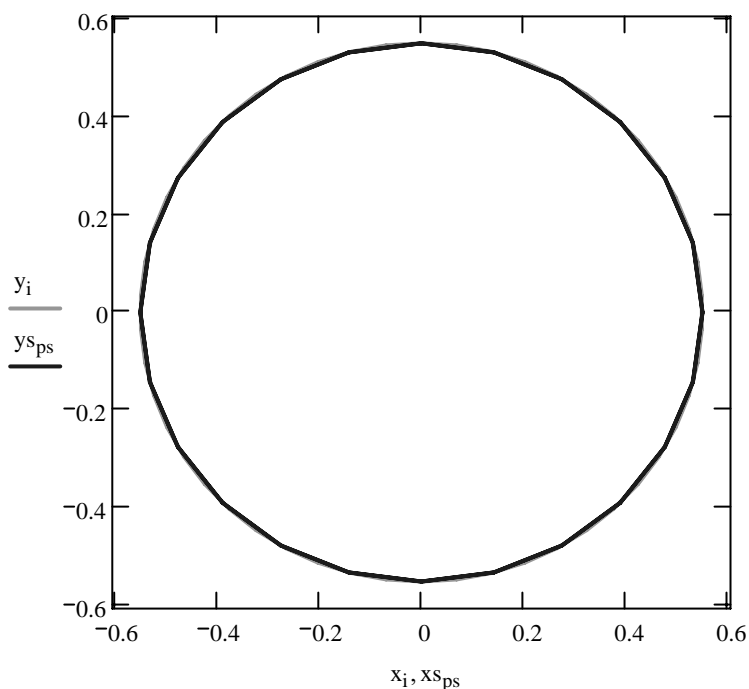
$$y_{ST} := \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{x_{ps+1}^s - x_{ps}^s}{8} \cdot \left[ (y_{ps+1}^s + y_{ps}^s)^2 + \frac{(y_{ps+1}^s - y_{ps}^s)^2}{3} \right] \right] \quad y_{ST} = -0.011 \text{ m}$$

$$I_{xS} := \sum_{ps=1}^{ns} \left[ \left[ (x_{ps+1}^s - x_{ps}^s) \cdot \frac{y_{ps+1}^s + y_{ps}^s}{24} \right] \cdot \left[ (y_{ps+1}^s + y_{ps}^s)^2 + (y_{ps+1}^s - y_{ps}^s)^2 \right] \right] \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := - \sum_{ps=1}^{ns} \left[ \left[ (y_{ps+1}^s - y_{ps}^s) \cdot \frac{x_{ps+1}^s + x_{ps}^s}{24} \right] \cdot \left[ (x_{ps+1}^s + x_{ps}^s)^2 + (x_{ps+1}^s - x_{ps}^s)^2 \right] \right] \quad I_{yS} = 0 \text{ m}^4$$

$$I_{xS} := I_{xS} - A_{ST} \cdot x_{ST}^2 \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := I_{yS} - A_{ST} \cdot y_{ST}^2 \quad I_{yS} = 0.00000 \text{ m}^4$$



**Rebar Data Layer 1 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	804	0	-474	51	0	0	0
2	804	-220	-420	52	0	0	0
3	804	-390	-269	53	0	0	0
4	804	-471	-57	54	0	0	0
5	804	-443	168	55	0	0	0
6	804	-314	355	56	0	0	0
7	804	-113	460	57	0	0	0
8	804	113	460	58	0	0	0
9	804	314	355	59	0	0	0
10	804	443	168	60	0	0	0
11	804	471	-57	61	0	0	0
12	804	390	-269	62	0	0	0
13	804	220	-420	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0



**Rebar Data Layer 2 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	0	0	0	51	0	0	0
2	0	0	0	52	0	0	0
3	0	0	0	53	0	0	0
4	0	0	0	54	0	0	0
5	0	0	0	55	0	0	0
6	0	0	0	56	0	0	0
7	0	0	0	57	0	0	0
8	0	0	0	58	0	0	0
9	0	0	0	59	0	0	0
10	0	0	0	60	0	0	0
11	0	0	0	61	0	0	0
12	0	0	0	62	0	0	0
13	0	0	0	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

$$A1 := A1 \cdot \text{mm}^2 \quad A2 := A2 \cdot \text{mm}^2 \quad A3 := A3 \cdot \text{mm}^2 \quad A4 := A4 \cdot \text{mm}^2$$

$$X1 := X1 \cdot \text{mm} \quad X2 := X2 \cdot \text{mm} \quad X3 := X3 \cdot \text{mm} \quad X4 := X4 \cdot \text{mm}$$

$$Y1 := Y1 \cdot \text{mm} \quad Y2 := Y2 \cdot \text{mm} \quad Y3 := Y3 \cdot \text{mm} \quad Y4 := Y4 \cdot \text{mm}$$

$$k := 1..50$$

$$A_{\text{bar}_k} := A1_k \quad x_{\text{bar}_k} := X1_k \quad y_{\text{bar}_k} := Y1_k$$

$$A_{\text{bar}_{k+50}} := A2_k \quad x_{\text{bar}_{k+50}} := X2_k \quad y_{\text{bar}_{k+50}} := Y2_k$$

$$A_{\text{bar}_{k+100}} := A3_k \quad x_{\text{bar}_{k+100}} := X3_k \quad y_{\text{bar}_{k+100}} := Y3_k$$

$$A_{\text{bar}_{k+150}} := A4_k \quad x_{\text{bar}_{k+150}} := X4_k \quad y_{\text{bar}_{k+150}} := Y4_k$$

### Calculate Section Properties of Reinforcement

$$A_{\text{BAR}} := \sum_{j=1}^{200} A_{\text{bar}_j} \quad A_{\text{BAR}} = 10455 \text{ mm}^2$$

$$\rho := \frac{A_{\text{BAR}}}{A_C} \quad \rho = 0.011$$

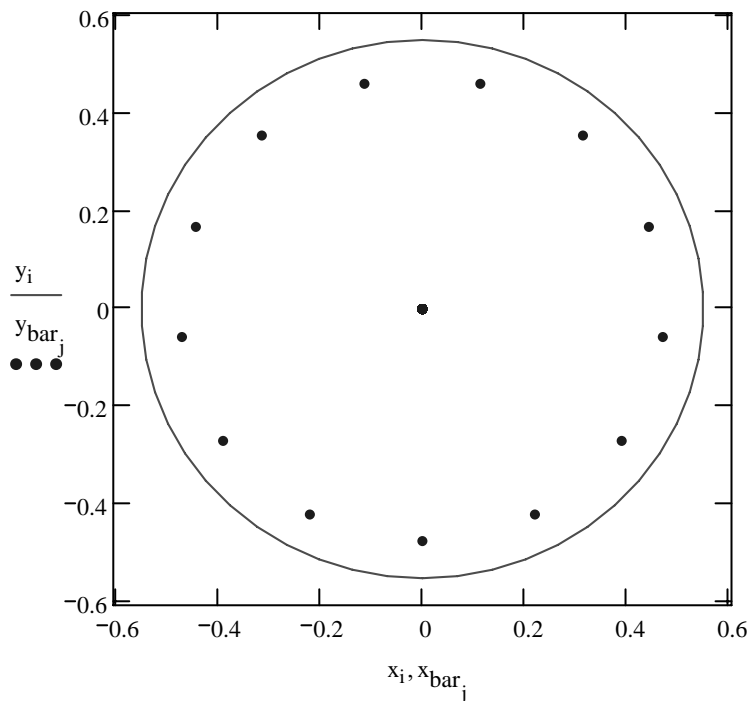
$$x_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot x_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad x_b = 0 \text{ m}$$

$$y_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot y_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad y_b = 0 \text{ m}$$

$$I_{x_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (x_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot x_b^2 \quad I_{x_b} = 0.00117 \text{ m}^4$$

$$I_{y_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (y_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot y_b^2 \quad I_{y_b} = 0.00117 \text{ m}^4$$

$j := 1 .. 200$



**Calculate Composite Section Properties (before cracking)**

Effective area  $A_E := A_C \cdot [1 + \rho \cdot (\alpha - 1)] + A_{ST} \cdot \alpha$   $A_E = 1018605 \text{ mm}^2$

Effective centroid  $x_E := \frac{A_C \cdot [(1 - \rho) \cdot x_C + \rho \cdot x_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot x_{ST}}{A_E}$   $x_E = 0.000 \text{ m}$

$y_E := \frac{A_C \cdot [(1 - \rho) \cdot y_C + \rho \cdot y_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot y_{ST}}{A_E}$   $y_E = 0.000 \text{ m}$

Effective stiffness  $I_{EX} := I_{xC} + I_{xb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot x_C^2 + \rho \cdot x_b^2 \cdot \alpha] + (I_{xS} + A_{ST} \cdot x_{ST}^2) \cdot \alpha$   
 $I_{EX} = 0 \text{ m}^4$

$I_{EY} := I_{yC} + I_{yb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot y_C^2 + \rho \cdot y_b^2 \cdot \alpha] + (I_{yS} + A_{ST} \cdot y_{ST}^2) \cdot \alpha$   
 $I_{EY} = 0 \text{ m}^4$

Distance from extreme concrete fiber to centroid

$x_{F_{pos}} := \max(x - x_E)$   $x_{F_{neg}} := \min(x - x_E)$

$y_{F_{pos}} := \max(y - y_E)$   $y_{F_{neg}} := \min(y - y_E)$

Total depth of concrete section

$H_{CX} := x_{F_{pos}} - x_{F_{neg}}$   $H_{CX} = 1 \text{ m}$

$H_{CY} := y_{F_{pos}} - y_{F_{neg}}$   $H_{CY} = 1 \text{ m}$

Section modulus

$$Z_{Xpos} := \frac{I_{EX}}{xF_{pos}}$$

$$Z_{Xneg} := \frac{I_{EX}}{xF_{neg}}$$

$$Z_{Ypos} := \frac{I_{EY}}{yF_{pos}}$$

$$Z_{Yneg} := \frac{I_{EY}}{yF_{neg}}$$

Thickness of steel tube:

$$ts := y_1 - ys_1$$

$$ts = 0 \text{ mm}$$

**Establish Section Dimensions**

Positive case - determine coord of extreme concrete fiber

$$y_{Epos} := \max(y)$$

$$y_{Epos} = 550 \text{ mm}$$

Negative case - determine coord of extreme concrete fiber

$$y_{Eneg} := \min(y)$$

$$y_{Eneg} = -550 \text{ mm}$$

Offsets of rebar from extreme fiber

$$y_{Obar} := y_{Epos} - y_{bar}$$

Determine most extreme rebar (minimum offset)

$$y_{1bar} := \min(y_{Epos} - y_{bar})$$

$$y_{1bar} = 90 \text{ mm}$$

Determine most extreme rebar (maximum offset)

$$y_{nbar} := \max(y_{Epos} - y_{bar})$$

$$y_{nbar} = 1024 \text{ mm}$$

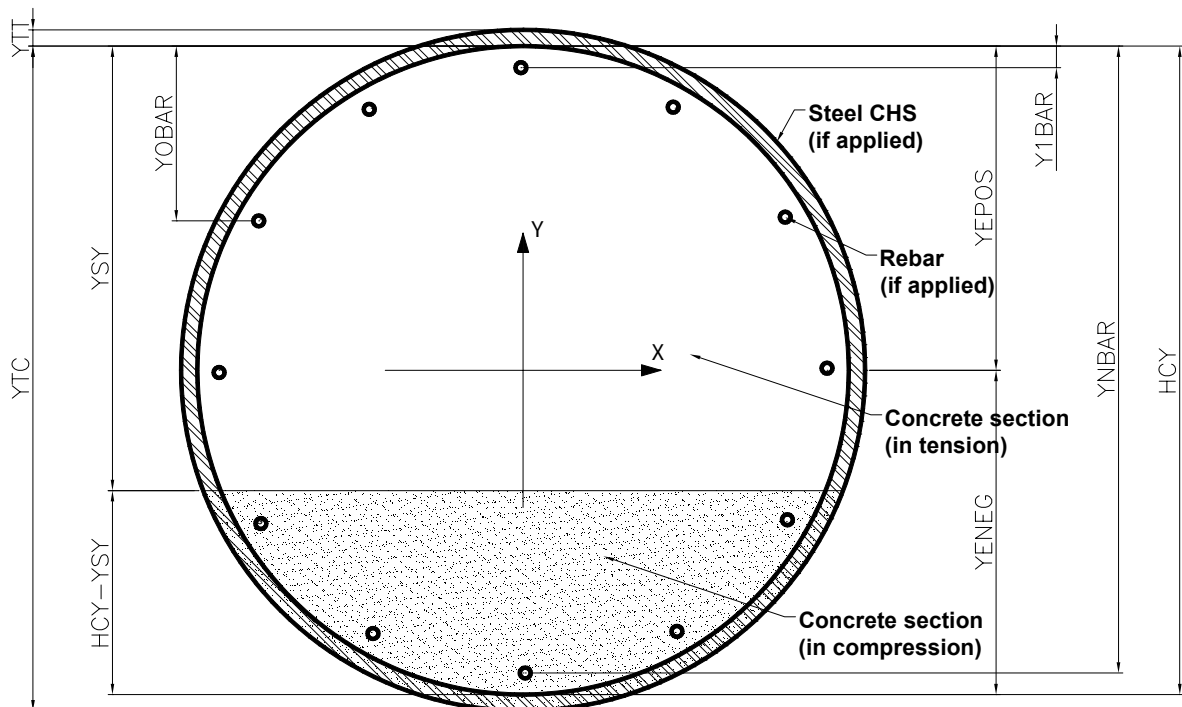
Offsets of extreme steel tube fiber from extreme concrete fiber

$$y_{tt} := ts$$

$$y_{tt} = 0 \text{ mm}$$

$$y_{tc} := H_{CY} + ts$$

$$y_{tc} = 1100 \text{ mm}$$



**ASSIGN NEUTRAL AXIS VALUES**

Number of sections to analysed                      ns := 500

q := 2 .. ns

Distance of neutral axis from extreme fiber in tension                       $y_{SY_q} := H_{CY} \cdot \frac{q}{ns + 1}$

**Calculate stresses and strains in reinforcement and concrete at extreme fibers**

Calculate strain at extreme compression fiber assuming max allowable stress in concrete:

Trial value of concrete strain

$$\epsilon_{cc} := \frac{\sigma_{cc}}{E_C} \cdot 2 \qquad \frac{\sigma_{cc}}{E_C} = 0.001165$$

Given

$$\sigma_{cc} = \epsilon_{cc} \cdot \left( 4700 \sqrt{\frac{f_c \cdot 2}{MPa}} - \frac{4700^2}{2.68} \cdot \epsilon_{cc} \right) \cdot MPa$$

$$\epsilon_{cc} := \text{Find}(\epsilon_{cc}) \qquad \epsilon_{cc} = 0.003321$$

$$\epsilon_{cc} := \begin{cases} \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \epsilon_{cc} & \text{otherwise} \end{cases} \qquad \epsilon_{cc} = 0.003321$$

Strain at other stresses taken to be linear:

$$\epsilon_{cc}(f_c, \sigma_{cd}) := \begin{cases} \frac{\sigma_{cd}}{\sigma_{tc}} \cdot \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \frac{\sigma_{cd}}{\sigma_{rc}} \cdot \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \frac{\sigma_{cd}}{\sigma_{cc}} \cdot \epsilon_{cc} & \text{otherwise} \end{cases}$$

Calculate strain in steel tube assuming max allowable stress in concrete:

In compression                       $\epsilon_{tcc_q} := \epsilon_{cc} \cdot \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}}$

In tension                               $\epsilon_{tct_q} := \epsilon_{cc} \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}}$

Calculate strain in rebar assuming max allowable stress in concrete:

$$\begin{array}{l} \text{In} \\ \text{compression} \end{array} \quad \varepsilon_{rcc_q} := \varepsilon_{cc} \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

$$\begin{array}{l} \text{In} \\ \text{tension} \end{array} \quad \varepsilon_{rct_q} := \varepsilon_{cc} \cdot \frac{y_{1bar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

Calculate design max stress in compression taking account of other limits:

$$\sigma_{cd}(\varepsilon_{tcc}, q) := \left\{ \begin{array}{l} \sigma_{cd} \leftarrow \sigma_{cc} \quad \text{if } f_c > 0 \\ \sigma_{cd} \leftarrow \sigma_{tc} \quad \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \sigma_{cd} \leftarrow \sigma_{rc} \quad \text{if } (f_c = 0) \cdot (ts = 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{tc}}{\varepsilon_{tcc}} \quad \text{if } (\varepsilon_{tcc} > \varepsilon_{tc}) \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rc}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}} \quad \text{if } \left( \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}} > \varepsilon_{rc} \right) \cdot (A_{BAR} > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{ts}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}}} \quad \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} < \varepsilon_{ts} \right] \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rs}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}}} \quad \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}} < \varepsilon_{rs} \right] \cdot (A_{BAR} > 0) \\ \sigma_{cc} \quad \text{otherwise} \end{array} \right.$$

$$\sigma_{cd_q} := \sigma_{cd}(\varepsilon_{tcc_q}, q)$$

**CALCULATE FORCES AND MOMENTS AT EACH NEUTRAL AXIS LOCATION**

Calculate force in concrete:

$$F_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from concrete about column centroid:

$$M_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] \cdot y dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in rebar assuming design max stress in concrete:

$$y_{SY_q} := \begin{cases} y_{nbar} \cdot \frac{q}{ns + 1} & \text{if } (f_c = 0) \cdot (A_{BAR} > 0) \\ y_{SY_q} & \text{otherwise} \end{cases}$$

$$\varepsilon_{S_{j,q}} := \begin{cases} \frac{y_{SY_q} - y_{Obar_j}}{y_{nbar} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{if } f_c = 0 \\ \frac{y_{SY_q} - y_{Obar_j}}{H_{CY} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{otherwise} \end{cases}$$

Calculate force in each rebar:

$$F_{S_{j,q}} := \begin{cases} \varepsilon_{S_{j,q}} \cdot E_S \cdot A_{bar_j} & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total force in reinforcement:

$$F_{R_q} := \sum_j F_{S_{j,q}}$$

Calculate moment from reinforcement about section centroid:

$$M_{R_q} := \begin{cases} \sum_j -(\varepsilon_{S_{j,q}} E_S A_{bar_j} y_{bar_j}) & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in steel tube at extreme tension fiber:

$$\varepsilon_{tds_q} := \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate strain in steel tube at extreme compression fiber:

$$\varepsilon_{tdc_q} := \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate tensile force in steel tube:

$$F_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS} := \begin{cases} F_{TS1} - F_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate compressive force in steel tube:

$$F_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$



$$F_{TC2_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TC} := \begin{cases} F_{TC1} - F_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from tensile force in steel tube:

$$M_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} -2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} -2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS} := \begin{cases} M_{TS1} - M_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from compressive force in steel tube:

$$M_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC2_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC} := \begin{cases} M_{TC1} - M_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total axial response from section:

$$F_T := F_C + F_R + F_{TS} + F_{TC}$$

$$F_{TC} := F_C$$

Calculate total moment response from section:

$$M_T := M_C + M_R + M_{TS} + M_{TC}$$

$$M_{TC} := M_C$$

**CALCULATE MAXIMUM ALLOWABLE AXIAL FORCE IN SECTION**

Limiting strain in axial  
compression:

$$\varepsilon_{cL} := \begin{cases} \min(\varepsilon_{cc}, \varepsilon_{tc}) & \text{if } (A_{BAR} = 0) \cdot (ts \neq 0) \cdot (f_c \neq 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}) & \text{if } (ts = 0) \cdot (A_{BAR} \neq 0) \cdot (f_c \neq 0) \\ \varepsilon_{tc} & \text{if } (A_{BAR} = 0) \cdot (f_c = 0) \\ \varepsilon_{rc} & \text{if } (ts = 0) \cdot (f_c = 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}, \varepsilon_{tc}) & \text{otherwise} \end{cases} \quad \varepsilon_{cL} = 0.001950$$

Limiting concrete stress in axial compression

$$\sigma_{cL} := \begin{cases} \sigma_{cd2} & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases} \quad \sigma_{cL} = 18.93 \text{ MPa}$$

$$P_{MAX} := \sigma_{cL} \cdot A_C (1 - \rho) + \varepsilon_{cL} \cdot E_S (A_{BAR} + A_{ST})$$

$$P_{MAX} = 21821.2 \text{ kN} \quad F_{T_1} := P_{MAX} \quad M_{T_1} := 0 \cdot \text{kN} \cdot \text{m}$$

$$P_{MAXC} := \sigma_{cL} \cdot A_C \cdot (1 - \rho)$$

$$P_{MAXC} = 17743.7 \text{ kN} \quad F_{TC_1} := P_{MAXC} \quad M_{TC_1} := 0 \cdot \text{kN} \cdot \text{m}$$

**CALCULATE MINIMUM ALLOWABLE AXIAL FORCE IN SECTION**

$$P_{MIN} := \begin{cases} \varepsilon_{rs} \cdot E_S (A_{BAR}) & \text{if } ts = 0 \\ \varepsilon_{ts} \cdot E_S (A_{ST}) & \text{if } A_{BAR} = 0 \\ \max(\varepsilon_{ts}, \varepsilon_{rs}) \cdot E_S (A_{BAR} + A_{ST}) & \text{otherwise} \end{cases}$$

$$P_{MIN} = -1777.4 \text{ kN} \quad F_{T_{ns+1}} := P_{MIN} \quad M_{T_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

$$\text{Limit} := \begin{cases} \min(P, F_T) \cdot 0.75 & \text{if } \min(P) > 0 \\ \min(P, F_T) \cdot 1.25 & \text{otherwise} \end{cases}$$

$$P_{MINC} := 0 \text{ kN} \quad M_{TC_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

Diameter of Column  $D = 1100 \text{ mm}$

Percentage reinforcement  $\rho = 1.10 \%$

Thickness of CHS  $t_s = 0 \text{ mm}$

Characteristic strength of concrete

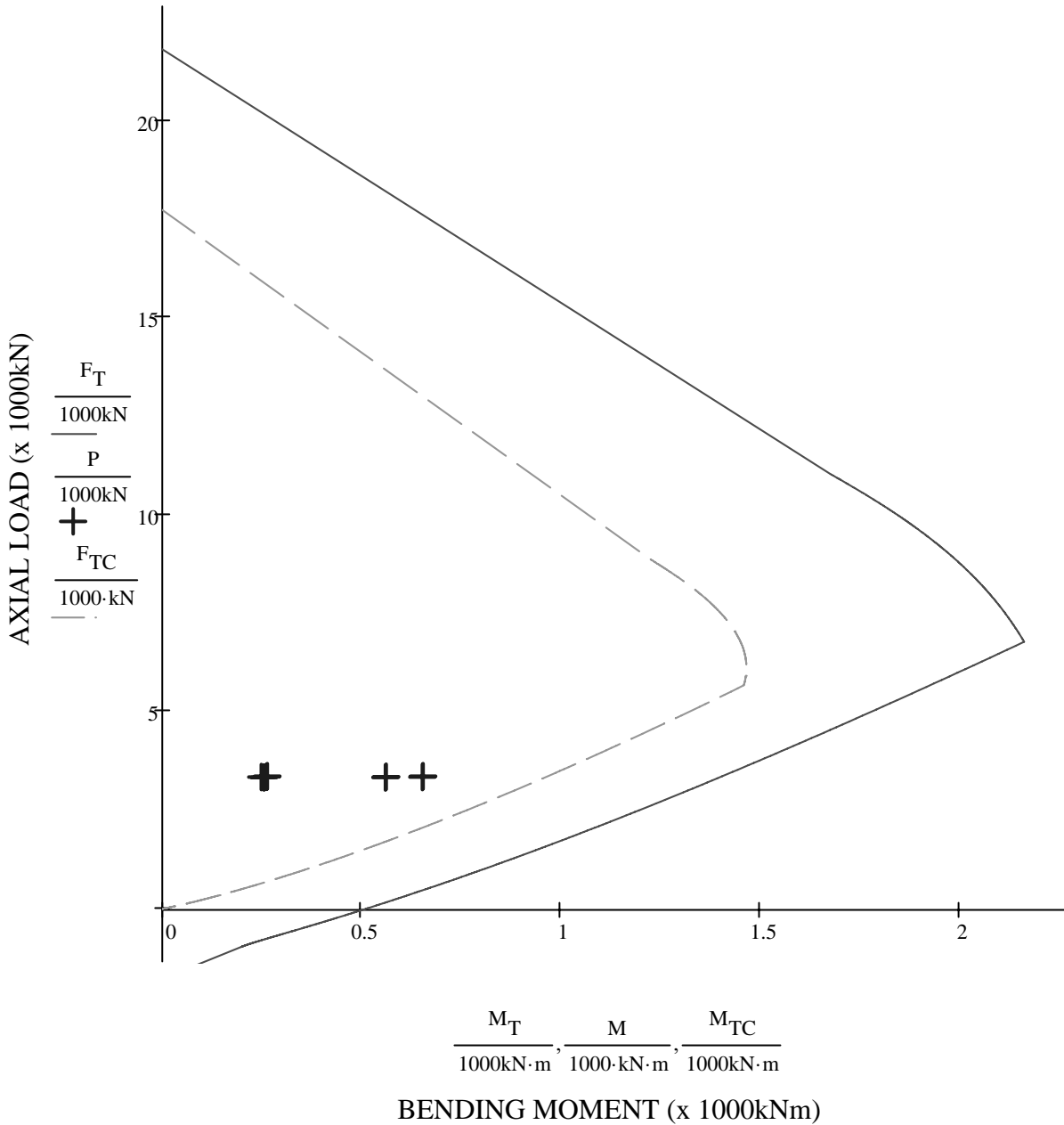
Yield Strength of Rebar

Yield Strength of CHS

$f_c = 30 \text{ MPa}$

$f_y = 390 \text{ MPa}$

$f_{ys} = 250 \text{ MPa}$



INTERACTION CURVE AT SERVICEABILITY LIMIT STATE

Equation of interaction line - upper region (between 1 and 2 calculation points)

$$m1 := \frac{M_{T_2} - M_{T_1}}{F_{T_2} - F_{T_1}} \quad c1 := F_{T_1}$$

Equation of interaction line - lower region (between ns and ns+1 calculation points)

$$m2 := \frac{M_{T_{ns}} - M_{T_{ns+1}}}{F_{T_{ns}} - F_{T_{ns+1}}} \quad c2 := F_{T_{ns+1}}$$

r := 1 .. 8

$$M_{SLS_r} := \begin{cases} 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r > F_{T_1} \\ 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r < F_{T_{ns+1}} \\ (P_r - c1) \cdot m1 & \text{if } (P_r > F_{T_2}) \cdot (P_r \leq F_{T_1}) \\ (P_r - c2) \cdot m2 & \text{if } (P_r \geq F_{T_{ns+1}}) \cdot (P_r < F_{T_{ns}}) \\ \text{otherwise} \\ \quad \begin{cases} j \leftarrow 1 \\ \text{while } F_{T_j} > P_r \\ \quad j \leftarrow j + 1 \\ M_{T_j} \end{cases} \end{cases}$$

$$\text{StressFactor}_r := \begin{cases} \text{"No Result"} & \text{if } M_{SLS_r} < 0.000000000000000001 \cdot \text{kN}\cdot\text{m} \\ \frac{M_r}{M_{SLS_r}} & \text{otherwise} \end{cases}$$

$$P = \begin{pmatrix} 3368 \\ 3368 \\ 3348 \\ 3348 \\ 3355 \\ 3355 \\ 3335 \\ 3335 \end{pmatrix} \text{ kN} \quad M = \begin{pmatrix} 655 \\ 264 \\ 653 \\ 249 \\ 562 \\ 263 \\ 561 \\ 256 \end{pmatrix} \text{ kN}\cdot\text{m} \quad M_{SLS} = \begin{pmatrix} 1406.2 \\ 1406.2 \\ 1393.5 \\ 1393.5 \\ 1393.5 \\ 1393.5 \\ 1393.5 \\ 1393.5 \end{pmatrix} \text{ kN}\cdot\text{m} \quad \text{StressFactor} = \begin{pmatrix} 0.466 \\ 0.188 \\ 0.469 \\ 0.179 \\ 0.403 \\ 0.188 \\ 0.402 \\ 0.183 \end{pmatrix}$$

**RESULTS SUMMARY**  
**SERVICEABILITY LIMIT STATE ANALYSIS OF CIRCULAR BEAM COLUMN**

Diameter of Column		1100	mm				
Percentage of rebar		1.10	%				
Load Case Ref	Pier	Applied Service Axial Load kN	Applied Service Bending Moment kNm	Service Limit State Bending Moment kNm	Allowable Stress Factor	Applied Stress Factor	Serviceability Limit State Design Result
1	P71	3368	655	1406.2	100%	47%	OK
2	P71	3368	264	1406.2	100%	19%	OK
3	P72	3348	653	1393.5	100%	47%	OK
4	P72	3348	249	1393.5	100%	18%	OK

## **Serviceability Check - Full Live Load**



**KATAHIRA & ENGINEERS  
INTERNATIONAL**

**Project:** Detailed Design Study of  
North Java Corridor Flyover Project

**Calculation:** Balaraja Flyover  
Serviceability Check - Full Live Load  
1100 mm Dia Circular RC Column - P7 Base Section

**Reference:** Project Specific Design Criteria

**Section Data**

MPa := 1000000·Pa

kN := 1000·N

Input Item		
Concrete Compressive Strength	fc	30 MPa
Structural Steel Yield Strength	fys	250 MPa
Rebar Yield Strength	fy	390 MPa
Diameter of reinforced concrete section	D	1100 mm
Thickness of CHS section	t	0 mm
Diameter of rebar - layer 1	dia1	32 mm
Diameter of rebar - layer 2	dia2	0 mm
Number bars - layer 1 (max 100)	n1	13
Number bars - layer 2 (max 100)	n2	0
Cover from face of section - layer 1	cov1	60 mm
Cover from face of section - layer 2	cov2	115 mm

**Load Data**

Ref	Pier	Load Case	P	M	Stress
			kN	kNm	Allowance
1	P71	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+CRSH	3359.1	1000.9	140%
2	P71	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+CRSH	3359.1	115.2	140%
3	P72	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+CRSH	3357.5	1003.6	140%
4	P72	Combination 1 - P + (TTD OR TTT) + (TTB or TTR) + Temp+CRSH	3357.5	130.6	140%



$$f_c := f_c \cdot \text{MPa} \quad f_{ys} := f_{ys} \cdot \text{MPa} \quad f_y := f_y \cdot \text{MPa} \quad D := D \cdot \text{mm} \quad ts := ts \cdot \text{mm}$$

$$\text{dia1} := \text{dia1} \cdot \text{mm} \quad \text{dia2} := \text{dia2} \cdot \text{mm} \quad \text{cov1} := \text{cov1} \cdot \text{mm} \quad \text{cov2} := \text{cov2} \cdot \text{mm}$$

$$P := P \cdot \text{kN} \quad M := M \cdot \text{kN} \cdot \text{m}$$

$$E_S := 200000 \cdot \text{MPa} \quad E_C := 4700 \sqrt{\frac{f_c}{\text{MPa}}} \cdot \text{MPa} \quad \text{Modular ratio} \quad \alpha := \begin{cases} \frac{E_S}{E_C} & \text{if } E_C > 0 \\ 1 & \text{otherwise} \end{cases} \quad \alpha = 7.77$$

$$E_C = 25743 \text{ MPa}$$

### Calculate Basic Allowable Stresses

Calculate rupture stress:

$$\sigma_{ct} := 0.5 \cdot \left( \frac{f_c}{\text{MPa}} \right)^{\frac{2}{3}} \cdot \text{MPa} \quad \sigma_{ct} = 4.8 \text{ MPa}$$

Calculate basic allowable stress of concrete

$$\sigma_{cc} := 1.0 \cdot f_c \quad \sigma_{cc} = 30.0 \text{ MPa}$$

Calculate basic allowable tensile stress of rebar

$$\sigma_{rs} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 170 \text{ MPa} \\ 170 \text{ MPa} & \text{otherwise} \end{cases} \quad \sigma_{rs} = 170 \text{ MPa}$$

Calculate basic allowable compressive stress of rebar

$$\sigma_{rc} := \begin{cases} 0.5 \cdot f_y & \text{if } 0.5 \cdot f_y \leq 110 \text{ MPa} \\ f_y & \text{otherwise} \end{cases} \quad \sigma_{rc} = 390 \text{ MPa}$$

Calculate basic allowable stress of structural steel

$$\sigma_{ts} := -0.6 f_{ys} \quad \sigma_{ts} = -150 \text{ MPa}$$

$$\sigma_{tc} := 1 f_{ys} \quad \sigma_{tc} = 250 \text{ MPa}$$

Limiting strain of rebar

$$\epsilon_{rs} := -\frac{\sigma_{rs}}{E_S} \quad \epsilon_{rs} = -0.000850$$

$$\epsilon_{rc} := \frac{\sigma_{rc}}{E_S} \quad \epsilon_{rc} = 0.001950$$

Limiting strain of structural steel

$$\epsilon_{ts} := \frac{\sigma_{ts}}{E_S} \quad \epsilon_{ts} = -0.000750$$

$$\epsilon_{tc} := \frac{\sigma_{tc}}{E_S} \quad \epsilon_{tc} = 0.001250$$

### Concrete Cross Section Data - generated

n := 50      Number of Points - 50 points maximum

i := 1 .. n + 1      Range from 1 to n+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	550
2	-69	-546	27	69	546
3	-137	-533	28	137	533
4	-202	-511	29	202	511
5	-265	-482	30	265	482
6	-323	-445	31	323	445
7	-377	-401	32	377	401
8	-424	-351	33	424	351
9	-464	-295	34	464	295
10	-498	-234	35	498	234
11	-523	-170	36	523	170
12	-540	-103	37	540	103
13	-549	-35	38	549	35
14	-549	35	39	549	-35
15	-540	103	40	540	-103
16	-523	170	41	523	-170
17	-498	234	42	498	-234
18	-464	295	43	464	-295
19	-424	351	44	424	-351
20	-377	401	45	377	-401
21	-323	445	46	323	-445
22	-265	482	47	265	-482
23	-202	511	48	202	-511
24	-137	533	49	137	-533
25	-69	546	50	69	-546

k := 1 .. 25      XS1 := XS1·mm    XS2 := XS2·mm    YS1 := YS1·mm    YS2 := YS2·mm

$x_k := XS1_k$        $y_k := YS1_k$        $x_{k+25} := XS2_k$        $y_{k+25} := YS2_k$        $x_{n+1} := XS1_1$        $y_{n+1} := YS1_1$

### Calculate Section Properties of Concrete Section

$$A_C := - \sum_{i=1}^n \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{2} \right] \quad A_C = 0.94783 \text{ m}^2$$

$$x_C := - \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{y_{i+1} - y_i}{8} \cdot \left[ (x_{i+1} + x_i)^2 + \frac{(x_{i+1} - x_i)^2}{3} \right] \right] \quad x_C = 0 \text{ m}$$

$$y_C := \frac{1}{A_C} \cdot \sum_{i=1}^n \left[ \frac{x_{i+1} - x_i}{8} \cdot \left[ (y_{i+1} + y_i)^2 + \frac{(y_{i+1} - y_i)^2}{3} \right] \right] \quad y_C = 0 \text{ m}$$

$$I_x := \sum_{i=1}^n \left[ \left[ (x_{i+1} - x_i) \cdot \frac{y_{i+1} + y_i}{24} \right] \cdot \left[ (y_{i+1} + y_i)^2 + (y_{i+1} - y_i)^2 \right] \right] \quad I_x = 0.07149 \text{ m}^4$$

$$I_y := - \sum_{i=1}^n \left[ \left[ (y_{i+1} - y_i) \cdot \frac{x_{i+1} + x_i}{24} \right] \cdot \left[ (x_{i+1} + x_i)^2 + (x_{i+1} - x_i)^2 \right] \right] \quad I_y = 0.07149 \text{ m}^4$$

$$I_{xC} := I_x - A_C \cdot x_C^2 \quad I_{xC} = 0.07149 \text{ m}^4$$

$$I_{yC} := I_y - A_C \cdot y_C^2 \quad I_{yC} = 0.07149 \text{ m}^4$$

### Steel Tube Cross Section Data - generated from input

ns := 50      Number of Points - 50 points maximum

ps := 1 .. ns + 1      Range from 1 to ns+1

Ref.	X mm	Y mm	Ref.	X mm	Y mm
1	0	-550	26	0	-550
2	-142	-531	27	142	-531
3	-275	-476	28	275	-476
4	-389	-389	29	389	-389
5	-476	-275	30	476	-275
6	-531	-142	31	531	-142
7	-550	0	32	550	0
8	-531	142	33	531	142
9	-476	275	34	476	275
10	-389	389	35	389	389
11	-275	476	36	275	476
12	-142	531	37	142	531
13	0	550	38	0	550
14	142	531	39	-142	531
15	275	476	40	-275	476
16	389	389	41	-389	389
17	476	275	42	-476	275
18	531	142	43	-531	142
19	550	0	44	-550	0
20	531	-142	45	-531	-142
21	476	-275	46	-476	-275
22	389	-389	47	-389	-389
23	275	-476	48	-275	-476
24	142	-531	49	-142	-531
25	0	-550	50	0	-550

$$XSS1 := XSS1 \cdot \text{mm}$$

$$XSS2 := XSS2 \cdot \text{mm}$$

$$YSS1 := YSS1 \cdot \text{mm}$$

$$YSS2 := YSS2 \cdot \text{mm}$$

$$z := 1 .. 25$$

$$xs_z := XSS1_z$$

$$ys_z := YSS1_z$$

$$z := 26 .. 50$$

$$xs_z := XSS2_{z-25}$$

$$ys_z := YSS2_{z-25}$$

$$xs_{ns+1} := XSS1_1$$

$$ys_{ns+1} := YSS1_1$$

**Calculate Section Properties of Steel Tube Section**

$$A_{ST} := - \sum_{ps=1}^{ns} \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{2} \right] \quad A_{ST} = 0 \text{ m}^2$$

$$x_{ST} := - \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{y_{ps+1}^{s} - y_{ps}^{s}}{8} \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + \frac{(x_{ps+1}^{s} - x_{ps}^{s})^2}{3} \right] \right] \quad x_{ST} = 0.2 \text{ m}$$

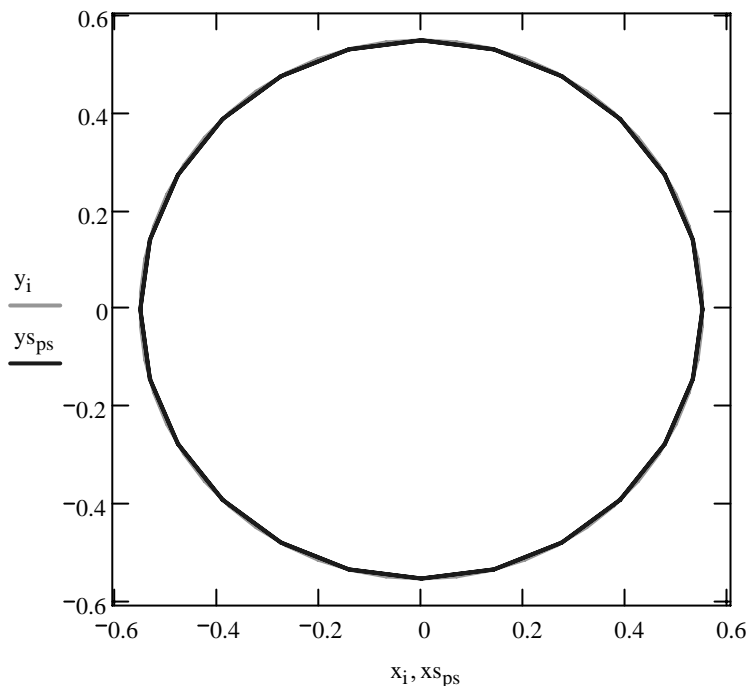
$$y_{ST} := \frac{1}{A_{ST}} \cdot \sum_{ps=1}^{ns} \left[ \frac{x_{ps+1}^{s} - x_{ps}^{s}}{8} \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + \frac{(y_{ps+1}^{s} - y_{ps}^{s})^2}{3} \right] \right] \quad y_{ST} = -0.011 \text{ m}$$

$$I_{xS} := \sum_{ps=1}^{ns} \left[ \left[ (x_{ps+1}^{s} - x_{ps}^{s}) \cdot \frac{y_{ps+1}^{s} + y_{ps}^{s}}{24} \right] \cdot \left[ (y_{ps+1}^{s} + y_{ps}^{s})^2 + (y_{ps+1}^{s} - y_{ps}^{s})^2 \right] \right] \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := - \sum_{ps=1}^{ns} \left[ \left[ (y_{ps+1}^{s} - y_{ps}^{s}) \cdot \frac{x_{ps+1}^{s} + x_{ps}^{s}}{24} \right] \cdot \left[ (x_{ps+1}^{s} + x_{ps}^{s})^2 + (x_{ps+1}^{s} - x_{ps}^{s})^2 \right] \right] \quad I_{yS} = 0 \text{ m}^4$$

$$I_{xS} := I_{xS} - A_{ST} \cdot x_{ST}^2 \quad I_{xS} = 0 \text{ m}^4$$

$$I_{yS} := I_{yS} - A_{ST} \cdot y_{ST}^2 \quad I_{yS} = 0.00000 \text{ m}^4$$



**Rebar Data Layer 1 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	804	0	-474	51	0	0	0
2	804	-220	-420	52	0	0	0
3	804	-390	-269	53	0	0	0
4	804	-471	-57	54	0	0	0
5	804	-443	168	55	0	0	0
6	804	-314	355	56	0	0	0
7	804	-113	460	57	0	0	0
8	804	113	460	58	0	0	0
9	804	314	355	59	0	0	0
10	804	443	168	60	0	0	0
11	804	471	-57	61	0	0	0
12	804	390	-269	62	0	0	0
13	804	220	-420	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

**Rebar Data Layer 2 - generated from input**

Ref	Area mm <sup>2</sup>	X mm	Y mm	Ref	Area mm <sup>2</sup>	X mm	Y mm
1	0	0	0	51	0	0	0
2	0	0	0	52	0	0	0
3	0	0	0	53	0	0	0
4	0	0	0	54	0	0	0
5	0	0	0	55	0	0	0
6	0	0	0	56	0	0	0
7	0	0	0	57	0	0	0
8	0	0	0	58	0	0	0
9	0	0	0	59	0	0	0
10	0	0	0	60	0	0	0
11	0	0	0	61	0	0	0
12	0	0	0	62	0	0	0
13	0	0	0	63	0	0	0
14	0	0	0	64	0	0	0
15	0	0	0	65	0	0	0
16	0	0	0	66	0	0	0
17	0	0	0	67	0	0	0
18	0	0	0	68	0	0	0
19	0	0	0	69	0	0	0
20	0	0	0	70	0	0	0
21	0	0	0	71	0	0	0
22	0	0	0	72	0	0	0
23	0	0	0	73	0	0	0
24	0	0	0	74	0	0	0
25	0	0	0	75	0	0	0
26	0	0	0	76	0	0	0
27	0	0	0	77	0	0	0
28	0	0	0	78	0	0	0
29	0	0	0	79	0	0	0
30	0	0	0	80	0	0	0
31	0	0	0	81	0	0	0
32	0	0	0	82	0	0	0
33	0	0	0	83	0	0	0
34	0	0	0	84	0	0	0
35	0	0	0	85	0	0	0
36	0	0	0	86	0	0	0
37	0	0	0	87	0	0	0
38	0	0	0	88	0	0	0
39	0	0	0	89	0	0	0
40	0	0	0	90	0	0	0
41	0	0	0	91	0	0	0
42	0	0	0	92	0	0	0
43	0	0	0	93	0	0	0
44	0	0	0	94	0	0	0
45	0	0	0	95	0	0	0
46	0	0	0	96	0	0	0
47	0	0	0	97	0	0	0
48	0	0	0	98	0	0	0
49	0	0	0	99	0	0	0
50	0	0	0	100	0	0	0

$$A1 := A1 \cdot \text{mm}^2 \quad A2 := A2 \cdot \text{mm}^2 \quad A3 := A3 \cdot \text{mm}^2 \quad A4 := A4 \cdot \text{mm}^2$$

$$X1 := X1 \cdot \text{mm} \quad X2 := X2 \cdot \text{mm} \quad X3 := X3 \cdot \text{mm} \quad X4 := X4 \cdot \text{mm}$$

$$Y1 := Y1 \cdot \text{mm} \quad Y2 := Y2 \cdot \text{mm} \quad Y3 := Y3 \cdot \text{mm} \quad Y4 := Y4 \cdot \text{mm}$$

$$k := 1..50$$

$$A_{\text{bar}_k} := A1_k \quad x_{\text{bar}_k} := X1_k \quad y_{\text{bar}_k} := Y1_k$$

$$A_{\text{bar}_{k+50}} := A2_k \quad x_{\text{bar}_{k+50}} := X2_k \quad y_{\text{bar}_{k+50}} := Y2_k$$

$$A_{\text{bar}_{k+100}} := A3_k \quad x_{\text{bar}_{k+100}} := X3_k \quad y_{\text{bar}_{k+100}} := Y3_k$$

$$A_{\text{bar}_{k+150}} := A4_k \quad x_{\text{bar}_{k+150}} := X4_k \quad y_{\text{bar}_{k+150}} := Y4_k$$

### Calculate Section Properties of Reinforcement

$$A_{\text{BAR}} := \sum_{j=1}^{200} A_{\text{bar}_j} \quad A_{\text{BAR}} = 10455 \text{ mm}^2$$

$$\rho := \frac{A_{\text{BAR}}}{A_C} \quad \rho = 0.011$$

$$x_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot x_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad x_b = 0 \text{ m}$$

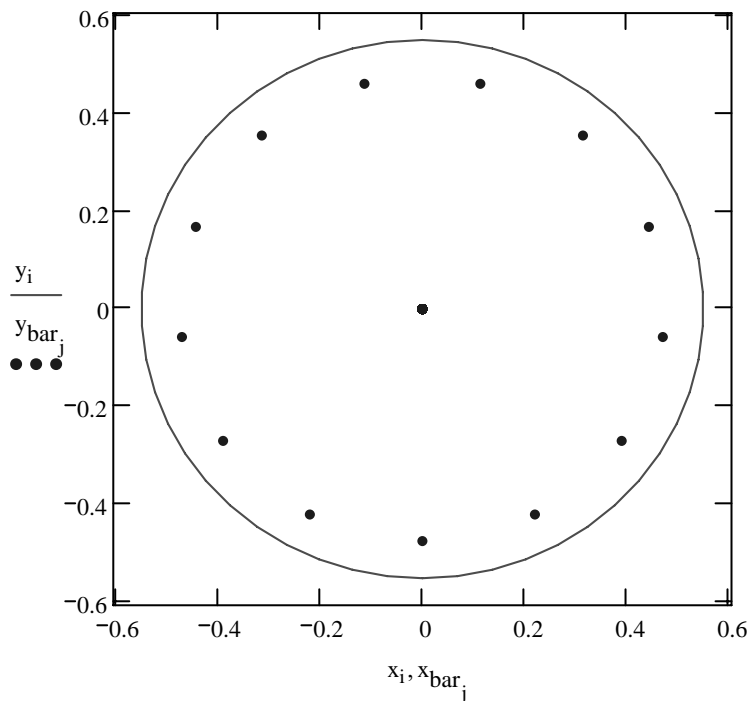
$$y_b := \begin{cases} \left[ \sum_{j=1}^{200} (A_{\text{bar}_j} \cdot y_{\text{bar}_j}) \right] \cdot \frac{1}{A_{\text{BAR}}} & \text{if } A_{\text{BAR}} > 0 \\ 0\text{m} & \text{otherwise} \end{cases} \quad y_b = 0 \text{ m}$$

$$I_{x_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (x_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot x_b^2 \quad I_{x_b} = 0.00117 \text{ m}^4$$

$$I_{y_b} := \sum_{j=1}^{200} \left[ A_{\text{bar}_j} \cdot (y_{\text{bar}_j})^2 \right] + A_{\text{BAR}} \cdot y_b^2 \quad I_{y_b} = 0.00117 \text{ m}^4$$



$j := 1 .. 200$



**Calculate Composite Section Properties (before cracking)**

Effective area  $A_E := A_C \cdot [1 + \rho \cdot (\alpha - 1)] + A_{ST} \cdot \alpha$   $A_E = 1018605 \text{ mm}^2$

Effective centroid  $x_E := \frac{A_C \cdot [(1 - \rho) \cdot x_C + \rho \cdot x_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot x_{ST}}{A_E}$   $x_E = 0.000 \text{ m}$

$y_E := \frac{A_C \cdot [(1 - \rho) \cdot y_C + \rho \cdot y_b \cdot \alpha] + A_{ST} \cdot \alpha \cdot y_{ST}}{A_E}$   $y_E = 0.000 \text{ m}$

Effective stiffness  $I_{EX} := I_{xC} + I_{xb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot x_C^2 + \rho \cdot x_b^2 \cdot \alpha] + (I_{xS} + A_{ST} \cdot x_{ST}^2) \cdot \alpha$   
 $I_{EX} = 0 \text{ m}^4$

$I_{EY} := I_{yC} + I_{yb} \cdot (\alpha - 1) + A_C \cdot [(1 - \rho) \cdot y_C^2 + \rho \cdot y_b^2 \cdot \alpha] + (I_{yS} + A_{ST} \cdot y_{ST}^2) \cdot \alpha$   
 $I_{EY} = 0 \text{ m}^4$

Distance from extreme concrete fiber to centroid

$x_{F_{pos}} := \max(x - x_E)$   $x_{F_{neg}} := \min(x - x_E)$

$y_{F_{pos}} := \max(y - y_E)$   $y_{F_{neg}} := \min(y - y_E)$

Total depth of concrete section

$H_{CX} := x_{F_{pos}} - x_{F_{neg}}$   $H_{CX} = 1 \text{ m}$

$H_{CY} := y_{F_{pos}} - y_{F_{neg}}$   $H_{CY} = 1 \text{ m}$

Section modulus

$$Z_{Xpos} := \frac{I_{EX}}{xF_{pos}}$$

$$Z_{Xneg} := \frac{I_{EX}}{xF_{neg}}$$

$$Z_{Ypos} := \frac{I_{EY}}{yF_{pos}}$$

$$Z_{Yneg} := \frac{I_{EY}}{yF_{neg}}$$

Thickness of steel tube:

$$ts := y_1 - ys_1$$

$$ts = 0 \text{ mm}$$

**Establish Section Dimensions**

Positive case - determine coord of extreme concrete fiber

$$y_{Epos} := \max(y)$$

$$y_{Epos} = 550 \text{ mm}$$

Negative case - determine coord of extreme concrete fiber

$$y_{Eneg} := \min(y)$$

$$y_{Eneg} = -550 \text{ mm}$$

Offsets of rebar from extreme fiber

$$y_{Obar} := y_{Epos} - y_{bar}$$

Determine most extreme rebar (minimum offset)

$$y_{1bar} := \min(y_{Epos} - y_{bar})$$

$$y_{1bar} = 90 \text{ mm}$$

Determine most extreme rebar (maximum offset)

$$y_{nbar} := \max(y_{Epos} - y_{bar})$$

$$y_{nbar} = 1024 \text{ mm}$$

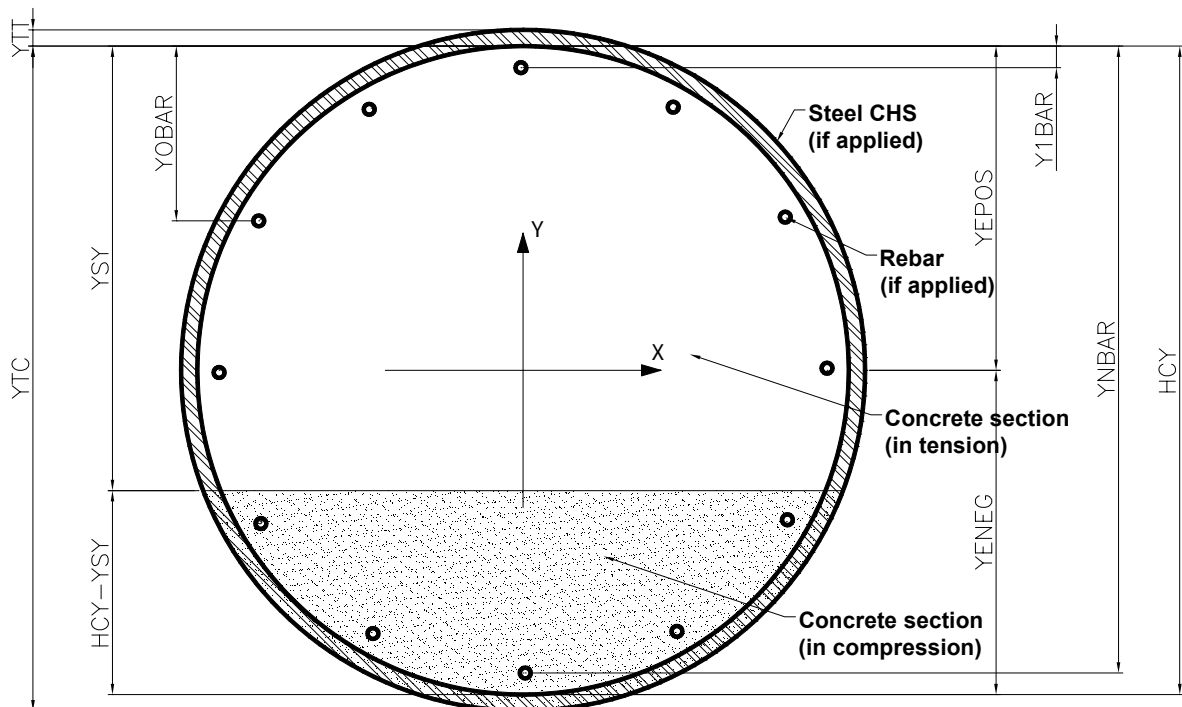
Offsets of extreme steel tube fiber from extreme concrete fiber

$$y_{tt} := ts$$

$$y_{tt} = 0 \text{ mm}$$

$$y_{tc} := H_{CY} + ts$$

$$y_{tc} = 1100 \text{ mm}$$



**ASSIGN NEUTRAL AXIS VALUES**

Number of sections to analysed                      ns := 500

q := 2 .. ns

Distance of neutral axis from extreme fiber in tension                       $y_{SY_q} := H_{CY} \cdot \frac{q}{ns + 1}$

**Calculate stresses and strains in reinforcement and concrete at extreme fibers**

Calculate strain at extreme compression fiber assuming max allowable stress in concrete:

Trial value of concrete strain

$$\epsilon_{cc} := \frac{\sigma_{cc}}{E_C} \cdot 2 \qquad \frac{\sigma_{cc}}{E_C} = 0.001165$$

Given

$$\sigma_{cc} = \epsilon_{cc} \cdot \left( 4700 \sqrt{\frac{f_c \cdot 2}{MPa}} - \frac{4700^2}{2.68} \cdot \epsilon_{cc} \right) \cdot MPa$$

$$\epsilon_{cc} := \text{Find}(\epsilon_{cc}) \qquad \epsilon_{cc} = 0.003321$$

$$\epsilon_{cc} := \begin{cases} \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \epsilon_{cc} & \text{otherwise} \end{cases} \qquad \epsilon_{cc} = 0.003321$$

Strain at other stresses taken to be linear:

$$\epsilon_{cc}(f_c, \sigma_{cd}) := \begin{cases} \frac{\sigma_{cd}}{\sigma_{tc}} \cdot \epsilon_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \frac{\sigma_{cd}}{\sigma_{rc}} \cdot \epsilon_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \frac{\sigma_{cd}}{\sigma_{cc}} \cdot \epsilon_{cc} & \text{otherwise} \end{cases}$$

Calculate strain in steel tube assuming max allowable stress in concrete:

$$\begin{aligned} \text{In compression} \quad \epsilon_{tcc_q} &:= \epsilon_{cc} \cdot \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \\ \text{In tension} \quad \epsilon_{tct_q} &:= \epsilon_{cc} \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \end{aligned}$$

Calculate strain in rebar assuming max allowable stress in concrete:

$$\text{In compression} \quad \varepsilon_{rcc_q} := \varepsilon_{cc} \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

$$\text{In tension} \quad \varepsilon_{rct_q} := \varepsilon_{cc} \cdot \frac{y_{1bar} - y_{SY_q}}{H_{CY} - y_{SY_q}}$$

Calculate design max stress in compression taking account of other limits:

$$\sigma_{cd}(\varepsilon_{tcc}, q) := \begin{cases} \sigma_{cd} \leftarrow \sigma_{cc} & \text{if } f_c > 0 \\ \sigma_{cd} \leftarrow \sigma_{tc} & \text{if } (f_c = 0) \cdot (A_{BAR} = 0) \\ \sigma_{cd} \leftarrow \sigma_{rc} & \text{if } (f_c = 0) \cdot (ts = 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{tc}}{\varepsilon_{tcc}} & \text{if } (\varepsilon_{tcc} > \varepsilon_{tc}) \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rc}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}}} & \text{if } \left( \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{y_{nbar} - y_{SY_q}}{H_{CY} - y_{SY_q}} > \varepsilon_{rc} \right) \cdot (A_{BAR} > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{ts}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}}} & \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} < \varepsilon_{ts} \right] \cdot (ts > 0) \\ \sigma_{cd} \leftarrow \sigma_{cd} \cdot \frac{\varepsilon_{rs}}{\varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}}} & \text{if } \left[ \varepsilon_{cc}(f_c, \sigma_{cd}) \cdot \frac{-(y_{SY_q} - y_{1bar})}{H_{CY} - y_{SY_q}} < \varepsilon_{rs} \right] \cdot (A_{BAR} > 0) \\ \sigma_{cc} & \text{otherwise} \end{cases}$$

$$\sigma_{cd_q} := \sigma_{cd}(\varepsilon_{tcc_q}, q)$$

**CALCULATE FORCES AND MOMENTS AT EACH NEUTRAL AXIS LOCATION**

Calculate force in concrete:

$$F_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from concrete about column centroid:

$$M_{C_q} := \begin{cases} \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot (1 - \rho) \cdot \left[ \frac{\sigma_{cd_q} \cdot \left[ y + \left(\frac{H_{CY}}{2} - y_{SY_q}\right) \right]}{H_{CY} - y_{SY_q}} \right] \cdot y dy & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in rebar assuming design max stress in concrete:

$$y_{SY_q} := \begin{cases} y_{nbar} \cdot \frac{q}{ns + 1} & \text{if } (f_c = 0) \cdot (A_{BAR} > 0) \\ y_{SY_q} & \text{otherwise} \end{cases}$$

$$\varepsilon_{S_{j,q}} := \begin{cases} \frac{y_{SY_q} - y_{Obar_j}}{y_{nbar} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{if } f_c = 0 \\ \frac{y_{SY_q} - y_{Obar_j}}{H_{CY} - y_{SY_q}} \cdot \varepsilon_{cc}(f_c, \sigma_{cd_q}) & \text{otherwise} \end{cases}$$

Calculate force in each rebar:

$$F_{S_{j,q}} := \begin{cases} \varepsilon_{S_{j,q}} \cdot E_S \cdot A_{bar_j} & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total force in reinforcement:

$$F_{R_q} := \sum_j F_{S_{j,q}}$$

Calculate moment from reinforcement about section centroid:

$$M_{R_q} := \begin{cases} \sum_j -(\varepsilon_{S_{j,q}} E_S A_{bar_j} y_{bar_j}) & \text{if } A_{BAR} > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate strain in steel tube at extreme tension fiber:

$$\varepsilon_{tds_q} := \frac{-(y_{SY_q} + y_{tt})}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate strain in steel tube at extreme compression fiber:

$$\varepsilon_{tdc_q} := \frac{y_{tc} - y_{SY_q}}{H_{CY} - y_{SY_q}} \varepsilon_{cc}(f_c, \sigma_{cd_q})$$

Calculate tensile force in steel tube:

$$F_{TS1_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS2_q} := \int_{\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TS} := \begin{cases} F_{TS1} - F_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate compressive force in steel tube:

$$F_{TC1_q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SY_q}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SY_q} \right) \right]}{H_{CY} - y_{SY_q} + y_{tt}} \right] dy$$

$$F_{TC2q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] dy$$

$$F_{TC} := \begin{cases} F_{TC1} - F_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from tensile force in steel tube:

$$M_{TS1q} := \int_{\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2} + y_{tt}} -2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS2q} := \int_{\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} -2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tds_q} \cdot E_S \cdot \left[ y - \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TS} := \begin{cases} M_{TS1} - M_{TS2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate moment from compressive force in steel tube:

$$M_{TC1q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2} + y_{tt}} 2 \sqrt{\left(\frac{H_{CY}}{2} + y_{tt}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC2q} := \int_{-\left(\frac{H_{CY}}{2} - y_{SYq}\right)}^{\frac{H_{CY}}{2}} 2 \sqrt{\left(\frac{H_{CY}}{2}\right)^2 - y^2} \cdot \left[ \frac{\varepsilon_{tdc_q} \cdot E_S \cdot \left[ y + \left( \frac{H_{CY}}{2} - y_{SYq} \right) \right]}{H_{CY} - y_{SYq} + y_{tt}} \right] \cdot y \, dy$$

$$M_{TC} := \begin{cases} M_{TC1} - M_{TC2} & \text{if } ts > 0 \\ 0 & \text{otherwise} \end{cases}$$

Calculate total axial response from section:

$$F_T := F_C + F_R + F_{TS} + F_{TC}$$

$$F_{TC} := F_C$$

Calculate total moment response from section:

$$M_T := M_C + M_R + M_{TS} + M_{TC}$$

$$M_{TC} := M_C$$



### CALCULATE MAXIMUM ALLOWABLE AXIAL FORCE IN SECTION

Limiting strain in axial  
compression:

$$\varepsilon_{cL} := \begin{cases} \min(\varepsilon_{cc}, \varepsilon_{tc}) & \text{if } (A_{BAR} = 0) \cdot (ts \neq 0) \cdot (f_c \neq 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}) & \text{if } (ts = 0) \cdot (A_{BAR} \neq 0) \cdot (f_c \neq 0) \\ \varepsilon_{tc} & \text{if } (A_{BAR} = 0) \cdot (f_c = 0) \\ \varepsilon_{rc} & \text{if } (ts = 0) \cdot (f_c = 0) \\ \min(\varepsilon_{cc}, \varepsilon_{rc}, \varepsilon_{tc}) & \text{otherwise} \end{cases} \quad \varepsilon_{cL} = 0.001950$$

Limiting concrete stress in axial compression

$$\sigma_{cL} := \begin{cases} \sigma_{cd2} & \text{if } f_c > 0 \\ 0 & \text{otherwise} \end{cases} \quad \sigma_{cL} = 18.93 \text{ MPa}$$

$$P_{MAX} := \sigma_{cL} \cdot A_C (1 - \rho) + \varepsilon_{cL} \cdot E_S (A_{BAR} + A_{ST})$$

$$P_{MAX} = 21821.2 \text{ kN} \quad F_{T_1} := P_{MAX} \quad M_{T_1} := 0 \cdot \text{kN} \cdot \text{m}$$

$$P_{MAXC} := \sigma_{cL} \cdot A_C \cdot (1 - \rho)$$

$$P_{MAXC} = 17743.7 \text{ kN} \quad F_{TC_1} := P_{MAXC} \quad M_{TC_1} := 0 \cdot \text{kN} \cdot \text{m}$$

### CALCULATE MINIMUM ALLOWABLE AXIAL FORCE IN SECTION

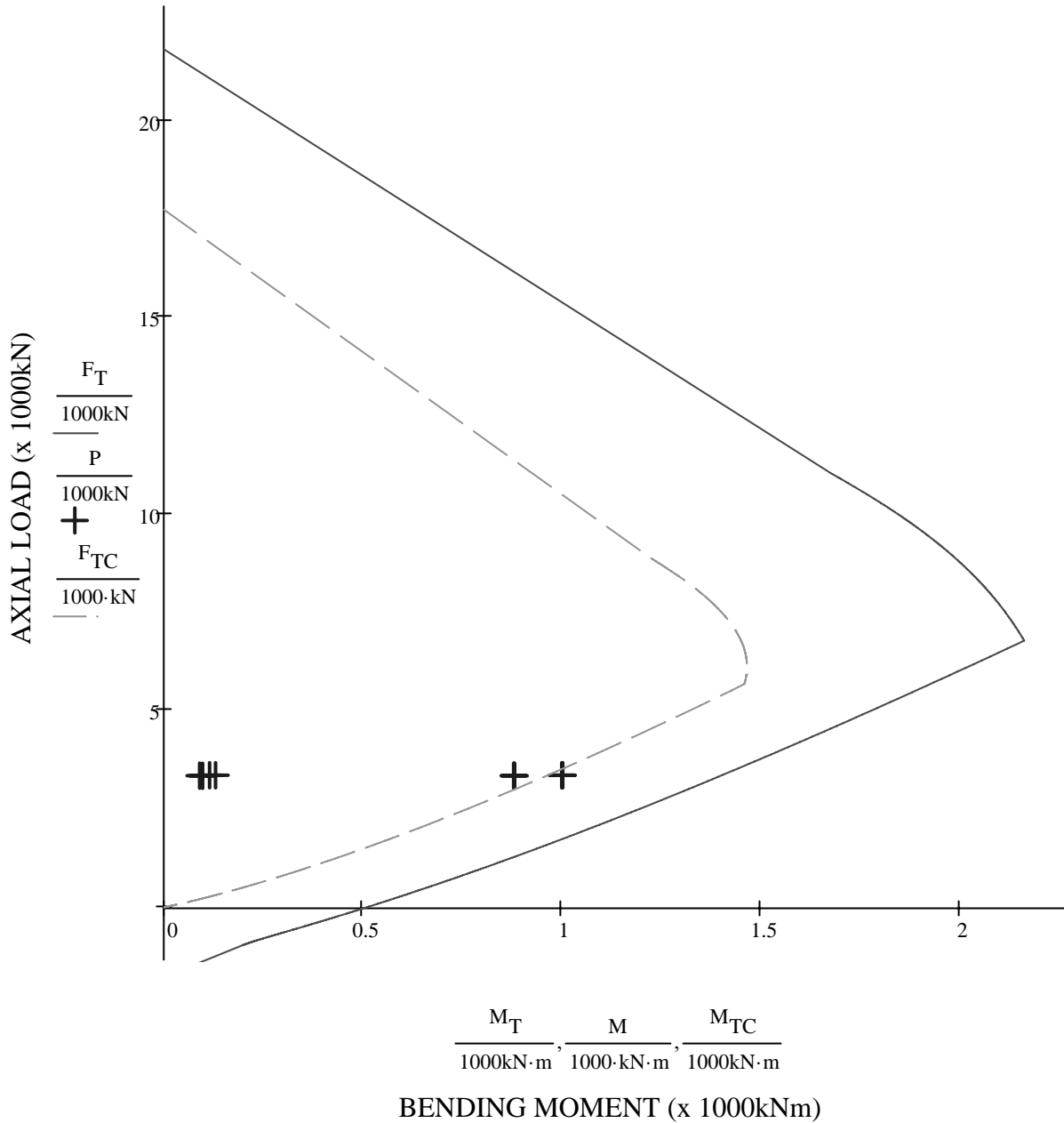
$$P_{MIN} := \begin{cases} \varepsilon_{rs} \cdot E_S (A_{BAR}) & \text{if } ts = 0 \\ \varepsilon_{ts} \cdot E_S (A_{ST}) & \text{if } A_{BAR} = 0 \\ \max(\varepsilon_{ts}, \varepsilon_{rs}) \cdot E_S (A_{BAR} + A_{ST}) & \text{otherwise} \end{cases}$$

$$P_{MIN} = -1777.4 \text{ kN} \quad F_{T_{ns+1}} := P_{MIN} \quad M_{T_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

$$\text{Limit} := \begin{cases} \min(P, F_T) \cdot 0.75 & \text{if } \min(P) > 0 \\ \min(P, F_T) \cdot 1.25 & \text{otherwise} \end{cases}$$

$$P_{MINC} := 0 \text{ kN} \quad M_{TC_{ns+1}} := 0 \cdot \text{kN} \cdot \text{m}$$

Diameter of Column	D = 1100 mm	Characteristic strength of concrete	$f_c = 30 \text{ MPa}$
Percentage reinforcement	$\rho = 1.10 \%$	Yield Strength of Rebar	$f_y = 390 \text{ MPa}$
Thickness of CHS	$t_s = 0 \text{ mm}$	Yield Strength of CHS	$f_{ys} = 250 \text{ MPa}$



Equation of interaction line - upper region (between 1 and 2 calculation points)

$$m1 := \frac{M_{T_2} - M_{T_1}}{F_{T_2} - F_{T_1}} \quad c1 := F_{T_1}$$

Equation of interaction line - lower region (between ns and ns+1 calculation points)

$$m2 := \frac{M_{T_{ns}} - M_{T_{ns+1}}}{F_{T_{ns}} - F_{T_{ns+1}}} \quad c2 := F_{T_{ns+1}}$$

r := 1 .. 8

$$M_{SLS_r} := \begin{cases} 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r > F_{T_1} \\ 0.000000000000000001 \cdot \text{kN}\cdot\text{m} & \text{if } P_r < F_{T_{ns+1}} \\ (P_r - c1) \cdot m1 & \text{if } (P_r > F_{T_2}) \cdot (P_r \leq F_{T_1}) \\ (P_r - c2) \cdot m2 & \text{if } (P_r \geq F_{T_{ns+1}}) \cdot (P_r < F_{T_{ns}}) \\ \text{otherwise} \\ \begin{cases} j \leftarrow 1 \\ \text{while } F_{T_j} > P_r \\ j \leftarrow j + 1 \\ M_{T_j} \end{cases} \end{cases}$$

$$\text{StressFactor}_r := \begin{cases} \text{"No Result"} & \text{if } M_{SLS_r} < 0.000000000000000001 \cdot \text{kN}\cdot\text{m} \\ \frac{M_r}{M_{SLS_r}} & \text{otherwise} \end{cases}$$

$$P = \begin{pmatrix} 3359 \\ 3359 \\ 3357 \\ 3357 \\ 3346 \\ 3346 \\ 3344 \\ 3344 \end{pmatrix} \text{ kN} \quad M = \begin{pmatrix} 1001 \\ 115 \\ 1004 \\ 131 \\ 880 \\ 90 \\ 883 \\ 98 \end{pmatrix} \text{ kN}\cdot\text{m} \quad M_{SLS} = \begin{pmatrix} 1393.5 \\ 1393.5 \\ 1393.5 \\ 1393.5 \\ 1393.5 \\ 1393.5 \\ 1393.5 \\ 1393.5 \end{pmatrix} \text{ kN}\cdot\text{m} \quad \text{StressFactor} = \begin{pmatrix} 0.718 \\ 0.083 \\ 0.720 \\ 0.094 \\ 0.632 \\ 0.065 \\ 0.633 \\ 0.070 \end{pmatrix}$$

**RESULTS SUMMARY**  
**SERVICEABILITY LIMIT STATE ANALYSIS OF CIRCULAR BEAM COLUMN**

Diameter of Column		1100	mm				
Percentage of rebar		1.10	%				
Load Case Ref	Pier	Applied Service Axial Load kN	Applied Service Bending Moment kNm	Service Limit State Bending Moment kNm	Allowable Stress Factor	Applied Stress Factor	Serviceability Limit State Design Result
1	P71	3359	1001	1393.5	140%	72%	OK
2	P71	3359	115	1393.5	140%	8%	OK
3	P72	3357	1004	1393.5	140%	72%	OK
4	P72	3357	131	1393.5	140%	9%	OK