

CHAPTER 5 GROUND SILL

5.1. Ground Sill with Head at WF. 124

Location and Purpose

The following groundsill is proposed in the river improvement plan.

Being located at 1,055 m upstream portion from Simongan Weir, this ground sill is placed at the point in which the riverbed elevation changes in the form of step.

The requirements that the ground sill must meet are i) to prevent riverbed degradation ii) to stabilize the upstream and downstream riverbeds and, iii) to maintain longitudinal and cross sectional forms of river channel.

Structural Type

The ground sill (WF 124) is of concrete gravity type connected with an apron to safeguard its own body from hydraulic force during floods. The concrete body is constructed on the hard sandy layer without using foundation piles. Flexible gabion mattresses are placed on upstream and downstream riverbeds of the ground sill with a length of 20 m and 30 m respectively to protect riverbed, while 3.5 m length of RC Sheet piles are provided at both end of main sill body for protection against seepage.

The design of ground sills is made to ensure structural stability against sliding, overturning and bearing capacity of the sub-base ground, and to satisfy hydraulic stability against piping, uplift and scouring.

(1) Structural Dimension, etc

(a) River Channel

	Upstream	downstream
Riverbed width	40.0 m	35.0 m
Elevation of riverbed	EL. +3.843	EL. +2.343
Side slope (m)	2.0 m	2.0 m
Riverbed slope (I)	$1/1250$	$1/1250$
Manning Coefficient (n)	0.030	0.030

(b) Hydraulic Drop

Main body height	(H ₁)	2.50 m
Main body crown width	(B)	1.50 m
Main body bottom width	(B _o)	2.25 m
Drop height	(p)	1.50 m
Apron thickness	(t)	1.00 m
Apron length	(L)	9.00 m
Total bottom width	(L _o)	10.50 m

(c) Side Wall

		Main wall	Transition wall	
			Upstream end	Downstream end
Total height	(h _o)	2.50 m	2.50 m	1.00 m
Wall height	(h)	2.00 m	2.00 m	0.50 m
Wall thickness	(b ₁ -b ₂)	(0.3 - 0.4) m	(0.3 - 0.4) m	0.30 m
Slab thickness	(h ₁)	0.50 m	0.50 m	0.50 m
Bottom width of slab	(b)	1.80 m	1.80 m	0.80 m
Length	(l)	10.50 m	10.90 m	

(d) Revetment

Length	Upstream	20.00 m
	Main structure	10.50 m
	Downstream	30.00 m
Section	as shown on standard drawings	

(e) Riverbed protection

Upstream length	(L ₁)	20.00 m
Downstream length	(L ₂)	30.00 m
Thickness	(t ₁)	0.50 m

5.1.1 Hydraulic Design

(1) Design Condition

(a) Normal condition

Design discharge	Q = 70.0 m ³ /s
Upstream water level	EL. + 5.283 m
Downstream water level	EL. + 3.893 m
Upstream water depth	H _o = 1.55 m
Downstream water depth	H = 1.44 m

(b) Flood condition

Design discharge	Q = 790.0 m ³ /s
Upstream water level	EL. + 9.743 m
Downstream water level	EL. + 8.843 m
Upstream water depth	H _o = 5.90 m
Downstream water depth	H = 6.50 m

(2) Examination of Apron Length

(a) Normal condition

$$\begin{aligned}\Delta h &= (+5.283) - (+3.893) = 1.39 \text{ m} \\ &> H_o/3 (= 0.517 \text{ m})\end{aligned}$$

perfect overflow will be occurred.

Upstream channel :

$$\begin{aligned}A &= (B + m \cdot H_o) H_o \\ &= (40.0 + 2 \times 1.44) \times 1.44 = 61.747 \text{ m}^2\end{aligned}$$

$$\begin{aligned}V_o &= Q/A \\ &= 70 / 61.747 = 1.134 \text{ m/s}\end{aligned}$$

$$V_o^2 / 2g = (1.134)^2 / 2 / 9.8 = 0.065 \text{ m}$$

Examination of hydraulic jump by Bernoulli equation

$$\begin{aligned}d_1 + V_1^2 / 2g &= p + H_o + V_o^2 / 2g \\ &= 1.5 + 1.44 + 0.065 = 3.005 \text{ m}\end{aligned}$$

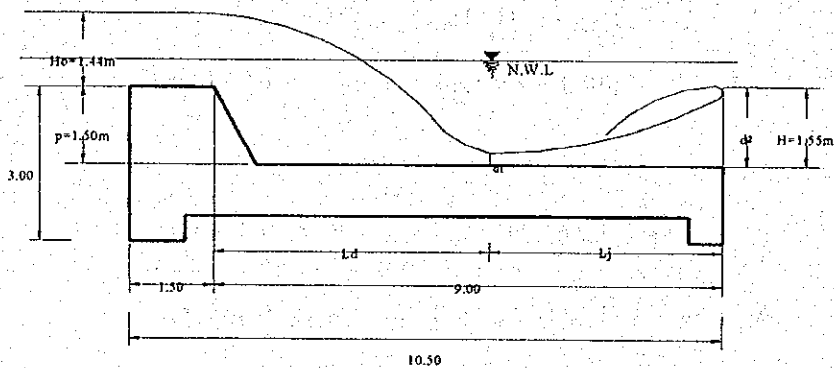
$$\text{Trial } d_1 = 0.23 \text{ m}$$

$$\begin{aligned}V_1 &= Q / b / d_1 \\ &= 70.0 / 39.4 / 0.23 = 7.725 \text{ m/s}\end{aligned}$$

$$\begin{aligned}d_1 + V_1^2 / 2g &= 0.23 + (7.725)^2 / 2 / 9.8 = 3.044 \text{ m} \\ &\sim 3.005 \text{ m}\end{aligned}$$

$$\begin{aligned}F_r &= V_1 / (g \cdot d_1)^{1/2} \\ &= 7.725 / (9.8 \times 0.23)^{1/2} = 5.145\end{aligned}$$

$$\begin{aligned}
 d_2 &= d_1 \times 0.5 \left((1 + 8 F_1^2)^{1/2} - 1 \right) \\
 &= 0.23 \times 0.5 \times \left((1 + 8 \times (5.145)^2)^{1/2} - 1 \right) = 1.56 \text{ m} \\
 L_j &= c (d_2 - d_1) \quad ; \quad C = 5 \\
 &= 5 \times (1.56 - 0.23) = 6.65 \text{ m} \\
 L_d &= V_o \left(2 (p + H_o/2) / g \right)^{1/2} \\
 &= 1.134 \times \left(2 \times (1.5 + 1.44/2) / 9.8 \right)^{1/2} = 0.76 \text{ m} \\
 L &= L_d + L_j \\
 &= 6.65 + 0.76 = 7.41 \text{ m} \\
 &< \text{adopted } L = 9.0 \text{ m}
 \end{aligned}$$



(b) Flood condition

$$\begin{aligned}
 \Delta h &= (+9.743) - (+8.843) = 0.90 \text{ m} \\
 &> H_o / 3 (= 1.967 \text{ m})
 \end{aligned}$$

unperfect overflow will be occurred (No hydraulic jump).

(3) Examination of Apron Thickness

Applying the following formula

$$\begin{aligned}
 t &= 0.1 (0.6 p + 3 H_o - 1.0) \\
 &= 0.1 \times (0.6 \times 1.5 + 3 \times 1.44 - 1.0) = 0.422 \text{ m} \\
 &< \text{adopted } t = 1.0 \text{ m}
 \end{aligned}$$

(4) Examination of Creep Length

Normal condition, after construction, downstream channel start to fill.

Creep length will be estimated by Lane's method as follows :

$$\begin{aligned} Cl &= (\Sigma L_v + \Sigma L_h / 3) / H \\ Cl &\geq C (= 7 \text{ for fine sand}) \end{aligned}$$

The cut off wall of about 3.5 m length are provided at both end.

$$\begin{aligned} H &= 1.44 + 1.5 = 2.94 \text{ m} \\ L_v &= 3.0 + 1.5 + 2 \times 0.5 + 4 \times 3.5 = 19.5 \text{ m} \\ L_h &= 10.5 \text{ m} \\ C_l &= (19.5 + 10.5 / 3) / 2.94 = 7.823 \\ &> C (= 7) \end{aligned}$$

5.1.2 Structural Design

5.1.2.1 Main Sill Body

(1) Design Condition

(a) Hydraulic Condition

(i) Normal Condition

Design discharge	Q = 70.0 m ³ /s
Upstream water depth	H _o = 1.55 m
Downstream water depth	H = 1.44 m

(ii) Flood condition

Design discharge	Q = 790.0 m ³ /s
Upstream water depth	H _o = 5.90 m
Downstream water depth	H = 6.50 m

(iii) Seismic condition

Water level	EL. + 5.20
Upstream water depth	H _o = 5.90 m
Downstream water depth	H = 6.50 m

(b) The material data

(i) Soil Material *)

Original soil material

Wet unit weight	$\gamma_t = 1.6 \text{ t/m}^3$
Submerged unit weight	$\gamma'_s = 0.8 \text{ t/m}^3$
Internal friction angle	$\phi = 27^\circ$
Cohesion	$c = 0.0 \text{ t/m}^2$

Back fill under the main body

Wet unit weight	$\gamma_{t1} = 1.8 \text{ t/m}^3$
Submerged unit weight	$\gamma'_{s1} = 1.0 \text{ t/m}^3$
Internal friction angle	$\phi_1 = 30^\circ$
Cohesion	$c_1 = 0.0 \text{ t/m}^2$

(ii) Others

Unit weight of mass concrete	$\gamma'_c = 2.35 \text{ t/m}^3$
Unit weight of gabion mattress	$\gamma_{gm} = 2.00 \text{ t/m}^3$
Unit weight of water	$\gamma_w = 1.0 \text{ t/m}^3$
Seismic coefficient	$kh = 0.12$

*) Based on soil investigation on RB33 and RB34 (Location WF124) soil layer at El. + 0.3m to + 5.0m are silty sand, fine to medium with average N-value of about N = 12.

Soil internal friction angle will be estimated based on N-value as follows : $\phi = 15 + \sqrt{15 \cdot N} = 27.25 \sim 27^\circ$

For N=12, assumed $\gamma_t = 1.6 \text{ t/m}^3$ (wet), $\gamma'_s = 0.8 \text{ t/m}^3$ (submerged)

At main body foundation, original soil material of about 1 m depth will be excavated and to be filled by very fine sand with an internal friction angle of about $\phi_1 = 30^\circ$

(c) Design Load

(i) Earth pressure

Coulomb's formula

$$\alpha = 0, \quad \theta = 0, \quad \delta = 0$$

Passive earth pressure is omitted.

(ii) Uplift pressure

Effective uplift pressure is 70% only.

(d) The Combination of Load

Load		Condition	Normal	Flood	Seismic
The vertical load	Weight of main body		+	+	+
	Weight of water		+	+	+
	Uplift pressure		+	+	+
The horizontal load	Earth pressure		+	+	+
	Water pressure		+	+	+
	Horizontal earthquake pressure				+

“+” consider in the calculation

(2) Stability Analysis

(a) Coefficient of Active earth pressure

Applying Coulomb's formula as follows:

(in ordinary)

$$K_a = \frac{\cos^2(\phi - \theta)}{\cos^2\theta \cos(\phi + \delta) \left[1 + \sqrt{\frac{\sin(\phi + \delta) \sin(\phi - \alpha)}{\cos(\theta + \delta) \cos(\theta - \alpha)}} \right]^2}$$

(in seismic)

$$K_{ca} = \frac{\cos^2(\phi - \theta_o - \theta)}{\cos\theta_o \cdot \cos^2\theta \cdot \cos(\theta + \theta_o + \delta) \left[1 + \sqrt{\frac{\sin(\phi + \delta) \sin(\phi - \alpha - \theta_o)}{\cos(\theta + \theta_o + \delta) \cos(\theta - \alpha)}} \right]^2}$$

$$kh' = \frac{\gamma_s}{\gamma_s - 1} kh$$

$$\tan \theta = \frac{kh}{1 - kv}, kv = 0 \quad (\text{saturated})$$

$$\tan \theta_o = \frac{kh'}{1 - kv} \quad (\text{submerged})$$

$$\text{For } \theta = 0, \delta = 0, \alpha = 0$$

$$kh' = \frac{1.8}{1.8 - 1} \times 0.12 = 0.27$$

$$\theta = \text{atan } 0.12 = 6.84$$

$$\theta_o = \text{atan } 0.27 = 15.11$$

(in ordinary)

$$K_a = \frac{\cos^2(27)}{1 + \sqrt{\sin^2(27)}} = 0.376$$

(in seismic)

$$K_{ca} = \frac{\cos^2(27 - 6.84)}{\cos 6.84 \times \cos 6.84 \times \left[1 + \sqrt{\frac{\sin 27 \times \sin (27 - 6.84)}{\cos (6.84)}} \right]^2}$$

$$= 0.458$$

$$K_{ca} = \frac{\cos^2(27 - 15.11)}{\cos 15.11 \times \cos 15.11 \times \left[1 + \sqrt{\frac{\sin 27 \times \sin (27 - 15.11)}{\cos (15.11)}} \right]^2}$$

$$= 0.5975$$

(b) Allowable bearing capacity

Bearing capacity beneath structure will be estimated by the following formula:

$$q_u = \alpha \cdot c \cdot k \cdot N_c + k \cdot q \cdot N_q + \frac{1}{2} \cdot \gamma \cdot B \cdot N_\gamma$$

$$k = 1 + 0.3 D_f / B$$

$$q_s = q_u / 3$$

$$q_{es} = q_u / 2$$

$$\text{For } \theta = 27^\circ, N_q = 14.0$$

$$N_\gamma = 9.0$$

At upstream end, $D_f = 3.0$ m

$$k = 1 + 0.3 \times 3 / 10.50 = 1.010$$

$$\begin{aligned} q_u &= 1.01 \times (3.0 \times 0.8) \times 14.0 + \frac{1}{2} \times 1.0 \times 10.5 \times 9.0 \\ &= 64.386 \text{ t/m}^2 \end{aligned}$$

$$q_a = 27.062 \text{ t/m}^2 \quad (\text{in ordinary})$$

$$q_{es} = 40.593 \text{ t/m}^2 \quad (\text{in seismic})$$

At downstream end, $D_f = 1.5$ m

$$k = 1 + 0.3 \times 1.5 / 10.50 = 1.02$$

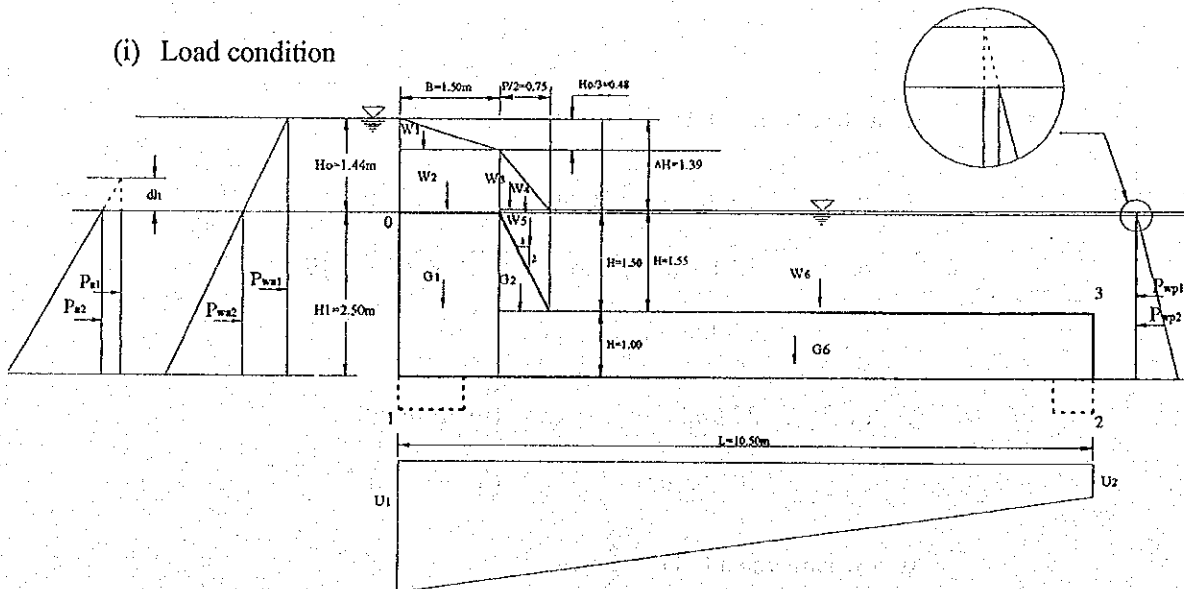
$$\begin{aligned} q_u &= 1.02 \times (1.5 \times 0.8) \times 14.0 + \frac{1}{2} \times 1.0 \times 10.5 \times 9.0 \\ &= 54.936 \text{ t/m}^2 \end{aligned}$$

$$q_a = 21.462 \text{ t/m}^2 \quad (\text{in ordinary})$$

$$q_{es} = 32.193 \text{ t/m}^2 \quad (\text{in seismic})$$

(c) Stability analysis on Normal Condition

(i) Load condition



(ii) Weight of structure

$$\begin{aligned}
 G_1 &= (p + t) \times B \times \gamma'c \\
 &= 2.5 \times 1.5 \times 2.35 &= 8.812 \text{ t/m} \\
 x_1 &= 10.5 - 1.5/2 &= 9.750 \text{ m} \\
 G_2 &= \frac{1}{4} p^2 \times \gamma'c \\
 &= \frac{1}{4} \times (1.5)^2 \times 2.35 &= 1.322 \text{ t/m} \\
 x_2 &= 10.5 - 1.5 - 0.75/3 &= 8.750 \text{ m} \\
 G_3 &= (L - B) \times t \times \gamma'c \\
 &= 9 \times 1.0 \times 2.35 &= 21.150 \text{ t/m} \\
 x_3 &= (10.5 - 1.5)/2 &= 4.500 \text{ m}
 \end{aligned}$$

(iii) Uplift pressure

Applying the following formula:

$$U_x = H_x - L_x / L \cdot \Delta H$$

$$\Delta H = 1.39 \text{ m}$$

$$L = 3.0 + 10.5 + 1.5 + 4 \times 3.5 = 30 \text{ m}$$

Point	H _x	L _x	u _x
0	1.44	0.00	1.440
1	4.44	3.00	4.301
2	4.44	28.50	3.120
3	2.94	30.00	1.550

$$\begin{aligned}
 U_{1-3} &= (U_1 + U_2) / 2 \times L \times \gamma_w \\
 &= (4.301 + 3.120) / 2 \times 10.5 \times 1.0 = 38.960 \text{ t/m} \\
 x_u &= 10.5 - (4.301 + 2 \times 3.12) / 7.421 \times 10.5 / 3 = 5.529 \text{ m}
 \end{aligned}$$

(iv) Water pressure

Vertical

$$\begin{aligned}
 W_1 &= \frac{1}{2} \times (H_0/3) \times B \times \gamma_w \\
 &= \frac{1}{2} \times (0.48) \times 1.5 \times 1.0 = 0.360 \text{ t/m}
 \end{aligned}$$

$$x_{w1} = 10.5 - 1.5 / 2 = 10.000 \text{ m}$$

$$\begin{aligned}
 W_2 &= \left(\frac{2}{3}H_0\right) \times B \times \gamma_w \\
 &= 0.96 \times 1.50 \times 1.0 = 1.440 \text{ t/m}
 \end{aligned}$$

$$x_{w2} = 10.5 - 1.5 / 3 = 9.750 \text{ m}$$

$$\begin{aligned}
 W_3 &= \frac{1}{2} \times \left(\frac{1}{2}p\right) \times (\Delta H - H_0/3) \times \gamma_w \\
 &= \frac{1}{2} \times 0.75 \times 0.91 \times 1.0 = 0.341 \text{ t/m}
 \end{aligned}$$

$$x_{w3} = 10.5 - 1.5 - 0.75 / 2 = 8.750 \text{ m}$$

$$\begin{aligned}
 W_4 &= \left(\frac{1}{2}p\right) \times (H-p) \times \gamma_w \\
 &= 0.75 \times 0.05 \times 1.0 = 0.380 \text{ t/m}
 \end{aligned}$$

$$x_{w4} = 10.5 - 1.5 - 0.75 / 2 = 8.625 \text{ m}$$

$$\begin{aligned}
 W_5 &= \frac{1}{2} \times \left(\frac{1}{2}p\right) \times p \times \gamma_w \\
 &= \frac{1}{2} \times 0.75 \times 1.5 \times 1.0 = 0.563 \text{ t/m}
 \end{aligned}$$

$$x_{w5} = 10.5 - 1.5 - \frac{2}{3} \times 0.75 = 8.500 \text{ m}$$

$$\begin{aligned}
 W_6 &= H \times (L - B - p/2) \times \gamma_w \\
 &= 1.55 \times 8.25 \times 1.0 = 12.787 \text{ t/m}
 \end{aligned}$$

$$x_{w6} = (10.5 - 2.25) / 2 = 4.125 \text{ m}$$

Horizontal

$$P_{wal} = H_0 \times \gamma_w \times H_1$$

$$\begin{aligned}
 &= 1.44 \times 1.0 \times 2.5 & = 3.600 \text{ t/m} \\
 y_{wa1} &= H_1/2 & = 1.250 \text{ m} \\
 P_{wa2} &= \frac{1}{2} \times H_1 \times \gamma_w & \\
 &= \frac{1}{2} \times (2.5)^2 \times 1.0 & = 3.125 \text{ t/m} \\
 y_{wa2} &= H_1/3 & = 0.8333 \text{ m} \\
 P_{wp1} &= (H-p) \times \gamma_w \times H_1 & \\
 &= 0.05 \times 1.0 \times 2.5 & = 0.125 \text{ t/m} \\
 y_{wp1} &= 1.250 \text{ m} \\
 P_{wp2} &= \frac{1}{2} \times H_1^2 \times \gamma_w & \\
 &= \frac{1}{2} \times (2.5)^2 \times 1.0 & = 3.125 \text{ t/m} \\
 y_{wp2} &= 0.833 \text{ m}
 \end{aligned}$$

(v) Earth pressure

Surcharge due to gabion :

$$\begin{aligned}
 dh &= (t_1 \times \gamma_{gm}) / \gamma'_s - t_1 \\
 &= (0.5 \times 1.20) / 0.8 - 0.5 & = 0.250 \text{ t/m}
 \end{aligned}$$

Active earth pressure :

$$\begin{aligned}
 P_{a1} &= dh \times \gamma'_s \times K_a \times H_1 \\
 &= 0.25 \times 0.8 \times 0.376 \times 2.5 & = 0.188 \text{ t/m} \\
 y_{a1} &= H_1/2 & = 1.250 \text{ m} \\
 P_{a2} &= \frac{1}{2} \times H_1^2 \times \gamma'_s \times K_a \\
 &= \frac{1}{2} \times (2.5)^2 \times 0.8 \times 0.376 & = 0.940 \text{ t/m} \\
 y_{a2} &= H_1/3 & = 0.833 \text{ m}
 \end{aligned}$$

(vi) Vertical Force and Moment

	Vertical Force (t/m)	Arm (m)	Vertical Moment (tm/m)
G ₁	8.812	9.750	85.917
G ₂	1.322	8.750	11.568
G ₃	21.150	4.500	95.175
W ₁	0.360	10.000	3.600
W ₂	1.440	9.750	14.040
W ₃	0.341	8.750	2.984
W ₄	0.038	8.625	0.328
W ₅	0.563	8.500	4.786
W ₆	12.787	4.125	52.746
U _{1,2}	-27.272	5.529	-150.787
FV	19.541	MV	120.357

* Effective uplift of about 70%.

(vii) Horizontal Force and Moment

	Horizontal Force (t/m)	Arm (m)	Horizontal Moment (tm/m)
P _{a1}	0.138	1.250	0.235
P _{a2}	0.940	0.833	0.783
P _{wa1}	3.600	1.250	4.500
P _{wa2}	3.125	0.833	2.604
P _{wp1}	-0.125	1.250	-0.156
P _{wp2}	-3.125	0.833	-2.604
FH	4.603	MH	5.362

* Effective uplift of about 70%.

(viii) Check of stability

Stability against sliding

$$\begin{aligned} SF &= FV / FH \cdot \tan \phi_1 \\ &= 19.541 / 4.603 \times \tan 30 &= 2.451 \\ &> 1.5 \end{aligned}$$

Stability against overturning

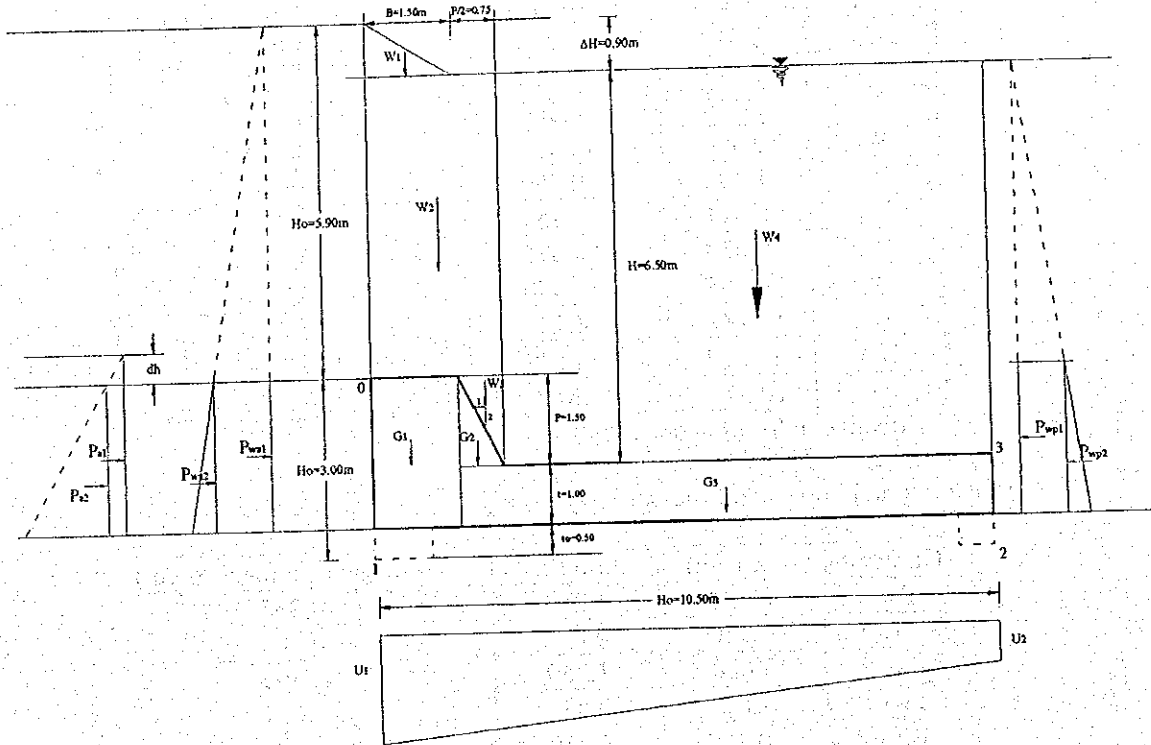
$$\begin{aligned} e &= L/2 - (MV - MH) / FV \\ &= 10.5/2 - (120.357 - 5.362) / 19.541 &= 0.635 (-) \\ &< L/6 (1.75 \text{ m}) \end{aligned}$$

Stability of bearing strata

$$\begin{aligned} q &= FV/L (1 \pm 6 e/L) \\ q_{\max} &= 19.541 / 10.5 \times (1 + 6 \times 0.635/10.5) &= 2.536 \text{ t/m}^2 \\ &< q_s = 21.462 \text{ t/m}^2 \\ q_{\min} &= 19.541 / 10.5 \times (1 - 6 \times 0.635/10.5) &= 1.186 \text{ t/m}^2 \\ &< q_a = 27.062 \text{ t/m}^2 \end{aligned}$$

(d) Stability analysis on Flood Condition

(i) Load condition



(ii) Weight of structure

$$\begin{aligned}
 G_1 &= (p + t) \times B \times \gamma'c &= 8.812 \text{ t/m} \\
 &= 2.5 \times 1.5 \times 2.35 \\
 x_1 &= 10.5 - 1.5/2 &= 9.750 \text{ m} \\
 G_2 &= \frac{1}{4} p^2 \times \gamma'c &= 1.322 \text{ t/m} \\
 &= \frac{1}{4} \times (1.5)^2 \times 2.35 \\
 x_2 &= 10.5 - 1.5 - 0.75/3 &= 8.750 \text{ m} \\
 G_3 &= (L - B) \times t \times \gamma'c &= 21.150 \text{ t/m} \\
 &= 9 \times 1.0 \times 2.35 \\
 x_3 &= (10.5 - 1.5)/2 &= 4.500 \text{ m}
 \end{aligned}$$

(iii) Uplift pressure

Applying the following formula:

$$\begin{aligned}
 U_x &= H_x - L_x / L \cdot \Delta H \\
 \Delta H &= 0.90 \text{ m}
 \end{aligned}$$

$$L = 3.0 + 10.5 + 1.5 + 4 \times 3.5 = 30 \text{ m}$$

Point	H_x	L_x	U_x
0	5.90	0.00	5.900
1	8.90	3.00	8.810
2	8.90	28.50	8.045
3	7.40	30.00	6.500

$$U_{1-2} = (U_1 + U_2) / 2 \times L \times \gamma_w$$

$$= (8.810 + 8.045) / 2 \times 10.5 \times 1.0 = 88.489 \text{ t/m}$$

$$x_u = 10.5 - (8.81 + 2 \times 8.045) / 16.855 \times 10.5 / 3 = 5.329 \text{ m}$$

(iv) Water pressure

Vertical

$$W_1 = \frac{1}{2} \times \Delta H \times B \times \gamma_w$$

$$= \frac{1}{2} \times 0.90 \times 1.5 \times 1.0 = 0.675 \text{ t/m}$$

$$x_{w1} = 10.5 - 1.5 / 3 = 10.000 \text{ m}$$

$$W_2 = (B + p/2) \times (H-p) \times \gamma_w$$

$$= 2.25 \times 5.00 \times 1.0 = 11.250 \text{ t/m}$$

$$x_{w2} = 10.5 - (B + p/2) / 2 = 9.375 \text{ m}$$

$$W_3 = \frac{1}{2} \times p \times (\frac{1}{2}p) \times \gamma_w$$

$$= \frac{1}{2} \times 1.50 \times 0.75 \times 1.0 = 0.563 \text{ t/m}$$

$$x_{w3} = 10.5 - 1.5 - 2/3 \times 0.75 = 8.500 \text{ m}$$

$$W_4 = H \times (L - B - p/2)$$

$$= 6.5 \times (10.5 - 2.25) = 53.625 \text{ t/m}$$

$$x_{w4} = 8.250 / 2 = 4.125 \text{ m}$$

Horizontal

$$P_{wa1} = H_o \times \gamma_w \times H_t$$

$$= 5.90 \times 1.0 \times 2.5 = 14.750 \text{ t/m}$$

$$y_{wa1} = H_t / 2 = 1.250 \text{ m}$$

$$P_{wa2} = \frac{1}{2} \times H_t \times \gamma_w$$

$$= \frac{1}{2} \times (2.5)^2 \times 1.0 = 3.125 \text{ t/m}$$

$$y_{wa2} = H_t / 3 = 0.833 \text{ m}$$

$$P_{wpt} = (H - p) \times \gamma_w \times H_t$$

$$= 5.00 \times 1.0 \times 2.5 = 12.500 \text{ t/m}$$

$$y_{wpt} = 1.250 \text{ m}$$

$$\begin{aligned}
 P_{wp2} &= \frac{1}{2} \times H_1^2 \times \gamma_w \\
 &= \frac{1}{2} \times (2.5)^2 \times 1.0 &= 3.125 \text{ t/m} \\
 y_{wp2} &= 0.833 \text{ m}
 \end{aligned}$$

(v) Earth pressure

Surcharge due to gabion :

$$\begin{aligned}
 dh &= (t_1 \times \gamma'_{gm}) / \gamma'_s - t_1 \\
 &= (0.5 \times 1.20) / 0.8 - 0.5 &= 0.250 \text{ t/m}
 \end{aligned}$$

Active earth pressure :

$$\begin{aligned}
 P_{a1} &= dh \times \gamma'_s \times K_a \times H_1 \\
 &= 0.25 \times 0.8 \times 0.376 \times 2.5 &= 0.188 \text{ t/m}
 \end{aligned}$$

$$y_{a1} = H_1/2 = 1.250 \text{ m}$$

$$\begin{aligned}
 P_{a2} &= \frac{1}{2} \times H_1^2 \times \gamma'_s \times K_a \\
 &= \frac{1}{2} \times (2.5)^2 \times 0.8 \times 0.376 &= 0.940 \text{ t/m}
 \end{aligned}$$

$$y_{a2} = H_1/3 = 0.833 \text{ m}$$

(vi) Vertical Force and Moment

	Vertical Force (t/m)	Arm (m)	Vertical Moment (tm/m)
G ₁	8.812	9.750	85.917
G ₂	1.322	8.750	11.568
G ₃	21.150	4.500	95.175
W ₁	0.675	10.000	6.750
W ₂	11.250	9.375	105.469
W ₃	0.563	8.500	4.786
W ₄	53.625	4.125	221.203
U _{1,2}	-61.942	5.329	-330.089
FV	35.455	MV	200.779

* Effective uplift of about 70%.

(vii) Horizontal Force and Moment

	Horizontal Force (t/m)	Arm (m)	Horizontal Moment (tm/m)
P _{a1}	0.188	1.250	0.235
P _{a2}	0.940	0.833	0.783
P _{wa1}	14.750	1.250	18.438
P _{wa2}	3.125	0.833	2.604
P _{wp1}	-12.500	1.250	-15.625
P _{wp2}	-3.125	0.833	-2.604
FH	3.378	MH	3.831

* Effective uplift of about 70%.

(viii) Check of stability

Stability against sliding

$$\begin{aligned} SF &= FV / FH \cdot \tan \phi \\ &= 35.455 / 3.378 \times \tan 27 \\ &= 6.060 \\ &> 1.5 \end{aligned}$$

Stability against overturning

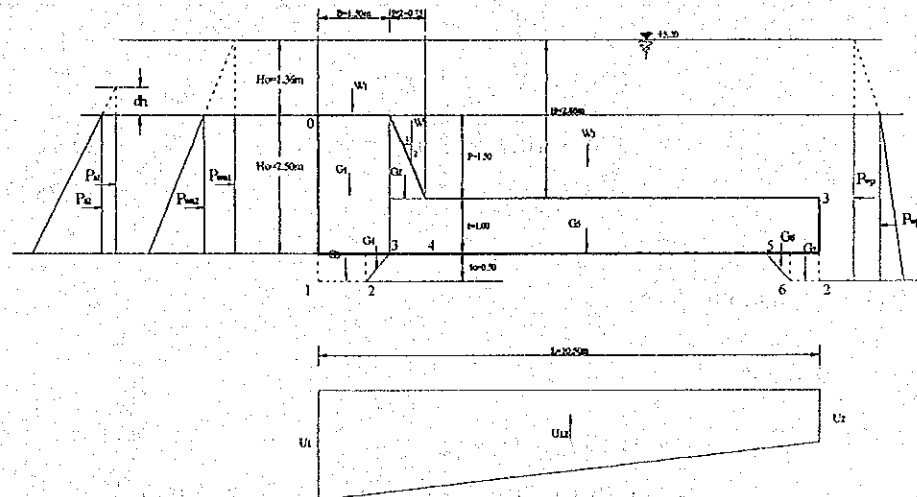
$$\begin{aligned} e &= L/2 - (MV - MH) / FV \\ &= 10.5 / 2 - (200.779 - 3.831) / 35.455 = 0.305 \text{ (-)} \\ &< L/6 \text{ (1.75 m)} \end{aligned}$$

Stability of bearing strata

$$\begin{aligned} q &= FV/L (1 \pm 6 e / L) \\ q_{\max} &= 35.455 / 10.5 \times (1 + 6 \times 0.305 / 10.5) = 3.965 \text{ t/m}^2 \\ &< q_a = 21.462 \text{ t/m}^2 \\ q_{\min} &= 35.455 / 10.5 \times (1 - 6 \times 0.305 / 10.5) = 2.788 \text{ t/m}^2 \\ &< q_a = 27.062 \text{ t/m}^2 \end{aligned}$$

(e) Stability analysis on Seismic Condition

(i) Load condition



(ii) Weight of Structure

$$G_1 = (p + t) \times B \times \gamma'c$$

$$\begin{aligned}
 &= 2.5 \times 1.5 \times 2.35 &= 8.812 \text{ t/m} \\
 x_1 &= 10.5 - 1.5/2 &= 9.750 \text{ m} \\
 G_2 &= \frac{1}{4} p^2 \times \gamma'c & \\
 &= \frac{1}{4} \times (1.5)^2 \times 2.35 &= 1.322 \text{ t/m} \\
 x_2 &= 10.5 - 1.5 - 0.75/3 &= 8.750 \text{ m} \\
 G_3 &= (L - B_1 - B_2) \times t \times \gamma'c & \\
 &= 9 \times 1.0 \times 2.35 &= 21.150 \text{ t/m} \\
 x_3 &= (10.5 - 1.5)/2 &= 4.500 \text{ m}
 \end{aligned}$$

(iii) Uplift pressure

Applying the following formula:

$$U_x = H_x - L_x / L \cdot \Delta H$$

$$\Delta H = 0.00 \text{ m}$$

$$L = 30.0 \text{ m}$$

Point	H_x	L_x	U_x
0	1.36	0.00	1.36
1	4.36	3.00	4.36
2	4.36	28.50	4.36
3	2.86	30.00	2.86

$$\begin{aligned}
 U_{1,2} &= (U_1 + U_2) / 2 \times L \times \gamma_w & \\
 &= 4.36 \times 10.5 \times 1.0 &= 45.78 \text{ t/m} \\
 x_{1,2} &= 10.5 / 2 &= 5.25 \text{ t/m}
 \end{aligned}$$

(iv) Water pressure

Vertical

$$\begin{aligned}
 W_1 &= (B + p/2) \times H_o \times \gamma_w & \\
 &= (1.50 + 0.50) \times 1.36 \times 1.0 &= 3.060 \text{ t/m} \\
 x_{w1} &= 10.5 - 2.25 / 2 &= 9.375 \text{ m} \\
 W_2 &= \frac{1}{2} \times (p/2) \times p \times \gamma_w & \\
 &= \frac{1}{2} \times 0.75 \times 1.50 \times 1.0 &= 0.563 \text{ t/m} \\
 x_{w2} &= 10.5 - 1.5 - 2/3 \times 0.75 &= 8.500 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 W_3 &= (L - B - p/2) \times H \times \gamma_w \\
 &= (10.5 - 1.50 - 0.75) \times 2.86 \times 1.0 = 23.595 \text{ t/m} \\
 x_{w3} &= (10.5 - 1.5 - 0.75) / 2 = 4.125 \text{ m}
 \end{aligned}$$

Horizontal

$$P_{wa} = P_{wp} \quad (\text{balance})$$

(v) Earth pressure

Surcharge due to gabion :

$$\begin{aligned}
 dh &= (t_1 \times \gamma'_{gm}) / \gamma'_s - t_1 \\
 &= (0.5 \times 1.20) / 0.8 - 0.5 = 0.250 \text{ m}
 \end{aligned}$$

Active earth pressure :

$$\begin{aligned}
 P_{ea1} &= dh \times \gamma'_s \times K'_{ea} \times H_1 \\
 &= 0.25 \times 0.8 \times 0.598 \times 2.5 = 0.299 \text{ t/m} \\
 \bar{x}_{ea1} &= H_1 / 2 = 1.250 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 P_{ea2} &= \frac{1}{2} (H_1)^2 \times \gamma'_s \times K'_{ea} \\
 &= \frac{1}{2} (2.5)^2 \times 0.8 \times 0.598 = 1.495 \text{ t/m} \\
 \bar{x}_{ea2} &= H_1 / 3 = 0.833 \text{ m}
 \end{aligned}$$

(vi) Earthquake pressure

$$\begin{aligned}
 G_{e1} &= G_1 \times kh \\
 &= 8.812 \times 0.12 = 1.057 \text{ t/m} \\
 y_{e1} &= 2.5 / 2 = 1.250 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 G_{e2} &= G_2 \times kh \\
 &= 1.322 \times 0.12 = 0.159 \text{ t/m} \\
 y_{e2} &= 1.0 + 1.50 / 3 = 1.50 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 G_{e3} &= G_3 \times kh \\
 &= 21.150 \times 0.12 = 2.538 \text{ t/m} \\
 y_{e3} &= 0.5 + 1.0 / 2 = 0.50 \text{ m}
 \end{aligned}$$

(vii) Vertical Force and Moment

	Vertical Force (t/m)	Arm (m)	Vertical Moment (tm/m)
G ₁	8.812	9.750	85.917
G ₂	1.322	8.750	11.568
G ₃	21.150	4.500	95.175
W ₁	3.060	9.375	28.688
W ₂	0.563	8.500	4.786
W ₃	23.595	4.125	97.329
U ₁₋₂	-32.046	5.250	-168.242
FV _e	26.456	MV _e	155.221

* Effective uplift of about 70%.

(viii) Horizontal Force and Moment

	Horizontal Force (t/m)	Arm (m)	Horizontal Moment (tm/m)
G _{e1}	1.057	1.250	1.321
G _{e2}	0.159	1.500	0.239
G _{e3}	2.538	0.500	1.269
P _{ea1}	0.299	1.250	0.374
P _{ea2}	1.495	0.833	1.246
FH _e	5.548	MH _e	4.449

• Effective Uplift of about 70%.

(ix) Check of stability

Stability against sliding

$$\begin{aligned} SF &= FV_e / FH_e \cdot \tan \phi_1 \\ &= 26.456 / 5.548 \times \tan 30 &= 2.753 \\ &> 1.200 \end{aligned}$$

Stability against overturning

$$\begin{aligned} e &= L/2 - (MV_e - MH_e) / FV_e \\ &= 10.5/2 - (155.221 - 4.449) / 26.456 &= 0.449 (-) \\ &< L/3 (3.50 \text{ m}) \end{aligned}$$

Stability of bearing strata

$$q = FV_e / L (1 \pm 6 e / L)$$

$$q_{\max} = 26.456 / 10.5 \times (1 + 6 \times 0.449/10.5) = 3.166 \text{ t/m}^2$$

$$< q_{\text{ca}} = 32.193 \text{ t/m}^2$$

$$q_{\min} = 26.456 / 10.5 \times (1 - 6 \times 0.449/10.5) = 1.873 \text{ t/m}^2$$

$$< q_{\text{ca}} = 40.593 \text{ t/m}^2$$

5.1.2.2 Approach Wall

Design Condition

(a) Hydraulic Condition

(i) Normal Condition

- No water in the river
- Ground water level 1.0 m above bottom level

(ii) Seismic Condition

- No water in the river
- Ground water level 1.0 m above bottom level
- $kh = 0.12$

(b) The Material Data

(i) Soil Material

Wet unit weight	$\gamma_t = 1.6 \text{ t/m}^3$
Saturated unit weight	$\gamma_s = 1.8 \text{ t/m}^3$
Submerged unit weight	$\gamma'_s = 0.8 \text{ t/m}^3$
Internal friction angle	$\phi = 27^\circ$
Cohesion	$c = 0.0 \text{ t/m}^2$

(ii) Others

Unit weight of R.C.	$\gamma_c = 2.50 \text{ t/m}^3$
Unit weight of mass concrete	$\gamma'_c = 2.35 \text{ t/m}^3$
Unit weight of wet masonry	$\gamma_m = 2.30 \text{ t/m}^3$
Unit weight of gravel	$\gamma_g = 2.00 \text{ t/m}^3$
Allowable compressive strength of concrete (K_{225})	$\bar{\sigma}_b = 75 \text{ kg/m}^2$
Allowable compressive strength of steel (U_{24})	$\bar{\sigma}_s = 1400 \text{ kg/m}^2$
Variable - n	$n = 21$

(c) Design Load

(i) Earth pressure

- Coulomb's formula
- Mean ground surface slope $\alpha=26.56^\circ(=\text{atn}0.5)$
- Angle between backside of wall & vertical plane $\theta=2.86^\circ(=\text{atn}0.05)$
- Friction angle at wall (δ)

		Normal	Seismic
Stability calculation	Soil to soil	ϕ	$\phi/2$
Structural calculation	Soil to concrete	$\phi/3$	0

(ii) Surcharge due to Revetment

$$dh = (t1 \times \gamma m + t2 \times \gamma g) / \gamma s - (t1 + t2) = 0.097 \sim 0.10 \text{ m}$$

(iii) Surcharge due to Apron

$$dh1 = (t3 \times \gamma'c) / \gamma s - t3 = 0.305 \sim 0.3 \text{ m}$$

(d) The Combination of Load

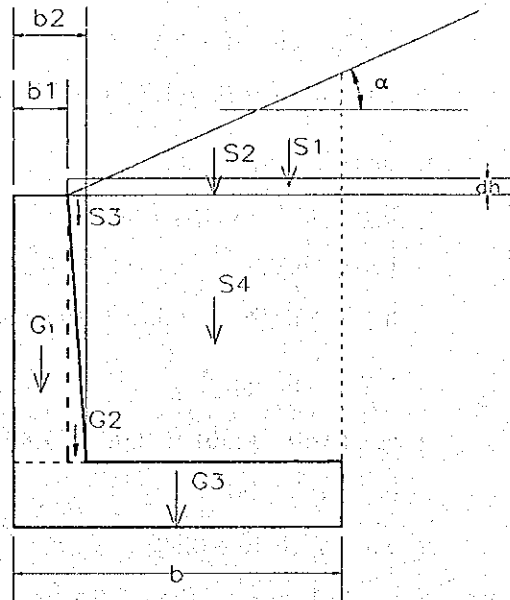
Load		Condition	Normal	Seismic
The vertical load	Weight of main wall		+	+
	Weight of soil		+	+
The horizontal load	Earth pressure		+	+
	Water pressure		+	+
	Horizontal earthquake pressure			+

“+” consider in the calculation

Stability Analysis

(a) Center gravity of Structure

(i) Proposed condition



(ii) Weight of wall body

$$G_1 = b_1 \times h \times \gamma_c = 0.3 \times 2.0 \times 2.50 = 1.500 \text{ t/m}$$

$$x_1 = b_1 / 2 = 0.15 \text{ m}$$

$$y_1 = h_1 + h / 2 = 0.50 + 2.0 / 2 = 1.50 \text{ m}$$

$$G_2 = \frac{1}{2} (b_2 - b_1) \times h \times \gamma_c = \frac{1}{2} (0.4 - 0.3) \times 2.0 \times 2.50 = 0.250 \text{ t/m}$$

$$x_2 = b_1 + (b_2 - b_1) / 3 = 0.3 + (0.4 - 0.3) / 3 = 0.333 \text{ m}$$

$$y_2 = h_1 + h / 3 = 0.50 + 2.0 / 3 = 1.167 \text{ m}$$

$$G_3 = b \times h_1 \times \gamma_c = 1.80 \times 0.50 \times 2.50 = 2.250 \text{ t/m}$$

$$x_3 = b / 2 = 1.80 / 2 = 0.90 \text{ m}$$

$$y_3 = h_1 / 2 = 0.5 / 2 = 0.250 \text{ m}$$

(iii) Weight of soil

$$\begin{aligned} S_1 &= \frac{1}{4} (b-b_1)^2 \times \gamma_s \\ &= \frac{1}{4} \times (1.80 - 0.30)^2 \times 1.80 = 1.013 \text{ t/m} \end{aligned}$$

$$\begin{aligned} x_{S1} &= b_1 + \frac{2}{3} (b - b_1) \\ &= 0.3 + \frac{2}{3} (1.8 - 0.3) = 1.300 \text{ m} \end{aligned}$$

$$\begin{aligned} y_{S1} &= h + h_1 + dh + (b - b_1) / 2 / 3 \\ &= 2.0 + 0.5 + 0.10 + (1.8 - 0.3) / 2 / 3 = 2.850 \text{ m} \end{aligned}$$

$$\begin{aligned} S_2 &= dh \times (b - b_1) \times \gamma_s \\ &= 0.10 \times (1.8 - 0.3) \times 1.8 = 0.270 \text{ t/m} \end{aligned}$$

$$x_{S2} = b_1 + (b - b_1) / 2 = 0.3 + (1.8 - 0.3) / 2 = 1.050 \text{ m}$$

$$y_{S2} = h + h_1 + dh / 2 = 2.50 + 0.10 / 2 = 2.600 \text{ m}$$

$$\begin{aligned} S_3 &= \frac{1}{2} (b_2 - b_1) \times h \times \gamma_s \\ &= \frac{1}{2} \times (0.40 - 0.30) \times 2.00 \times 1.80 = 0.180 \text{ t/m} \end{aligned}$$

$$\begin{aligned} x_{S3} &= b_1 + \frac{2}{3} (b - b_1) \\ &= 0.3 + \frac{2}{3} (0.40 - 0.30) = 0.367 \text{ m} \end{aligned}$$

$$y_{S3} = h_1 + \frac{2}{3} h = 0.5 + 2.0 \times \frac{2}{3} = 1.833 \text{ m}$$

$$\begin{aligned} S_4 &= (b - b_2) \times h \times \gamma_s \\ &= (1.80 - 0.40) \times 2.00 \times 1.80 = 5.040 \text{ t/m} \end{aligned}$$

$$\begin{aligned} x_{S4} &= b_2 + (b - b_2) / 2 \\ &= 0.4 + (1.8 - 0.4) / 2 = 1.100 \text{ m} \end{aligned}$$

$$\begin{aligned} y_{S4} &= h_1 + h / 2 \\ &= 0.5 + 2.00 / 2 = 1.500 \text{ m} \end{aligned}$$

(iv) Buoyant Force / Uplift

$$\begin{aligned} U &= b \times (h + h_1 - z) \times \gamma_w \\ &= 1.8 \times (2.0 + 0.5 - 1.5) \times 1.0 = 1.800 \text{ t/m} \end{aligned}$$

$$x_u = b / 2 = 1.8 / 2 = 0.900 \text{ m}$$

$$\begin{aligned} y_u &= (h + h_1 - z) / 2 \\ &= (2.0 + 0.5 - 1.5) / 2 = 0.500 \text{ m} \end{aligned}$$

(v) Center Gravity of Structure

	Weight, w (t/m)	x (m)	W.x (tm/m)	y (m)	W.y (tm/m)
G ₁	1.500	0.150	0.225	1.500	2.250
G ₂	0.250	0.333	0.083	1.167	0.292
G ₃	2.250	0.900	2.025	0.250	0.563
S ₁	1.012	1.300	1.316	2.850	2.884
S ₂	0.270	1.050	0.284	2.600	0.702
S ₃	0.180	0.367	0.066	1.833	0.330
S ₄	5.040	1.100	5.544	1.500	7.560
U	-1.800	0.900	-1.620	0.500	-0.900
Σ	8.702		7.922		13.680

$$x_o = \Sigma W_x / \Sigma W = 0.910 \text{ m}$$

$$y_o = \Sigma W_y / \Sigma W = 1.572 \text{ m}$$

For without uplift :

$$\Sigma W = 10.502$$

$$\Sigma W_x = 9.543$$

$$\Sigma W_y = 14.581$$

$$x_o' = 0.909 \text{ m}$$

$$y_o' = 1.388 \text{ m}$$

(b) Bearing Capacity Beneath Slab

$$q_u = \alpha \cdot c \cdot k \cdot N_c + k \cdot q \cdot N_q + \frac{1}{2} \cdot \gamma \cdot \beta \cdot B \cdot N_\gamma$$

$$\alpha = \beta = 1.0$$

$$c = 0$$

$$D_f = 1.00 \text{ m}$$

$$k = 1 + 0.3 D_f / B$$

$$= 1 + 0.3 (1.0 / 1.8) = 1.167$$

$$q = D_f \times \gamma'$$

$$\text{For } \phi = 27^\circ ; \theta = 0 ; N_q = 14.0$$

$$N_\gamma = 9.0$$

$$q_u = 1.167 \times (1.0 \times 2.35) \times 14.0 + \frac{1}{2} \times 0.8 \times 1.0 \times 1.8 \times 9.0$$

$$= 44.874 \text{ t/m}^2$$

$$q_a = q_u / 3 = 14,958 \text{ t/m}^2 \quad (\text{in ordinary})$$

$$q_{ea} = q_u / 2 = 22,437 \text{ t/m}^2 \quad (\text{in seismic})$$

(c) Coefficient of Earth Pressure

Applying Coulomb's formula as follows:

(in ordinary)

$$\theta = 2.86^\circ ; \alpha = 26.56^\circ ; \delta = \phi = 27$$

$$K_a = \frac{\cos^2(\phi - \theta)}{\cos^2\theta \cos(\theta + \delta) \left[1 + \sqrt{\frac{\sin(\phi + \delta) \sin(\phi - \alpha)}{\cos(\theta + \delta) \cos(\theta - \alpha)}} \right]^2}$$

$$K_a = \frac{\cos^2(27 - 2.86)}{\cos^2(2.86) \times \cos(2.86 + 27) \left[1 + \sqrt{\frac{\sin(27 + 27) \times \sin(27 - 26.56)}{\cos(2.86 + 27) \times \cos(2.86 - 26.56)}} \right]^2}$$

$$= 0.818$$

$$K_p = \frac{\cos^2(\phi + \theta)}{\cos^2\theta \cos(\theta + \delta) \left[1 - \sqrt{\frac{\sin(\phi - \delta) \times \sin(\phi + \alpha)}{\cos(\theta + \delta) \cos(\theta - \alpha)}} \right]^2}$$

$$K_p = \frac{\cos^2(27 + 2.86)}{\cos^2(2.86) \times \cos(2.86 + 27) \left[1 - \sqrt{\frac{\sin(27 - 27) \times \sin(27 - 26.56)}{\cos(2.86 + 27) \times \cos(2.86 - 26.56)}} \right]^2}$$

$$= 0.869$$

(in seismic)

$$\theta = 6.84^\circ ; \theta_o' = 15.11^\circ$$

$$\delta = \phi/2 = 13.5^\circ ; \theta = 2.86^\circ ; \alpha = 26.56^\circ$$

$$K_{ca} = \frac{\cos^2(\phi - \theta_o - \theta)}{\cos\theta_o \cdot \cos^2\theta \cdot \cos(\theta + \theta_o + \delta) \left[1 + \sqrt{\frac{\sin(\phi + \delta) \sin(\phi - \alpha - \theta_o)}{\cos(\theta + \theta_o + \delta) \cos(\theta - \alpha)}} \right]^2}$$

$$K_{ca} = \frac{\cos^2(27 - 6.84 - 2.86)}{\cos(6.84) \times \cos^2(2.86) \times \cos(2.86 + 6.84 + 13.5) \left[1 + \sqrt{\frac{\sin(27 + 13.5) \times \sin(27 - 26.56 - 6.84)}{\cos(2.86 + 6.84 + 13.5) \times \cos(2.86 - 26.56)}} \right]^2}$$

$$= 1.001$$

$$K_{ca}' = \frac{\cos^2(\phi - \theta'_o - \theta)}{\cos \theta'_o \cdot \cos^2 \theta \cdot \cos(\theta + \theta'_o + \delta) \left[1 + \sqrt{\frac{\sin(\phi + \delta) \sin(\phi - \alpha - \theta'_o)}{\cos(\theta + \theta'_o + \delta) \cos(\theta - \alpha)}} \right]^2}$$

$$K_{ca}' = \frac{\cos^2(27 - 15.11 - 2.86)}{\cos(15.11) \times \cos^2(2.86) \times \cos(2.86 + 15.11 + 13.5) \left[1 + \sqrt{\frac{\sin(27 + 13.5) \times \sin(27 - 26.56 - 15.11)}{\cos(2.86 + 15.11 + 13.5) \times \cos(2.86 - 26.56)}} \right]^2}$$

$$= 1.187$$

$$K_{ep} = \frac{\cos^2(\phi - \theta_o + \theta)}{\cos \theta_o \cdot \cos^2 \theta \cdot \cos(\theta - \theta_o + \delta) \left[1 - \sqrt{\frac{\sin(\phi - \delta) \sin(\phi + \alpha - \theta_o)}{\cos(\theta - \theta_o + \delta) \cos(\theta - \alpha)}} \right]^2}$$

$$K_{ep} = \frac{\cos^2(27 - 6.84 + 2.86)}{\cos(6.84) \times \cos^2(2.86) \times \cos(2.86 - 6.84 + 13.5) \left[1 - \sqrt{\frac{\sin(27 - 13.5) \times \sin(27 + 26.56 - 6.84)}{\cos(2.86 - 6.84 + 13.5) \times \cos(2.86 - 26.56)}} \right]^2}$$

$$= 2.705$$

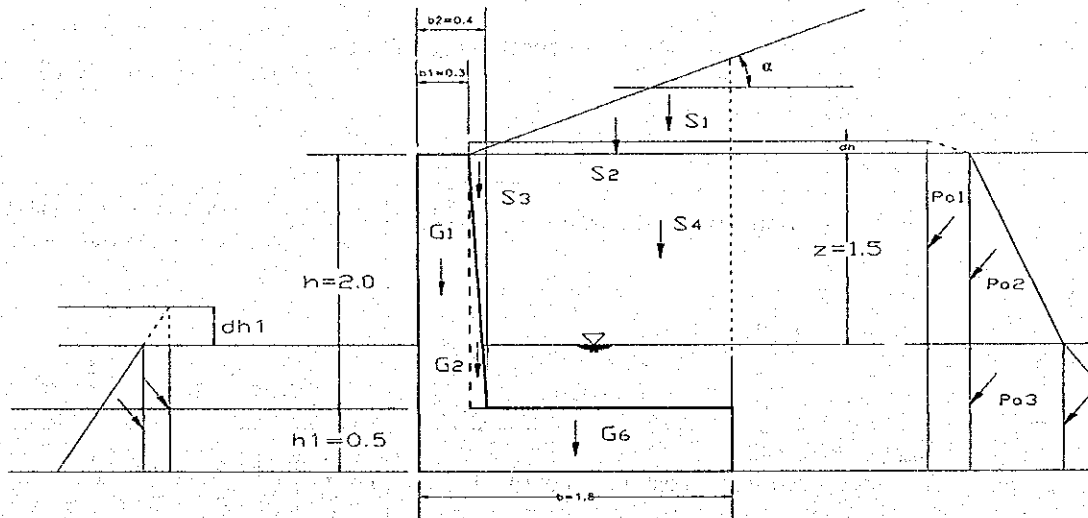
$$K_{ep}' = \frac{\cos^2(\phi - \theta'_o + \theta)}{\cos \theta'_o \cdot \cos^2 \theta \cdot \cos(\theta - \theta'_o + \delta) \left[1 - \sqrt{\frac{\sin(\phi - \delta) \sin(\phi + \alpha - \theta'_o)}{\cos(\theta - \theta'_o + \delta) \cos(\theta - \alpha)}} \right]^2}$$

$$K_{ep}' = \frac{\cos^2(27 - 15.11 + 2.86)}{\cos(15.11) \times \cos^2(2.86) \times \cos(2.86 - 15.11 + 13.5) \left[1 - \sqrt{\frac{\sin(27 - 13.5) \times \sin(27 + 26.56 - 15.11)}{\cos(2.86 - 15.11 + 13.5) \times \cos(2.86 - 26.56)}} \right]^2}$$

$$= 2.682$$

(d) Stability analysis on Normal Condition

(i) Load Condition



(ii) External Force

Active earth pressure :

$$\begin{aligned}
 P_{a1} &= dh \times \gamma_s \times K_a \times (h+h_1) \\
 &= 0.10 \times 1.8 \times 0.818 \times 2.50 = 0.368 \text{ t/m} \\
 P_{a2} &= \frac{1}{2} \times z^2 \times \gamma_s \times K_a \\
 &= \frac{1}{2} \times (1.5)^2 \times 1.8 \times 0.818 = 1.656 \text{ t/m} \\
 P_{a3} &= z \times \gamma_s \times K_a \times (h+h_1-z) \\
 &= 1.5 \times 1.8 \times 0.818 \times 1.0 = 2.209 \text{ t/m} \\
 P_{a4} &= \frac{1}{2} \times (h+h_1-z) \times \gamma'_s \times K_a \\
 &= \frac{1}{2} \times (1.0)^2 \times 0.8 \times 0.818 = 0.327 \text{ t/m}
 \end{aligned}$$

Horizontal Active Earth Pressure

$$\begin{aligned}
 P_{ah1} &= P_{a1} \times \cos(\theta + \delta) \\
 &= 0.368 \times \cos(2.86 + 27) = 0.319 \text{ t/m} \\
 y_{a1} &= (h+h_1)/2 = 2.5/2 = 1.250 \text{ m} \\
 P_{ah2} &= P_{a2} \times \cos(\theta + \delta) \\
 &= 1.656 \times \cos(29.86) = 1.437 \text{ t/m} \\
 y_{a2} &= (h+h_1-z) + z/3 = 1.0 + 1.5/3 = 1.500 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 P_{ah3} &= P_{a3} \times \cos(\theta + \delta) \\
 &= 2.209 \times \cos(29.86) &= 1.915 \text{ t/m} \\
 y_{a3} &= (h + h_1 - z) + z/2 = 1.0 / 2 &= 0.500 \text{ m} \\
 P_{ah4} &= P_{a4} \times \cos(\theta + \delta) \\
 &= 0.327 \times \cos(29.86) &= 0.284 \text{ t/m} \\
 y_{a4} &= (h + h_1 - z) / 3 = 1.0 / 3 &= 0.333 \text{ m}
 \end{aligned}$$

Vertical Active Earth Pressure

$$\begin{aligned}
 P_{av1} &= P_{a1} \times \sin(\theta + \delta) \\
 &= 0.368 \times \sin(29.86) &= 0.183 \text{ t/m} \\
 x_{a1} &= 1.800 \text{ m} \\
 P_{av2} &= P_{a2} \times \sin(\theta + \delta) \\
 &= 1.656 \times \sin(29.86) &= 0.825 \text{ t/m} \\
 x_{a2} &= 1.800 \text{ m} \\
 P_{av3} &= P_{a3} \times \sin(\theta + \delta) \\
 &= 2.209 \times \sin(29.86) &= 1.100 \text{ t/m} \\
 x_{a3} &= 1.800 \text{ m} \\
 P_{av4} &= P_{a4} \times \sin(\theta + \delta) \\
 &= 0.327 \times \sin(29.86) &= 0.163 \text{ t/m} \\
 y_{a4} &= 1.800 \text{ m}
 \end{aligned}$$

Passive earth pressure :

$$\begin{aligned}
 P_{p1} &= dh_1 \times \gamma_s \times K_p \times (h - h_1 - z) \\
 &= 0.30 \times 1.8 \times 0.869 \times 1.0 &= 0.469 \text{ t/m} \\
 P_{p2} &= \frac{1}{2} \times (h - h_1 - z)^2 \times \gamma_s \times K_p \\
 &= \frac{1}{2} \times (1.0)^2 \times 1.8 \times 0.869 &= 0.782 \text{ t/m}
 \end{aligned}$$

Horizontal Passive Earth Pressure

$$\begin{aligned}
 P_{ph1} &= P_{p1} \times \cos(\theta - \delta) \\
 &= 0.469 \times \cos(2.86 - 27) &= 0.201 \text{ t/m} \\
 y_{p1} &= (h + h_1 - z) / 2 &= 0.500 \text{ m} \\
 P_{ph2} &= P_{p2} \times \cos(\theta - \delta) \\
 &= 0.782 \times \cos(24.14) &= 0.714 \text{ t/m} \\
 y_{p2} &= (h + h_1 - z) / 3 &= 0.333 \text{ m}
 \end{aligned}$$

Water Pressure

$$P_{wa} = \frac{1}{2} (h + h_1 - z)^2 \times \gamma_w$$

$$= \frac{1}{2} (1.0)^2 \times 1.0 = 0.500 \text{ t/m}$$

$$y_w = (h + h_1 - z) / 3 = 1.0 / 3 = 0.333 \text{ m}$$

(iii) Vertical Force and Moment

	Vertical Force (t/m)	Arm (m)	Vertical Moment (tm/m)
P_{av1}	0.183	1.800	0.329
P_{av2}	0.825	1.800	1.485
P_{av3}	1.100	1.800	1.980
P_{av4}	0.163	1.800	0.293
w	8.702	0.910	7.919
FV	10.973	MV	12.006

(iv) Horizontal Force and Moment

	Horizontal Force (t/m)	Arm (m)	Horizontal Moment (tm/m)
P_{ah1}	0.319	1.250	0.399
P_{ah2}	1.437	1.500	2.156
P_{ah1}	1.915	0.500	0.958
P_{ah2}	0.284	0.333	0.095
P_{wa}	0.500	0.167	0.084
P_{ph1}	-0.201	0.500	-0.101
P_{ph2}	-0.714	0.333	-0.238
FH	3.540	MH	3.353

(v) Check of stability

Stability against sliding

$$SF = FV / FH \cdot \tan \phi$$

$$= 10.973 / 3.540 \times \tan 27 = 1.565$$

$$> 1.5$$

Stability against overturning

$$e = b/2 - (MV - MH) / FV$$

$$= 1.8/2 - (12.006 - 3.353) / 10.973 = 0.111 (-)$$

$$< B/6 (=0.30 \text{ m})$$

Stability against bearing strata

$$q = FV/b (1 \pm 6 e / L)$$

$$q_{\max} = 10.973 / 1.8 \times (1 + 6 \times 0.111 / 1.8) = 8.352 \text{ t/m}^2$$

$$< q_t = 14.958 \text{ t/m}^2$$

(e) Stability analysis on Seismic Condition

(i) External Force

Active earth pressure :

$$\begin{aligned} P_{ea1} &= dh \times \gamma_s \times K_{ea} \times (h+h_1) \\ &= 0.10 \times 1.8 \times 1.001 \times 2.50 &= 0.450 \text{ t/m} \end{aligned}$$

$$\begin{aligned} P_{ea2} &= \frac{1}{2} \times z^2 \times \gamma_s \times K_{ea} \\ &= \frac{1}{2} \times (1.5)^2 \times 1.8 \times 1.001 &= 2.027 \text{ t/m} \end{aligned}$$

$$\begin{aligned} P_{ea3} &= z \times \gamma_s \times K_{ea} \times (h + h_1 - z) \\ &= 1.5 \times 1.8 \times 1.001 \times 1.0 &= 2.703 \text{ t/m} \end{aligned}$$

$$\begin{aligned} P_{ea4} &= \frac{1}{2} \times (h + h_1 - z) \times \gamma'_s \times K_{ea} \\ &= \frac{1}{2} \times (1.0)^2 \times 0.8 \times 1.187 &= 0.475 \text{ t/m} \end{aligned}$$

Horizontal Active Earth Pressure

$$\begin{aligned} P_{eah1} &= P_{ea1} \times \cos(\theta + \delta) \\ &= 0.450 \times \cos(2.86 + 13.5) &= 0.432 \text{ t/m} \end{aligned}$$

$$y_{ea1} = 1.250 \text{ m}$$

$$\begin{aligned} P_{eah2} &= P_{ea2} \times \cos(\theta + \delta) \\ &= 2.027 \times \cos(16.36) &= 1.945 \text{ t/m} \end{aligned}$$

$$y_{ea2} = 1.000 \text{ m}$$

$$\begin{aligned} P_{eah3} &= P_{ea3} \times \cos(\theta + \delta) \\ &= 2.703 \times \cos(16.36) &= 2.593 \text{ t/m} \end{aligned}$$

$$y_{ea3} = 0.500 \text{ m}$$

$$\begin{aligned} P_{eah4} &= P_{ea4} \times \cos(\theta + \delta) \\ &= 0.475 \times \cos(16.36) &= 0.455 \text{ t/m} \end{aligned}$$

$$y_{ea4} = 0.333 \text{ m}$$

Vertical Active Earth Pressure

$$\begin{aligned} P_{eav1} &= P_{ea1} \times \sin(\theta + \delta) \\ &= 0.450 \times \sin(16.36) &= 0.127 \text{ t/m} \end{aligned}$$

$$x_{ea1} = 1.800 \text{ m}$$

$$P_{ea2} = P_{ca2} \times \sin(\theta + \delta)$$

$$= 2.027 \times \sin(16.36) = 0.571 \text{ t/m}$$

$$x_{ea2} = 1.800 \text{ m}$$

$$P_{ca3} = P_{ca3} \times \sin(\theta + \delta)$$

$$= 2.703 \times \sin(16.36) = 0.761 \text{ t/m}$$

$$x_{ca3} = 1.800 \text{ m}$$

$$P_{ca4} = P_{ca4} \times \sin(\theta + \delta)$$

$$= 0.475 \times \sin(16.36) = 0.134 \text{ t/m}$$

$$y_{ca4} = 1.800 \text{ m}$$

Passive earth pressure :

$$P_{ep1} = dh_1 \times \gamma_s \times K_{ep} \times (h + h_1 - z)$$

$$= 0.30 \times 1.8 \times 2.705 \times 1.0 = 1.461 \text{ t/m}$$

$$P_{ep2} = \frac{1}{2} \times (h + h_1 - z)^2 \times \gamma_s \times K_{ep}$$

$$= \frac{1}{2} \times (1.0)^2 \times 1.8 \times 2.705 = 2.455 \text{ t/m}$$

Horizontal Passive Earth Pressure

$$P_{eph1} = P_{ep1} \times \cos(\theta - \delta)$$

$$= 1.461 \times \cos(2.86 - 13.5) = 1.436 \text{ t/m}$$

$$y_{ep1} = 0.500 \text{ m}$$

$$P_{eph2} = P_{ep2} \times \cos(\theta - \delta)$$

$$= 2.435 \times \cos(10.64) = 2.393 \text{ t/m}$$

$$y_{ep2} = 0.333 \text{ m}$$

Water Pressure

$$P_{wa} = \frac{1}{2} (h + h_1 - z)^2 \times \gamma_w$$

$$= \frac{1}{2} \times (1.0)^2 \times 1.0 = 0.500 \text{ t/m}$$

$$y_w = (h + h_1 - z) / 3 = 1.0 / 3 = 0.333 \text{ m}$$

Earthquake Force

$$W_e = W \times kh$$

$$= 10.502 \times 0.12$$

$$= 1.260 \text{ t/m}$$

$$y_e = 1.388 \text{ m}$$

(ii) Vertical Force and Moment

Vertical Force (t/m)		Arm (m)	Vertical Moment (tm/m)
Peav ₁	0.127	1.800	0.229
Peav ₂	0.571	1.800	1.028
Peav ₃	0.761	1.800	1.370
Peav ₄	0.134	1.800	0.241
W	8.702	0.910	7.919
FV _e	10.295	MV _e	10.787

(iii) Horizontal Force and Moment

Horizontal Force (t/m)		Arm (m)	Horizontal Moment (tm/m)
Peah ₁	0.432	1.250	0.540
Peah ₂	1.945	1.000	1.945
Peah ₃	2.593	0.500	1.297
Peah ₄	0.455	0.333	0.152
P _w	0.500	0.333	0.167
Peph ₁	-1.436	0.500	-0.718
Peph ₂	-2.393	0.333	-0.797
W _e	1.260	1.388	1.749
FH	3.356	MH _e	4.335

(iv) Check of stability

Stability against sliding

$$\begin{aligned} SF &= FV_e / FH_e \cdot \tan \phi \\ &= 10.295 / 3.356 \times \tan 27 &= 1.561 \\ &> 1.2 \end{aligned}$$

Stability against overturning

$$\begin{aligned} e &= b/2 - (MV_e - MH_e) / FV_e \\ &= 1.8/2 - (10.787 - 4.335) / 10.295 &= 0.273 \\ &< B/3 (=0.60 \text{ m}) \end{aligned}$$

Stability of bearing strata

$$\begin{aligned} q &= FV_e / b (1 \pm 6 e / b) \\ q_{\max} &= 10.787 / 1.8 \times (1 + 6 \times 0.273 / 1.8) &= 11.446 \text{ t/m}^2 \\ &< q_{\text{sa}} = 22.437 \text{ t/m} \end{aligned}$$

(3) Stress Strain Analysis

(a) Coefficient of Active Earth Pressure

Applying Coulomb's formula as follows:

(in ordinary)

$$\theta = 2.86^\circ ; \alpha = 26.56^\circ ; \delta = \phi/3 = 9^\circ$$

$$K_a = \frac{\cos^2(\phi - \theta)}{\cos^2\theta \cos(\phi + \delta) \left[1 + \sqrt{\frac{\sin(\phi + \delta) \sin(\phi - \alpha)}{\cos(\theta + \delta) \cos(\theta - \alpha)}} \right]^2}$$

$$K_a = \frac{\cos^2(27 - 2.86)}{\cos^2(2.86) \times \cos(2.86 + 9) \left[1 + \sqrt{\frac{\sin(27 + 9) \sin(27 - 26.56)}{\cos(2.86 + 9) \times \cos(2.86 - 26.56)}} \right]^2}$$

$$= 0.744$$

(in seismic)

$$\theta = 6.84^\circ ; \theta'_o = 15.11^\circ ; \theta = 2.86^\circ ; \alpha = 26.56^\circ ; \delta = 0$$

$$K_{ca} = \frac{\cos^2(\phi - \theta_o - \theta)}{\cos\theta_o \cdot \cos^2\theta \cdot \cos(\theta + \theta_o + \delta) \left[1 + \sqrt{\frac{\sin(\phi + \delta) \sin(\phi - \alpha - \theta_o)}{\cos(\theta + \theta_o + \delta) \cos(\theta - \alpha)}} \right]^2}$$

$$K_{ca} = \frac{\cos^2(27 - 6.84 - 2.86)}{\cos(6.84) \times \cos^2(2.86) \times \cos(2.86 + 6.84 + 0) \left[1 + \sqrt{\frac{\sin(27 + 0) \times \sin(27 - 26.56 - 6.84)}{\cos(2.86 + 6.84 + 0) \times \cos(2.86 - 26.56)}} \right]^2}$$

$$= 0.934$$

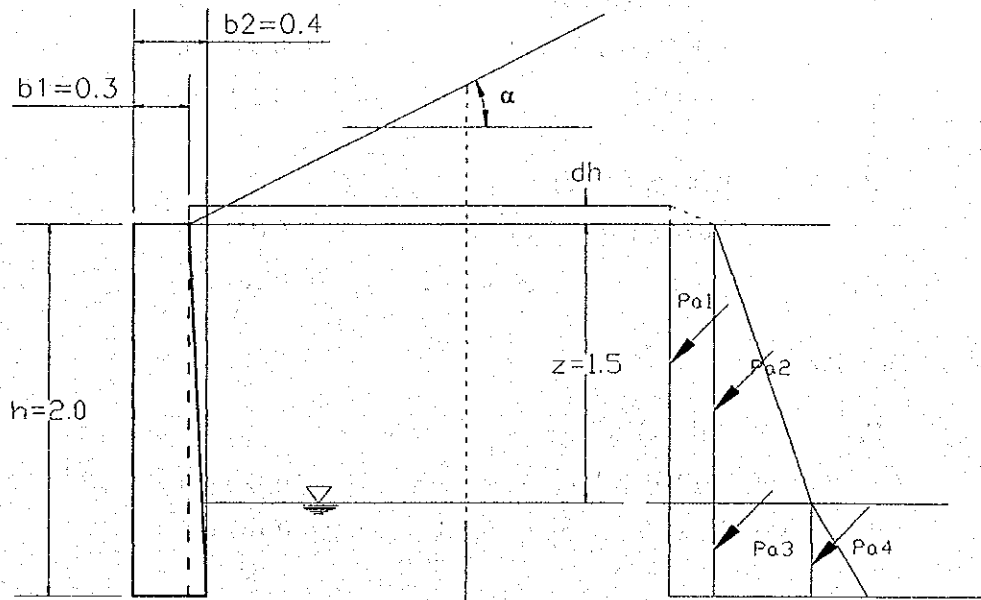
$$K_{ca}' = \frac{\cos^2(\phi - \theta'_o - \theta)}{\cos\theta'_o \cdot \cos^2\theta \cdot \cos(\theta + \theta'_o + \delta) \left[1 + \sqrt{\frac{\sin(\phi + \delta) \sin(\phi - \alpha - \theta'_o)}{\cos(\theta + \theta'_o + \delta) \cos(\theta - \alpha)}} \right]^2}$$

$$K_{ca}' = \frac{\cos^2(27 - 5.11 - 2.86)}{\cos(15.11) \times \cos^2(2.86) \times \cos(2.86 + 15.11) \left[1 + \sqrt{\frac{\sin(27) \times \sin(27 - 26.56 - 15.11)}{\cos(2.86 + 15.11) \times \cos(2.86 - 26.56)}} \right]^2}$$

$$= 1.065$$

(b) Wall

(i) Load Condition



(ii) External Force and Moment

(in ordinary)

Earth pressure :

$$\begin{aligned} P_{a1} &= dh \times \gamma_s \times K_a \times h \\ &= 0.10 \times 1.8 \times 0.744 \times 2.0 = 0.268 \text{ t/m} \end{aligned}$$

$$\begin{aligned} P_{a2} &= \frac{1}{2} \times z^2 \times \gamma_s \times K_a \\ &= \frac{1}{2} \times (1.5)^2 \times 1.8 \times 0.744 = 1.507 \text{ t/m} \end{aligned}$$

$$\begin{aligned} P_{a3} &= z \times \gamma_s \times K_a \times (h - z) \\ &= 1.5 \times 1.8 \times 0.744 \times 0.5 = 1.004 \text{ t/m} \end{aligned}$$

$$\begin{aligned} P_{a4} &= \frac{1}{2} \times (h - z)^2 \times \gamma'_s \times K_a \\ &= \frac{1}{2} \times (0.5)^2 \times 0.8 \times 0.744 = 0.074 \text{ t/m} \end{aligned}$$

Horizontal Earth Pressure

$$\begin{aligned} P_{ah1} &= P_{a1} \times \cos(\theta + \delta) \\ &= 0.268 \times \cos(2.86 + 9) = 0.262 \text{ t/m} \end{aligned}$$

$$y_{a1} = h / 2 = 1.000 \text{ m}$$

$$P_{ah2} = P_{a2} \times \cos(\theta + \delta)$$

$$= 1.507 \times \cos(11.86) = 1.474 \text{ t/m}$$

$$y_{a2} = (h - z) + z/3 = 0.5 + 1.5/3 = 1.000 \text{ m}$$

$$P_{ah3} = P_{a3} \times \cos(\theta + \delta)$$

$$= 1.004 \times \cos(11.86) = 0.983 \text{ t/m}$$

$$y_{a3} = (h - z)/2 = 0.5/2 = 0.250 \text{ m}$$

$$P_{ah4} = P_{a4} \times \cos(\theta + \delta)$$

$$= 0.074 \times \cos(11.86) = 0.073 \text{ t/m}$$

$$y_{a4} = (h - z)/3 = 0.5/3 = 0.167 \text{ m}$$

Water Pressure

$$P_w = \frac{1}{2} (h - z)^2 \times \gamma_w$$

$$= \frac{1}{2} (0.5)^2 \times 1.0 = 0.125 \text{ t/m}$$

$$y_w = (h - z)/3 = 0.5/3 = 0.167 \text{ m}$$

Horizontal Force and Moment

Horizontal Force (t/m)	Arm (m)	Horizontal Moment (tm/m)	
P _{ah1}	0.262	1.000	0.262
P _{ah2}	1.474	1.000	1.474
P _{ah3}	0.983	0.250	0.246
P _{ah4}	0.073	0.167	0.012
P _w	0.125	0.167	0.021
FH	2.917	MH	2.015

(in seismic)

Earth pressure :

$$P_{e1} = dh \times \gamma_s \times K_{ea} \times h$$

$$= 0.10 \times 1.8 \times 0.934 \times 2.0 = 0.336 \text{ t/m}$$

$$P_{e2} = \frac{1}{2} \times z^2 \times \gamma_s \times K_{ea}$$

$$= \frac{1}{2} \times (1.5)^2 \times 1.8 \times 0.934 = 1.891 \text{ t/m}$$

$$P_{e3} = z \times \gamma_s \times K_{ea} \times (h - z)$$

$$= 1.5 \times 1.8 \times 0.934 \times 0.5 = 1.261 \text{ t/m}$$

$$P_{e4} = \frac{1}{2} \times (h - z)^2 \times \gamma'_s \times K_{ea}$$

$$= \frac{1}{2} \times (0.5)^2 \times 0.8 \times 1.065 = 0.107 \text{ t/m}$$

Horizontal Earth Pressure

$$P_{eah1} = P_{ea1} \times \cos(\theta + \delta) = 0.336 \times \cos(2.86) = 0.336 \text{ t/m}$$

$$y_{ea1} = 1.000 \text{ m}$$

$$P_{eah2} = P_{ea2} \times \cos(\theta + \delta) = 1.891 \times \cos(2.86) = 1.889 \text{ t/m}$$

$$y_{ea2} = 1.000 \text{ m}$$

$$P_{eah3} = P_{ea3} \times \cos(\theta + \delta) = 1.261 \times \cos(2.86) = 1.259 \text{ t/m}$$

$$y_{ea3} = 0.250 \text{ m}$$

$$P_{eah4} = P_{ea4} \times \cos(\theta + \delta) = 0.107 \times \cos(2.86) = 0.106 \text{ t/m}$$

$$y_{ea4} = 0.167 \text{ m}$$

Water Pressure

$$P_w = \frac{1}{2} (h - z)^2 \times \gamma_w = \frac{1}{2} (0.5)^2 \times 1.0 = 0.125 \text{ t/m}$$

$$y_w = (h - z)/3 = 0.5/3 = 0.167 \text{ m}$$

Horizontal Force and Moment

Horizontal Force (t/m)		Arm (m)	Horizontal Moment (tm/m)
Peah1	0.336	1.000	0.336
Peah2	1.889	1.000	1.889
Peah3	1.259	0.250	0.315
Peah4	0.106	0.167	0.018
Pw	0.125	0.167	0.021
FH	3.715	MH	2.579

(iii) Bending Moment and Shear Force

$$FH = 2.917$$

$$MH = 2.015$$

$$FH_c = 3.715 < 1.5 FH$$

$$MH_c = 2.579 < 1.5 MH$$

Therefore bending moment and shear force in normal condition will be adopted for strain stress calculation.

(iv) Required Re-Bar

$$h_t = 40 \text{ cm}; \quad d = 5 \text{ cm}; \quad h = 35 \text{ cm}$$

$$\begin{aligned} \phi_o &= \sigma_s / n \sigma_b \\ &= 1400 / (21 \times 25) = 0.889 \end{aligned}$$

$$\begin{aligned} C_a &= \frac{h}{\sqrt{\frac{n \times M}{b \times \sigma_a}}} \\ &= \frac{35}{\sqrt{\frac{21 \times 201500}{100 \times 1400}}} \\ &= 6.366 \end{aligned}$$

$$\text{For } C_a = 6.366$$

$$\delta = 0.2$$

$$\phi = 3.930$$

$$\phi' = 7.754$$

$$n_o = 0.0265$$

Stresses:

$$\sigma_s = \bar{\sigma}_a = 1400 \text{ kg/cm}^2$$

$$\sigma'_b = \frac{\bar{\sigma}_a}{n\phi} = \frac{1400}{21 \times 3.93} = 16.96 \text{ kg/cm}^2$$

$$\sigma'_s = \frac{\bar{\sigma}_a}{\phi'} = \frac{1400}{7.754} = 180.552 \text{ kg/cm}^2$$

Re-bar will be arranged

$$A = \omega b h$$

$$= 0.0265 / 21 \times 100 \times 35 = 4.417 \text{ cm}^2$$

$$A_s = 0.2 \times A = 0.883 \text{ cm}^2$$

$$A' = \delta \cdot A = 0.883 \text{ cm}^2$$

$$A'_s = 0.2 \times A' = 0.176 \text{ cm}^2$$

$$\text{Re-bar : } D_{13-25} , \quad A = 5.32 \text{ cm}^2$$

$$D_{13-25} , \quad A_s = 5.32 \text{ cm}^2$$

(c) Slab

(i) Load Condition

See sketch of load condition for stability analysis.

(ii) Reaction beneath slab

(in ordinary)

Active earth pressure :

$$\begin{aligned} P_{a1} &= dh \times \gamma_s \times K_a \times (h+h_1) \\ &= 0.10 \times 1.8 \times 0.744 \times 2.50 = 0.335 \text{ t/m} \end{aligned}$$

$$\begin{aligned} P_{a2} &= \frac{1}{2} \times z^2 \times \gamma_s \times K_a \\ &= \frac{1}{2} \times (1.5)^2 \times 1.8 \times 0.744 = 1.507 \text{ t/m} \end{aligned}$$

$$\begin{aligned} P_{a3} &= z \times \gamma_s \times K_a \times (h+h_1-z) \\ &= 1.5 \times 1.8 \times 0.744 \times 1.0 = 2.009 \text{ t/m} \end{aligned}$$

$$\begin{aligned} P_{a4} &= \frac{1}{2} \times (h+h_1-z) \times \gamma_s \times K_a \\ &= \frac{1}{2} \times (1.0)^2 \times 0.8 \times 0.744 = 0.298 \text{ t/m} \end{aligned}$$

Horizontal Active Earth Pressure

$$\begin{aligned} P_{ah1} &= P_{a1} \times \cos(\theta + \delta) \\ &= 0.335 \times \cos(11.86) = 0.328 \text{ t/m} \end{aligned}$$

$$\begin{aligned} P_{ah2} &= P_{a2} \times \cos(\theta + \delta) \\ &= 1.507 \times \cos(11.86) = 1.474 \text{ t/m} \end{aligned}$$

$$\begin{aligned} P_{ah3} &= P_{a3} \times \cos(\theta + \delta) \\ &= 2.009 \times \cos(11.86) = 1.966 \text{ t/m} \end{aligned}$$

$$\begin{aligned} P_{ah4} &= P_{a4} \times \cos(\theta + \delta) \\ &= 0.298 \times \cos(11.86) = 0.291 \text{ t/m} \end{aligned}$$

Vertical Active Earth Pressure

$$\begin{aligned}P_{av1} &= P_{a1} \times \sin(\theta + \delta) \\ &= 0.335 \times \sin(11.86) &= 0.069 \text{ t/m} \\ P_{av2} &= P_{a2} \times \sin(\theta + \delta) \\ &= 1.507 \times \sin(11.86) &= 0.310 \text{ t/m} \\ P_{av3} &= P_{a3} \times \sin(\theta + \delta) \\ &= 2.009 \times \sin(11.86) &= 0.413 \text{ t/m} \\ P_{av4} &= P_{a4} \times \sin(\theta + \delta) \\ &= 0.298 \times \sin(11.86) &= 0.061 \text{ t/m}\end{aligned}$$

(in seismic)

$$\begin{aligned}P_{ca1} &= dh \times \gamma_s \times K_{ca} \times (h+h_1) \\ &= 0.10 \times 1.8 \times 0.934 \times 2.50 &= 0.420 \text{ t/m} \\ P_{ca2} &= \frac{1}{2} \times z^2 \times \gamma_s \times K_{ca} \\ &= \frac{1}{2} \times (1.5)^2 \times 1.8 \times 0.934 &= 1.891 \text{ t/m} \\ P_{ca3} &= z \times \gamma_s \times K_{ca} \times (h + h_1 - z) \\ &= 1.5 \times 1.8 \times 0.934 \times 1.0 &= 2.522 \text{ t/m} \\ P_{ca4} &= \frac{1}{2} \times (h + h_1 - z) \times \gamma_s \times K_{ca} \\ &= \frac{1}{2} \times (1.0)^2 \times 0.8 \times 1.065 &= 0.426 \text{ t/m}\end{aligned}$$

Horizontal Active Earth Pressure

$$\begin{aligned}P_{cah1} &= P_{ca1} \times \cos(\theta + \delta) \\ &= 0.420 \times \cos(2.86) &= 0.420 \text{ t/m} \\ P_{cah2} &= P_{ca2} \times \cos(\theta + \delta) \\ &= 1.891 \times \cos(2.86) &= 1.889 \text{ t/m} \\ P_{cah3} &= P_{ca3} \times \cos(\theta + \delta) \\ &= 2.522 \times \cos(2.86) &= 2.519 \text{ t/m} \\ P_{cah4} &= P_{ca4} \times \cos(\theta + \delta) \\ &= 0.426 \times \cos(2.86) &= 0.425 \text{ t/m}\end{aligned}$$

Vertical Active Earth Pressure

$$P_{cav1} = P_{ca1} \times \sin(\theta + \delta)$$

$$= 0.420 \times \sin(2.86) = 0.021 \text{ t/m}$$

$$P_{cav2} = P_{ca2} \times \sin(\theta + \delta)$$

$$= 1.891 \times \sin(2.86) = 0.094 \text{ t/m}$$

$$P_{cav3} = P_{ca3} \times \sin(\theta + \delta)$$

$$= 2.522 \times \sin(2.86) = 0.126 \text{ t/m}$$

$$P_{cav4} = P_{ca4} \times \sin(\theta + \delta)$$

$$= 0.426 \times \sin(2.86) = 0.021 \text{ t/m}$$

Water Pressure

$$P_{wa} = \frac{1}{2} (h + h_1 - z)^2 \times \gamma_w$$

$$= \frac{1}{2} (1.0)^2 \times 1.0 = 0.500 \text{ t/m}$$

Earthquake Force

$$W_e = W \times kh$$

$$= 10.502 \times 0.12$$

$$= 1.260 \text{ t/m}$$

$$y_e = 1.388 \text{ m}$$

Vertical Force and Moment

(in ordinary)

	Vertical Force (t/m)	Arm (m)	Vertical Moment (tm/m)
W	8.702	0.910	7.919
P _{av1}	0.069	1.800	0.124
P _{av2}	0.310	1.800	0.558
P _{av3}	0.413	1.800	0.743
P _{av4}	0.061	1.800	0.110
FV	9.555	MV	9.454

(in seismic)

Vertical Force (t/m)	Arm (m)	Vertical Moment (tm/m)
W	8.702	7.919
P _{eav1}	0.021	1.800
P _{eav2}	0.094	1.800
P _{eav3}	0.126	1.800
P _{eav4}	0.021	1.800
FVe	8.964	MVe
		8.391

Horizontal Force and Moment

(in ordinary)

Horizontal Force (t/m)	Arm (m)	Horizontal Moment (tm/m)
P _{ah1}	0.328	1.250
P _{ah2}	1.474	1.500
P _{ah3}	1.966	0.500
P _{ah4}	0.291	0.333
P _w	0.500	0.167
FH	4.559	MH
		3.785

(in seismic)

Horizontal Force (t/m)	Arm (m)	Horizontal Moment (tm/m)
P _{eah1}	0.420	1.250
P _{eah2}	1.889	1.500
P _{eah3}	2.519	0.500
P _{eah4}	0.425	0.333
P _w	0.500	0.167
W _e	1.260	1.388
FH _e	7.013	MH _e
		6.594

Reaction beneath Slab.

$$FV = 9.555$$

$$MV = 9.454$$

$$FV_e = 8.964 < 1.5 FV$$

$$MV_e = 8.391 < 1.5 MV$$

Therefore, force and moment in normal condition will be adopted on the estimation of Reaction Beneath Slab and Stress Strain analysis.

Reaction beneath slab will be estimated as follows:

$$\begin{aligned}
 e &= b/2 - (MV - MH) / FV \\
 &= 1.8/2 - (9.454 - 8.391) / 9.555 \\
 &= 0.30 \text{ m} \\
 &= b/6
 \end{aligned}$$

$$q = FV / b \times (1 \pm 6e/b)$$

$$\begin{aligned}
 q_{\max} &= 2 FV/b \\
 &= 2 \times 9.555 / 1.8 \\
 &= 10.617 \text{ t/m}^2
 \end{aligned}$$

$$q_{\min} = 0$$

(iii) Shearing Force and Moment

$$\begin{aligned}
 q_1 &= 0.5 \times \gamma_c + (h + dh) \times \gamma_s - (h + h_1 - z) \times \gamma_w \\
 &= 0.5 \times 2.5 + 2.10 \times 1.8 - 1.0 \times 1.0 \\
 &= 4.030 \text{ t/m}^2
 \end{aligned}$$

$$\begin{aligned}
 q_2 &= q_1 + (b - b_1) / 2 \times \gamma_s \\
 &= 4.03 + 0.75 \times 1.8 \\
 &= 5.380 \text{ t/m}^2
 \end{aligned}$$

$$\begin{aligned}
 q &= q_2 - 0.931x - q_{\min} - 5.898x \\
 &= 5.380 - 0.921x - 0 - 5.898x \\
 &= 5.380 - 6.829x
 \end{aligned}$$

$$\begin{aligned}
 v &= \int q (dx) \\
 &= \int_0^{x=1.45} (5.380 - 6.829x) dx \\
 &= \left[5.380x - 6.829 \frac{x^2}{2} \right]_0^{1.45} \\
 &= 0.622 \text{ t/m}
 \end{aligned}$$

$$\begin{aligned}
 M &= \int v(dx) \\
 &= \int_0^{x=1.45} (5.380x - 6.829 \frac{x^2}{2}) dx \\
 &= 5.380 \frac{x^2}{2} - 6.829 \frac{x^3}{6} \Big|_0^{1.45} \\
 &= 2.186 \text{ t.m/m}
 \end{aligned}$$

(iv) Required Re-bar

$$ht = 50 \text{ cm}; \quad d = 5 \text{ cm}; \quad h = 45 \text{ cm}$$

$$\begin{aligned}
 \phi_o &= \sigma / n \sigma_b \\
 &= 1400 / (21 \times 25) = 0.889
 \end{aligned}$$

$$\begin{aligned}
 C_a &= \frac{h}{\sqrt{\frac{n \times M}{b \times \sigma_a}}} \\
 &= \frac{45}{\sqrt{\frac{21 \times 218600}{100 \times 1400}}} \\
 &= 7.859
 \end{aligned}$$

$$\text{For } C_a = 7.859$$

$$\delta = 0.60$$

$$\phi = 5.050$$

$$\phi' = 12.790$$

$$n_o = 0.0172$$

Stresses:

$$\sigma_o = \bar{\sigma}_a = 1400 \text{ kg/cm}^2$$

$$\sigma'_b = \frac{\bar{\sigma}_a}{n\phi} = \frac{1400}{21 \times 5.05} = 13.201 \text{ kg/cm}^2$$

$$\sigma'_a = \frac{\bar{\sigma}_a}{\phi'} = \frac{1400}{12.790} = 109.46 \text{ kg/cm}^2$$

Re-bar will be arranged

$$A = \omega b h$$

$$= 0.0172 / 21 \times 100 \times 45 = 3.686 \text{ cm}^2$$

$$A_s = 0.2 \times A = 0.737 \text{ cm}^2$$

$$A' = \delta \cdot A = 2.211 \text{ cm}^2$$

$$A'_s = 0.2 \times A' = 0.442 \text{ cm}^2$$

Re-bar : D₁₃₋₂₅ , A = 5.32 cm²

D₁₃₋₂₅ , A_s = 5.32 cm²



5.2 Ground Sill without Head at WF 173

Location and Purpose

The following ground sill is proposed in the river improvement plan.

It is anticipated that riverbed degradation of Garang River channel downstream from the confluence with Kreo River arises after the completion of Jatibarang Dam. Accordingly, the existing structures constructed in the channel may be affected. For this reason, a ground sill aiming at protecting the pier foundation of Toll Road Bridge from riverbed/river bank encroachment is proposed at the immediate downstream portion of about 100 m from the bridge.

Structural Type

On the other hand, the ground sill (WF 173) consists of main sill body made of wet masonry and mounded gabion mattress placed on the upstream and downstream riverbeds. This type of ground sill is flexible to conform the riverbed variations.

The design of ground sills is made to ensure structural stability against sliding, overturning and bearing capacity of the sub-base ground, and to satisfy hydraulic stability against piping, uplift and scouring.

Structural Dimension etc.

(a) River Channel

Riverbed width		40.0 m
Side slope	(m)	2.0
Riverbed Slope	(I)	$1/1250$
Design Riverbed elevation		EL. + 5.793 m
Existing Lowest riverbed elevation		EL. + 5.030 m

(b) Main Sill Body

Height	(H)	2.0 m
Crown width	(B1)	1.5 m
Bottom width	(B)	2.5 m

(c) Side Wall

Height	(h)	2.5 m
Crown width	(b1)	0.5 m
Bottom width	(b)	1.2 m
Length		26.5 m

(d) Revetment

Length	Upstream	10.0 m
	Main structure	1.5 m
	Downstream	15.0 m

(e) Riverbed Protection

Upstream length	12.0 m
Downstream length	15.0 m
Thickness	0.5 m

5.2.1 Structural Design of Side Wall

Design Condition

(a) Hydraulic Condition

(i) Normal Condition

Water elevation	EL + 5.293
Water Depth	z = 0.30 m
Ground Water Table	EL + 5.593

(ii) Seismic Condition

Water elevation	EL + 5.293
Water Depth	z = 0.30 m
Ground Water Table	EL + 5.593

(b) The Material Data

(i) Soil Material^{*)}

Wet unit weight	$\gamma_t = 1.800 \text{ t/m}^3$
Saturated unit weight	$\gamma_s = 1.955 \text{ t/m}^3$
Submerged unit weight	$\gamma'_t = 0.955 \text{ t/m}^3$
Internal friction angle	$\phi = 42^\circ$

^{*)} Based on geological investigation on RB 47 and RB 48 (Location WF 173) Soil layer at el. 3.00 m to el. 7.00 m are silty gravelly sand, fine to very coarse grained with N-value of about N = 50 and $\gamma_{sat} = 1.955 \text{ t/m}^3$. Soil internal friction angle will be estimated based on N-value as follows $\phi = 15 + \sqrt{15 \cdot N} = 42.38 \sim 42^\circ$.

Cohesion	$C = 0.0 \text{ t/m}^3$
----------	-------------------------

(ii) Others

Unit weight of wet masonry	$\gamma_m = 2.30 \text{ t/m}^3$
Unit weight of gabion mattress / cobbles	$\gamma_{gm} = 2.20 \text{ t/m}^3$
Unit weight of gravel	$\gamma_g = 2.00 \text{ t/m}^3$
Unit weight of water	$\gamma_w = 1.00 \text{ t/m}^3$

(c) Design Load

(i) Earth Pressure

- Coulomb's formula
- Mean ground surface slope, $\alpha = 26.56^\circ$ (=atn 0.5)
- Angle between backside of wall & vertical plane, $\theta = 13.50^\circ$
(=atn 0.6/2.5)
- Friction angle at wall (δ)
 - Normal $\delta = \phi$
 - Seismic $\delta = \phi/2$
- Horizontal seismic coefficient $K_h = 0.12$

(ii) Surcharge due to revetment

$$dh = (t_1 \times \gamma_m + t_2 \times \gamma_g) / \gamma_t - (t_1 + t_2)$$

$$= (0.25 \times 2.3 + 0.25 \times 2.0) / 1.8 - 0.5 = 0.10 \text{ m}$$

(iii) Surcharge due to gabion mattress (submerged)

$$dh_1 = (t \times \gamma'_{gm}) / \gamma'_s - t$$

$$= (0.50 \times 1.20) / 0.955 - 0.5 = 0.13 \text{ m}$$

(d) The Combination of Load

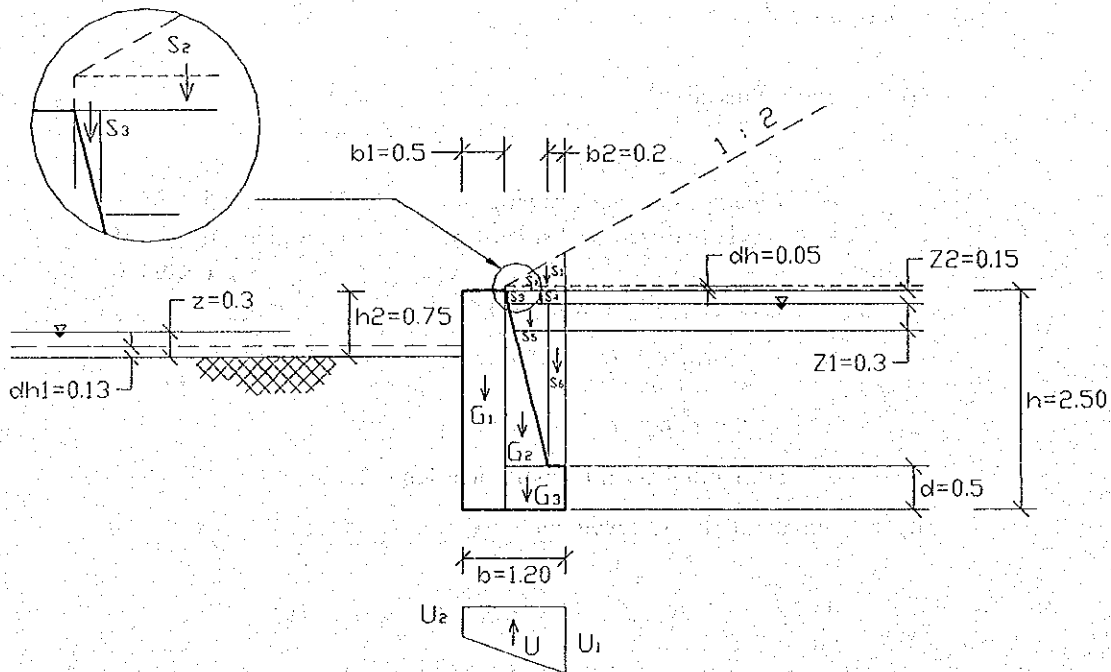
		Load Condition	
		Normal	Seismic
the vertical load	Weight of wall	+	+
	Weight of soil	+	+
	Uplift pressure	+	+
the horizontal load	Earth Pressure	+	+
	Water Pressure	+	+
	Horizontal Earthquake Pressure		+

“+” Consider in the calculation

Stability Analysis

(a) Center Gravity of Structure

(i) Proposed Condition



(ii) Weight of Wall Body

$$\begin{aligned}
 G_1 &= b_1 \times h \times \gamma_m & &= 2.875 \text{ t/m} \\
 &= 0.5 \times 2.5 \times 2.30 \\
 x_1 &= b_1/2 = 0.5/2 & &= 0.25 \text{ m} \\
 y_1 &= h/2 = 2.5/2 & &= 1.25 \text{ m} \\
 G_2 &= (b - b_1 - b_2) \times \frac{(h-d)}{2} \times \gamma_m & &= 1.150 \text{ t/m} \\
 &= 0.5 \times \frac{2.00}{2} \times 2.30 \\
 x_2 &= b_1 + (b - b_1 - b_2)/3 = 0.5 + 0.5/3 & &= 0.667 \text{ m} \\
 y_2 &= \frac{(h-d)}{3} = 2.0/3 & &= 0.667 \text{ m} \\
 G_3 &= (b - b_1) \times d \times \gamma_m & &= 0.805 \text{ t/m} \\
 &= 0.70 \times 0.50 \times 2.3 \\
 x_3 &= b_1 + (b - b_1)/2 = 0.5 + 0.7/2 & &= 0.85 \text{ m} \\
 y_3 &= d/2 = 0.5/2 & &= 0.25 \text{ m}
 \end{aligned}$$

(iii) Weight of Soil

$$\begin{aligned}
 S_1 &= \frac{1}{4} (b - b_1)^2 \times \gamma_s & &= 0.221 \text{ t/m} \\
 &= \frac{1}{4} (0.7)^2 \times 1.80 \\
 x_{S1} &= b_1 + \frac{2}{3} (b - b_1)
 \end{aligned}$$

$$\begin{aligned}
&= 0.5 + \frac{2}{3} (0.5) &= 0.833 \text{ m} \\
y_{s1} &= h + dh + (b - b_1)/2/3 \\
&= 2.5 + 0.10 + (0.7)/6 &= 2.717 \text{ m} \\
S_2 &= dh \times (b - b_1) \times \gamma_1 \\
&= 0.10 \times 0.5 \times 1.8 &= 0.09 \text{ t/m} \\
x_{s2} &= b_1 + (b - b_1)/2 \\
&= 0.5 + 0.7/2 &= 0.850 \text{ m} \\
y_{s2} &= h + dh/2 \\
&= 2.50 + 0.10/2 &= 2.550 \text{ m} \\
S_3 &= z_2 \times (z_2/4)/2 \times \gamma_1 \\
&= 0.15 \times (0.15/4)/2 \times 1.8 &= 0.005 \text{ t/m} \\
x_{s3} &= b_1 + \frac{2}{3} (z_2/4) \\
&= 0.5 + \frac{2}{3} (0.15/4) &= 0.525 \text{ m} \\
y_{s3} &= h - z_2/3 \\
&= 2.5 - 0.15/3 &= 2.45 \text{ m} \\
S_4 &= (b - b_1 - z_2/4) \times z_2 \times \gamma_1 \\
&= (0.7 - 0.15/4) \times 0.15 \times 1.8 &= 0.179 \text{ t/m} \\
x_{s4} &= b - (b - b_1 - z_2/4)/2 \\
&= 1.20 - (0.7 - 0.15/4)/2 &= 0.869 \text{ m} \\
y_{s4} &= h - z_2/2 \\
&= 2.5 - 0.15/2 &= 2.425 \text{ m} \\
S_5 &= (b - b_1 - b_2 - z_2/4) \times (h - d - z_2)/2 \times \gamma_s \\
&= 0.463 \times \frac{1.85}{2} \times 1.955 &= 0.836 \text{ t/m} \\
x_{s5} &= b_1 \times z_2/4 + \frac{2}{3} (b - b_1 - b_2 - z_2/4) \\
&= 0.5 + 0.15/4 + \frac{2}{3} (0.5 - 0.15/4) &= 0.846 \text{ m} \\
y_{s5} &= d + \frac{2}{3} (h - d - z_2) \\
&= 0.5 + \frac{2}{3} (1.85) &= 1.733 \text{ m} \\
S_6 &= (h - d - z_2) \times b_2 \times \gamma_s \\
&= 1.85 \times 0.2 \times 1.955 &= 0.723 \text{ t/m} \\
x_{s6} &= b - b_2/2 \\
&= 1.20 - 0.2/2 &= 1.10 \text{ m} \\
y_{s6} &= d + (h - d - z_2)/2 \\
&= 0.5 + 1.85/2 &= 1.425 \text{ m}
\end{aligned}$$

(iv) Buoyant Force (Uplift)

$$\Delta H = 0.3 \text{ m}$$

$$\begin{aligned}
u_1 &= 2.50 - 0.15 &= 2.35 \text{ m} \\
u_2 &= 2.35 - 2.05 &= 2.05 \text{ m}
\end{aligned}$$

$$\begin{aligned}
U &= b \times (u_1 + u_2)/2 \times \gamma_w \\
&= 1.20 \times (2.35 + 2.05)/2 \times 1.0 &= 2.640 \text{ t/m}
\end{aligned}$$

$$\begin{aligned}
x_U &= b - b/3 (u_1 + 2u_2)/(u_1 + u_2) \\
&= 1.2 - \frac{1.2}{3} (2.35 + 2 \times 2.05) / 4.40 &= 0.614 \text{ m}
\end{aligned}$$

$$y_U = 0.0 \text{ m}$$

(v) Center Gravity of Structure

Weight . W_i (t/m)	x_i (m)	$W_i \cdot x_i$ (tm/m)	y_i (m)	$W_i \cdot y_i$ (tm/m)
G_1	2.875	0.250	1.250	3.594
G_2	1.150	0.667	0.667	0.767
G_3	0.805	0.850	0.250	0.201
S_1	0.221	0.833	2.717	0.600
S_2	0.090	0.850	2.550	0.230
S_3	0.005	0.525	2.450	0.012
S_4	0.179	0.869	2.425	0.434
S_5	0.836	0.846	1.733	1.449
S_6	0.723	1.100	1.425	1.030
U	-2.640	0.614	0.000	0.000
Σ	4.244		2.470	8.317

$$x_o = \frac{\Sigma W_i \cdot x_i}{\Sigma W} = 0.582 \text{ m}$$

$$y = \frac{\Sigma W_i \cdot y_i}{\Sigma W} = 1.952 \text{ m}$$

For without uplift :

$$\Sigma W = 6.884 \text{ t/m}$$

$$\Sigma W_i \cdot x_i = 4.091 \text{ m}$$

$$\Sigma W_i \cdot y_i = 8.317 \text{ m}$$

$$x_o' = 0.594 \text{ m}$$

$$y_o' = 1.208 \text{ m}$$

(b) Bearing Capacity Beneath Slab

$$q_u = \alpha \cdot c \cdot k \cdot N + k \cdot g \cdot N_q + \frac{1}{2} \cdot \gamma \cdot \beta \cdot b \cdot N_\gamma$$

$$\alpha = \beta = 1.0$$

$$c = 0$$

$$Df = 1.75 \text{ m}$$

$$k = 1 + 0.3 \frac{Df}{b}$$

$$= 1 + 0.3 \left(\frac{1.75}{1.20} \right) = 1.438$$

$$q = t \times \gamma'_{gm} + (h_1 - t) \times \gamma'_s$$

$$= 0.5 \times 1.0 + 1.25 \times 0.955 = 1.694 \text{ t/m}^2$$

$$\text{For, } \phi = 42^\circ ; \theta = 13.5 ; N_q = 33$$

$$N_\gamma = 30$$

$$q_u = 1.438 \times 1.694 \times 33 + \frac{1}{2} \times 1.20 \times 30$$

$$= 98.387 \text{ t/m}^2$$

$$q_a = \frac{q_u}{3} = 32.796 \text{ t/m}^2 \quad (\text{in ordinary})$$

$$q_a = \frac{q_u}{3} = 49.194 \text{ t/m}^2 \quad (\text{in seismic})$$

(c) Coefficient of Earth Pressure

Applying Coulomb's formula as follows :

In Ordinary

$$\theta = 13.5^\circ ; \alpha = 26.56^\circ ; \delta = \phi = 42^\circ$$

$$\begin{aligned} K_a &= \frac{\cos^2(\phi - \theta)}{\cos^2 \theta \cos(\phi + \delta) \left[1 + \sqrt{\frac{(\sin \phi + \delta) \sin(\phi - \alpha)}{\cos(\theta + \delta) \cos(\theta - \alpha)}} \right]^2} \\ &= \frac{\cos^2(42 - 13.5)}{\cos^2(13.5) \times \cos(13.5 + 42) \left[1 + \sqrt{\frac{\sin(42 + 42) \times \sin(42 - 26.56)}{\cos(13.5 + 42) \times \cos(13.5 - 26.56)}} \right]^2} \\ &= 0.503 \end{aligned}$$

$$\begin{aligned} K_p &= \frac{\cos^2(\phi + \theta)}{\cos^2 \theta \cdot \cos(\theta + \delta) \left[1 - \sqrt{\frac{(\sin \phi - \delta) \sin(\phi + \alpha)}{\cos(\theta + \delta) \cos(\theta - \alpha)}} \right]^2} \\ &= \frac{\cos^2(42 + 13.5)}{\cos^2 13.5 \times \cos(13.5 + 42) \left[1 - \sqrt{\frac{\sin(42 - 42) \times \sin(42 + 26.56)}{\cos(13.5 + 42) \times \cos(13.5 - 26.56)}} \right]^2} \\ &= 0.599 \end{aligned}$$

(In Seismic)

$$\begin{aligned} K_h' &= \frac{\gamma_s}{\gamma_s - 1} \times K_h \\ &= \frac{1.955}{0.955} \times 0.12 = 0.2456 \end{aligned}$$

$$\theta_o = \text{atn } K_h' = \text{atn } 0.12 = 6.84^\circ$$

$$\theta_o' = \text{atn } K_h' = \text{atn } 0.2456 = 13.80^\circ$$

$$\delta = \phi/2 = 21^\circ ; \theta = 13.5^\circ ; \alpha = 26.56^\circ$$

$$K_{ea} = \frac{\cos^2(\phi - \theta_o - \theta)}{\cos \theta_o \cdot \cos^2 \theta \cdot \cos(\phi + \theta_o + \delta) \left[1 + \sqrt{\frac{(\sin \phi + \delta) \cdot \sin(\phi - \alpha - \theta_o)}{\cos(\theta + \theta_o + \delta) \cdot \cos(\theta - \alpha)}} \right]^2}$$

$$= \frac{\cos^2(42 - 6.84 - 13.5)}{\cos(6.84) \times \cos^2(13.5) \times \cos(13.5 + 6.84 + 21) \left[1 + \frac{\sin(42 + 21) \times \sin(42 - 26.56 - 6.84)}{\cos(13.5 + 6.84 + 21) \times \cos(13.5 - 26.56)} \right]^2}$$

$$= 0.602$$

$$K'_{ea} = \frac{\cos^2(42 - 13.8 - 13.5)}{\cos(13.8) \times \cos^2(13.5) \times \cos(13.5 + 1.38 + 21) \left[1 + \frac{\sin(42 + 21) \times \sin(42 - 26.56 - 13.8)}{\cos(13.5 + 13.8 + 21) \times \cos(13.5 - 26.56)} \right]^2}$$

$$= 1.067$$

$$K'_{ep} = \frac{\cos^2(\phi - \theta_o + \theta)}{\cos \theta_o \cdot \cos^2 \theta \cdot \cos(\phi - \theta_o + \delta) \left[1 - \frac{(\sin \phi - \delta) \cdot \sin(\phi + \alpha - \theta_o)}{\cos(\theta - \theta_o + \delta) \cdot \cos(\theta - \alpha)} \right]^2}$$

$$= \frac{\cos^2(42 - 6.84 + 13.5)}{\cos(6.84) \times \cos^2(13.5) \times \cos(13.5 - 6.84 + 21) \left[1 - \frac{\sin(42 - 21) \times \sin(42 + 26.56 - 6.84)}{\cos(13.5 - 6.84 + 21) \times \cos(13.5 - 26.56)} \right]^2}$$

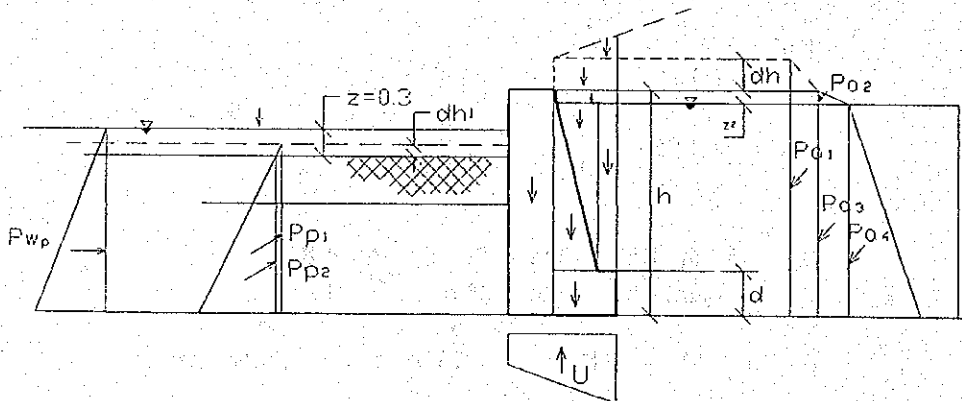
$$= 3.360$$

$$K'_{ep} = \frac{\cos^2(42 - 13.8 + 13.5)}{\cos(13.8) \times \cos^2(13.5) \times \cos(13.5 - 13.8 + 21) \left[1 - \frac{\sin(42 - 21) \times \sin(42 + 26.56 - 13.8)}{\cos(13.5 - 13.8 + 21) \times \cos(13.5 - 26.56)} \right]^2}$$

$$= 3.458$$

(d) Stability analysis on Normal Condition

(i) Load Condition



(ii) External Force

Active Earth Pressure

$$\begin{aligned} Pa_1 &= dh \times \gamma_t \times K_a \times h \\ &= 0.10 \times 1.80 \times 0.503 \times 2.5 &= 0.226 \text{ t/m} \\ Pa_2 &= \frac{1}{2} \times (z_2)^2 \times \gamma_t \times K_a \\ &= \frac{1}{2} \times (0.15)^2 \times 1.80 \times 0.503 &= 0.010 \text{ t/m} \\ Pa_3 &= z_2 \times \gamma_t \times K_a \times (h + z_2) \\ &= 0.15 \times 1.80 \times 0.503 \times 2.35 &= 0.319 \text{ t/m} \\ Pa_4 &= \frac{1}{2} \times (h - z_2)^2 \times \gamma'_s \times K_a \\ &= \frac{1}{2} \times (2.35)^2 \times 0.955 \times 0.503 &= 1.326 \text{ t/m} \end{aligned}$$

Horizontal Active Earth Pressure

$$\begin{aligned} Pah_1 &= Pa_1 \times \cos(\theta + \delta) \\ &= 0.226 \times \cos(13.5 + 42) &= 0.128 \text{ t/m} \\ y_{a1} &= h/2 &= 2.5/2 &= 1.25 \text{ m} \\ \\ Pah_2 &= Pa_2 \times \cos(\theta + \delta) \\ &= 0.010 \times \cos(55.5) &= 0.006 \text{ t/m} \\ y_{a2} &= z_2/3 + (h - z_2) \\ &= (0.15)/3 + 2.35 &= 2.400 \text{ m} \\ \\ Pah_3 &= Pa_3 \times \cos(\theta + \delta) \\ &= 0.319 \times \cos(55.5) &= 0.181 \text{ t/m} \\ y_{a3} &= (h - z_2)/2 \\ &= 2.35/2 &= 1.175 \text{ m} \\ \\ Pah_4 &= Pa_4 \times \cos(\theta + \delta) \\ &= 1.326 \times \cos(55.5) &= 0.751 \text{ t/m} \\ y_{a4} &= (h - z_2)/3 \\ &= 2.35/3 &= 0.783 \text{ m} \end{aligned}$$

Vertical Active Earth Pressure

$$\begin{aligned} Pav_1 &= Pa_1 \times \sin(\theta + \delta) \\ &= 0.226 \times \sin(55.5) &= 0.187 \text{ t/m} \\ x_{a1} &= 1.20 \text{ m} \\ \\ Pav_2 &= Pa_2 \times \sin(\theta + \delta) \\ &= 0.010 \times \sin(55.5) &= 0.008 \text{ t/m} \end{aligned}$$

$$\begin{aligned}
 x_{a2} &= 1.20 \text{ m} \\
 P_{av3} &= P_{a3} \times \sin(\theta + \delta) \\
 &= 0.319 \times \sin(55.5) &= 0.263 \text{ t/m} \\
 x_{a3} &= 1.20 \text{ m} \\
 P_{av4} &= P_{a4} \times \sin(\theta + \delta) \\
 &= 1.326 \times \sin(55.5) &= 1.093 \text{ t/m} \\
 x_{a4} &= 1.20 \text{ m}
 \end{aligned}$$

Passive Earth Pressure

$$\begin{aligned}
 P_{p1} &= dh_1 \times \gamma'_s \times K_p \times h_1 \\
 &= 0.13 \times 0.955 \times 0.599 \times 1.75 &= 0.130 \text{ t/m} \\
 P_{p2} &= \frac{1}{2} \times h_1^2 \times \gamma'_s \times K_p \\
 &= \frac{1}{2} \times (1.75)^2 \times 0.955 \times 0.599 &= 0.876 \text{ t/m}
 \end{aligned}$$

Horizontal Passive Earth Pressure

$$\begin{aligned}
 P_{ph1} &= P_{p1} \times \cos(\theta - \delta) \\
 &= 0.130 \times \cos(13.5 - 42) &= 0.114 \text{ t/m} \\
 y_{p1} &= h_1 / 2 \\
 &= 1.75 / 2 &= 0.875 \text{ m} \\
 P_{ph2} &= P_{p2} \times \cos(\theta - \delta) \\
 &= 0.876 \times \cos(-28.5) &= 0.770 \text{ t/m} \\
 y_{p2} &= h_1 / 3 \\
 &= 1.75 / 3 &= 0.583 \text{ m}
 \end{aligned}$$

Water Pressure

$$\begin{aligned}
 P_{wa} &= \frac{1}{2} (h - z_2)^2 \times \gamma_w \\
 &= \frac{1}{2} (2.35)^2 \times 1.0 &= 2.761 \text{ t/m} \\
 y_{wa} &= (h - z_2) / 3 \\
 &= 2.35 / 3 &= 0.783 \text{ m}
 \end{aligned}$$

(iii) Vertical Force and Moment

Vertical Force (t/m)		Arm (m)	Vertical Moment (tm/m)
P _{av1}	0.187	1.200	0.224
P _{av2}	0.008	1.200	0.010
P _{av3}	0.263	1.200	0.316
P _{av4}	1.093	1.200	1.312
W	4.244	-	2.470
FV	5.795	MV	4.331

(iv) Horizontal Force

Horizontal Force (t/m)		Arm (m)	Horizontal Moment (tm/m)
P _{ah1}	0.128	1.250	0.160
P _{ah2}	0.006	2.400	0.014
P _{ah3}	0.181	1.175	0.213
P _{ah4}	0.751	0.783	0.588
P _{ph2}	-0.114 ^{*)}	0.875	-0.100
P _{wa}	2.761	0.783	2.162
P _{wp}	-2.101	0.683	-1.435
FH	1.726	MH	1.153

^{*)} Passive earth pressure is omitted

(v) Check of Stability

Stability against sliding

$$\begin{aligned}
 SF &= \frac{FV}{FH} \cdot \tan \phi \\
 &= \frac{5.795}{1.726} \times \tan 42 &= 3.02 \\
 &> 1.5
 \end{aligned}$$

Stability against overturning

$$\begin{aligned}
 C &= \frac{b}{2} - \frac{(MV - MH)}{FV} \\
 &= \frac{1.20}{2} - \frac{(4.311 - 1.153)}{5.795} &= 0.052 \text{ m (-)} \\
 &< \frac{B}{6} (=0.20 \text{ m})
 \end{aligned}$$

Stability of bearing strata

$$\begin{aligned}
 q &= \frac{FV}{b} \times (1 \pm \frac{6e}{b}) \\
 q_{\max} &= \frac{5.795}{1.20} \times (1 + 6 \times \frac{0.052}{1.20}) &= 5.085 \text{ t/m}^2 \\
 &< q_a = 32.796 \text{ t/m}^2
 \end{aligned}$$

(e) Stability Analysis on Seismic Condition

(i) External Force

Active Earth Pressure

$$\begin{aligned} P_{ea1} &= dh \times \gamma_T \times K_{ea} \times h \\ &= 0.10 \times 1.80 \times 0.602 \times 2.5 &= 0.271 \text{ t/m} \end{aligned}$$

$$\begin{aligned} P_{ea2} &= \frac{1}{2} \times (z_2)^2 \times \gamma_1 \times K_{ea} \\ &= \frac{1}{2} \times (0.15)^2 \times 1.80 \times 0.602 &= 0.012 \text{ t/m} \end{aligned}$$

$$\begin{aligned} P_{ea3} &= (z_2) \times \gamma_s \times K_{ea} \times (h - z_2) \\ &= 0.15 \times 1.80 \times 0.602 \times 2.35 &= 0.382 \text{ t/m} \end{aligned}$$

$$\begin{aligned} P_{ea4} &= \frac{1}{2} \times (h - z_2)^2 \times \gamma'_s \times K'_{ea} \\ &= \frac{1}{2} \times (2.35)^2 \times 0.955 \times 1.067 &= 2.814 \text{ t/m} \end{aligned}$$

Horizontal Active Earth Pressure

$$\begin{aligned} P_{eah1} &= P_{ea1} \times \cos(\theta + \delta) \\ &= 0.271 \times \cos(13.5 + 21) &= 0.223 \text{ t/m} \end{aligned}$$

$$y_{ea1} = h/2 = 1.25 \text{ m}$$

$$\begin{aligned} P_{eah2} &= P_{ea2} \times \cos(\theta + \delta) \\ &= 0.012 \times \cos(34.5) &= 0.010 \text{ t/m} \end{aligned}$$

$$y_{ea2} = (z_2) / 3 + (h_1 - z) = 2.400 \text{ m}$$

$$\begin{aligned} P_{eah3} &= P_{ea3} \times \cos(\theta + \delta) \\ &= 0.382 \times \cos(34.5) &= 0.315 \text{ t/m} \end{aligned}$$

$$y_{ea3} = (h - z_2) / 2 = 1.175 \text{ m}$$

$$\begin{aligned} P_{eah4} &= P_{ea4} \times \cos(\theta + \delta) \\ &= 2.814 \times \cos(34.5) &= 2.319 \text{ t/m} \end{aligned}$$

$$y_{ea4} = (h - z_2) / 3 = 0.783 \text{ m}$$

Vertical active Earth Pressure

$$\begin{aligned} P_{eav1} &= P_{ea1} \times \sin(\theta + \delta) \\ &= 0.271 \times \sin(34.5) &= 0.153 \text{ t/m} \end{aligned}$$

$$y_{ea1} = 1.20 \text{ m}$$

$$P_{cav2} = P_{ca2} \times \sin(\theta + \delta)$$

$$= 0.012 \times \sin(34.5) = 0.007 \text{ t/m}$$

$$y_{ca2} = 1.20 \text{ m}$$

$$P_{cav3} = P_{ca3} \times \sin(\theta + \delta)$$

$$= 0.382 \times \sin(34.5) = 0.216 \text{ t/m}$$

$$y_{ca3} = 1.20 \text{ m}$$

$$P_{cav4} = P_{ca4} \times \sin(\theta + \delta)$$

$$= 2.814 \times \sin(34.5) = 1.594 \text{ t/m}$$

$$y_{ca4} = 1.20 \text{ m}$$

Passive Earth Pressure

$$P_{ep1} = dh_1 \times \gamma'_s \times K'_{ep} \times h_1$$

$$= 0.13 \times 0.955 \times 3.458 \times 1.75 = 0.751 \text{ t/m}$$

$$P_{ep2} = \frac{1}{2} \times h_1^2 \times \gamma'_s \times K'_{ep}$$

$$= \frac{1}{2} \times (1.75)^2 \times 0.955 \times 3.458 = 5.057 \text{ t/m}$$

Horizontal Passive Earth Pressure

$$P_{ep1} = P_{ep1} \times \cos(\theta + \delta)$$

$$= 0.751 \times \cos(13.5 - 21) = 0.745 \text{ t/m}$$

$$y_{ep1} = h_1 / 3 = 0.875 \text{ m}$$

$$P_{ep2} = P_{ep2} \times \cos(\theta + \delta)$$

$$= 5.057 \times \cos(-7.5) = 5.014 \text{ t/m}$$

$$y_{ep2} = h_1 / 3 = 0.583 \text{ m}$$

Water Pressure

$$P_{wa} = 2.761 \text{ t/m}$$

$$y_{wa} = 0.783 \text{ t/m}$$

$$P_{wp} = 2.101 \text{ t/m}$$

$$y_{wp} = 0.683 \text{ t/m}$$

Earthquake Force

$$W_e = W \times kh = 0.826 \text{ t/m}$$

$$y_e = 1.208 \text{ m}$$

(ii) Vertical Force and Moment

Vertical Force (t/m)		Arm (m)	Vertical Moment (tm/m)
P_{eav1}	0.153	1.200	0.184
P_{eav2}	0.007	1.200	0.008
P_{eav3}	0.216	1.200	0.259
P_{eav4}	1.594	1.200	1.913
W	4.244	-	2.470
FVe	6.214	MVe	4.834

(iii) Horizontal Force and Moment

Horizontal Force (t/m)		Arm (m)	Horizontal Moment (tm/m)
P_{eah1}	0.223	1.250	0.279
P_{eah2}	0.010	2.400	0.024
P_{eah3}	0.315	1.176	0.370
P_{eah4}	2.319	0.783	1.816
P_{eph}	-0.745 *	0.875	-0.652
P_{wa}	2.761	0.785	2.162
P_{wp}	-2.101	0.683	-1.435
W_e	0.826	1.208	0.998
FHe	4.353	MHe	0.639

*¹) Passive earth pressure is omitted

(iv) Check Stability

Stability against sliding

$$\begin{aligned} SF &= FV_e / FHe \cdot \tan \phi \\ &= 6.214 / 4.353 \times \tan 42^\circ &= 1.285 \\ &> 1.2 \end{aligned}$$

Stability against overturning

$$\begin{aligned} e &= \frac{b}{2} - (MV_e - MHe) / FV_e \\ &= \frac{1.2}{2} - (4.834 - 0.639) / 6.214 &= 0.075 \text{ m} \\ &< \frac{b}{6} (=0.20 \text{ m}) \end{aligned}$$

Stability of bearing strata

$$\begin{aligned} q &= \frac{FV_e}{b} (1 \pm be/b) \\ q_{\max} &= \frac{6.214}{1.2} (1 + 6 \times \frac{0.075}{1.20}) &= 7.120 \text{ t/m} \\ &< q_{ea} (= 49.194 \text{ t/m}^2) \end{aligned}$$