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11-9 Minimum Discharge values for the Stations Studied by JICA



COMPANHIA PARANAENSE DE ENERGIA - COPEL DIRETORIA DE ENGENHARIA E CONSTRUÇÃO - DEC SUPERINTENDÊNCIA DE PLANEJAMENTO E ESTUDOS - SPE DEPARTAMENTO DE HIDROLOGIA E ESTUDOS ENERGÉTICOS - DPHE

MINIMUM DISCHARGE VALUES FOR THE STATIONS STUDIED BY JICA FROM PARANÁ STATE



COMPANHIA PARANAENSE DE ENERGIA - COPEL DIRETORIA DE ENGENHARIA E CONSTRUÇÃO - DEC SUPERINTENDÊNCIA DE PLANEJAMENTO E ESTUDOS - SPE DEPARTAMENTO DE HIDROLOGIA E ESTUDOS ENERGÉTICOS - DPHE

TYPE OF DOCUMENT: TEC	CHNICAL REPORT		
TITLE:	·		
Minimum discharge values	for the stations calcula	ated by JICA from I	Paraná State
AUTHORS:		<u>'</u>	
Martha R. V. B. Sugai	CREA 6308/D - P		
Fabricio Müller	CREA 25950/D - 1	PR	
OBJECTIVE: Calculate the m	inimum discharge value	es in the stations cal	culated by ЛСА.
			s and ten years of recurrence
(Q _{10.7}) and the corresponde distribution for the fluviometr graphs and are compared with t	ent specific discharge ic stations studied by	es (q _{10.7}) were / ЛСА. These val	calculated with the Weibuli ues are shown in tables and
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KEY-WORDS: Weibull - Mi	nimum - Discharges		
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		DATE	NUMBER:
		3/95	DPHE/VHID - 5/95

MINIMUM DISCHARGE VALUES FOR THE STATIONS STUDIED BY JICA FROM PARANÁ STATE

The minimum discharge values for the stations calculated by HCA with mean from 7 days and 10 years of recurrence $(Q_{10,7})$ and the correspondent specific discharges $(q_{10,7})$ are shown at tables 1 and 2. For each station, two different periods were investigated:

- the historic period of the station;
- the available period in the station between 1974 and 1993.

The values of Q_{10.7} were calculated by the formula:

$$Q_{10,7} = (\overline{Q}_7) \times (K_{10})$$

where:

 \overline{Q}_7 = mean of the minimum discharge with 7 days of duration of each year;

 K_{10} = recurrence factor calculated for 10 years.

The recurrence factor is calculated from a non-dimensional series (see Sant'Ana et al., 1978) with the Weibull distribution (as presented by Kite, 1978), considered by the HG-52 project as the best distribution in fitting minimum discharges in all Parana State, except for two stations - 64693000 and 65175000 - calculated by the 3-parameter lognormal distribution or Galton distribution (see also Kite, 1978) because the program utilised don't accept skewness coefficients greater than 2 for the Weibull distribution.

Table 1 shows:

- the number of the station as presented by JICA;
- the code of the station (the station number 65895002 were obtained by a combination of the stations 65895002, fluviometric station of Salto Osório, from 1941 to 1975, and 65894995, Salto Osório dam inflow, from 1976 to 1993);
- · the station and the river where is located the station;

For the two periods (historical and available between 1974 and 1993) table 1 shows the values of:

- mean of the minimum of 7 days of duration;
- the recurrence factor K₁₀;
- the Q_{10,7} and the specific q_{10,7} discharge.

For comparison, table I shows the values of Q_{10,7} and the specific q_{10,7} discharge as calculated by JICA and based on HG-52 (Sant'Ana et al., 1982) study.

Table 2 shows the same as table 2 except the values of $\overline{\mathbb{Q}}_7$ and K_{10} for the two periods studied.

Figures 1 to 4 shows, for the Iguaçu, Ivai, Tibagi e Piquiri rivers the values of Q_{10,7} calculated with Weibull distribution (for all historical period and for the period from 74 to 93) and calculated by JICA based on HG-52 project plotted against drainage area in km².

REFERENCES

KITE, G. W., 1978. Frequency and risk analyses in hidrology. Fort Collins, Water Resources Publications.

SANT'ANA ET AL., 1982. Projeto HG-52: Aproveitamentos de pequeno porte. Curitiba, CEHPAR.

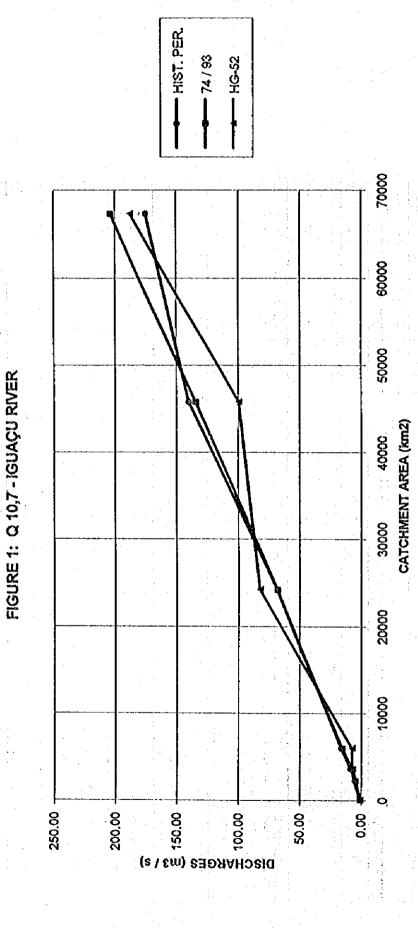
		_															
MAK. BC		CODE(") STATION	BASIN	RIVER				MISTO.	HISTORICAL REGISTER	į.			1974 / 1995 (* * *			3	rat 1987
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					Come		(W)	(mpe)	(M3.A)	0/10/10m2)	(mSm)	(mgm)	(40)(5)	0/a/lon2)		(m3.4s)	\$1=10m2)
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	2 64362000	TOWAZINA	L	å	2015	27.63	6.42	52307.0	807	3.	11.66	980150	\$6.8	297		29'6	1.92
	3 64370000	ANDIRA	-	•	2622	32,63	15.75	0 46496	732	8.	7.08	0 48767	10,23	3		607	108
	00077779	invers	O-QI_	Tibed	833	72.83	25.22	2220	12.15	272	27.22	777520	12.11	ន្ត	14	8,23	1,86
•^	00053475	TEAG			946	S	42.22	LE SELO	16.77	1.67	47.8	033063	15.76	1,76		1,05	15.
	CH491000	BARRA DO RIB. DAS ANTAS			895	4293	15.67	0.47484	Ŗ	ST.	8	0.46267	41.19	3,7		24.18	3.5
•	64507011	JATAZIMHO (EXTENDIDO)		-	21955	12,90	100 93	0.43083	43 46	1 38	122.06	0.39721	47.76	2.10		19.98	0.94
9	8 6455000	IVILA SIEVA JAPOIM	Preside	Precé	129+	C8483	37.68	18702.0	19.13	4.14	37.27	9577.0	19.94	4.35		20.02	4.50
	000 2349	TEREZACRISTINA	3	Ē	2252	\$7.81	9,76	26505.0	\$	1,36	10,00	0.42380	Ġ	1,19		57.4	133
2	0005	PORTO ESPANHOL			95	83	3	0,43702	14.60	ě	7.07	0,36362	13.08	S		7,74	0.00
=	64675002	PORTO BANANEIRAS			34200	282	14,02	0.36368	42.15	1,74	114.02	0,3696	42.15	X.	#	1704	1,67
- 2		PORTO PARAISO DO MORTE SRT			28427	3	145.74	0,46448	15,6	237	क्षे	0,40067	8	ñ		145.55	5,12
2	00000000	MOVO PORTO TAGUARA	-	_	3432	75/93	245,45	0,57542	141.24	4.10	245.45	0.57542	141.24	4,10	· ·	144.96	421
1	0051/2/1900	PORTO GUARANI	Paris.	Port	â	29/11	14,43	0,26637	(C)	1960		0.28537	7	8.0	76	10.64	25
\$	64795500	PONTE DO FICURE			000:-	7.00	8	0.41028	3	7.7	60.92	0.3750n	20	282		61.60	240
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£	8902,000	CUATUMEA			ž N	7.63	0	0,40696	Ą	38	30	0,40696	8	99"	73	5,46	22
R	65036000	PORTO AMAZOHAS	-		3862	26/93	Ž	7,675.0	Ş	Ħ	14.76	0.43497	2	2		7.32	8
75	. 00009059	SAC NATEUS OCCU.			6065	37.83	X,	0,62796	15.99	7	27.47	0.55653	S.	2.52		7.16	1,16
N	65310000	UNITO DA VITORIA			ž	31/80	4	0.0350	27.75	282	85,011	0.59901	3	597		22.23	3
ij	65495002	SALTO OSORIO			-285 -	193	8	0.52846	146.02	305	230.04	0.43349	Ž	32	-	8	217
*	00006659	SALTO CATARATAS		****	222	8	27.572	0,46050	174.41	27	65.45	0.44606	8	8		167.14	2.78
ก	65175000	Swe S		o.S.	7970	66.89	5,7	0.57026	8	3	16.9	0.30680	n n	8	ψ,	08.6	អ៊
<i>Y</i> a	6525000	FOZ DO CACHOEIRA		Tunbo	8	96/33	8	0.5550	27.5	3.10	8	0230	215	3.10	Ħ	100	0.92
ħ	65625000	SANTACLARA		ogca	2913	50.50	ት	0.55558	ii K	346	28.50	0.43404	1,35	28		12.60	22
E	2596000	AGUAS DOVERE		Shoot	9699	57/83	8	907970	16.24	2.2	75.25	0 39467	14 65	2.19		10.45	156
Ē.	A170000	CAPELA DO RIBEIRA	Ribbers	Shere	7257	27.75	50.00	0.67610	66.00	5.60	16.07	0.71452	50.74	6.93		47.87	6.60
8	_	MOUNTA	Clorken	- Ardean	77	26.93	335	0.48347	3	7.46	57	0.41549	ξ.	8		1	6.13
5	82195002	MORRETES (MARUMBI)		Menandi	ନ	76.92	62.0	0.395.0	23.	5,94	0.73	0.3962.0	63	88	*	0.33	623

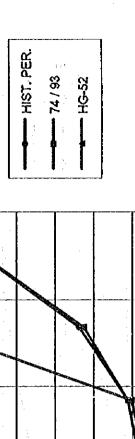
(7) - Sato Oabrio station were obtained by a composition from 65895002 station (from 41 to 75) and 65894985 station (from 76 to 93) (7). The stations that have the symbol § in "oba." column were calculated by Gatton's (or 2-parameter lognormal) distribution (* *). The stations that have the # symbol in "oba." column have a historical register minor than 74 / 93

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6517500 6526000 65625000 65625000	<u></u>			71579	8	174.45	25.	255.002	3.02		187.14	278
0009859		Negro	٤	7970	65/93	88	87.	11.11	87	L/r	9.80	Ŋ
65625000 SANTA CLAS 65960000 AGUAS DOV		t mbo	8	8	8683	13	3.10	215	3.10	*	20.0	28.0
65960000 AGUAS DO \		ğ	Jordão	3913	88	13.54	3.45	11.56	28		12.80	327
		č	Chopim	\$600	57/25	16.24	242	14.66	2.10		10.45	-8
29 ST20000 ICAPELA DO RIBEIRA	RA Riberta	Ribeira	P.I.S	7252	37/03	40.50	5.00	50.24	6.93		178,77	9.60
MORRETIES	LARA)	N. es	Litoranea (Nhundiaquara	217	38/33	1.62	7.46	5.	4.65		1,33	5.0
31 82195002 MORRETES (MARUMB)	JMBŋ	Xex	Manumbi	8	76/97	0.31	89	0.31	5.91	74	0.33	22

(*) - Salto Osório station were obtained by a composition from 65895002 station (from 41 to 75) and 65894995 station (from 76 to 93) (**) - The stations that have the symbol § in "obs." column were calculated by Calton's (or 3-parameter lognormal) distribution (***) - The stations that have the # symbol in "obs." column have a historical register minor than 74 f.93

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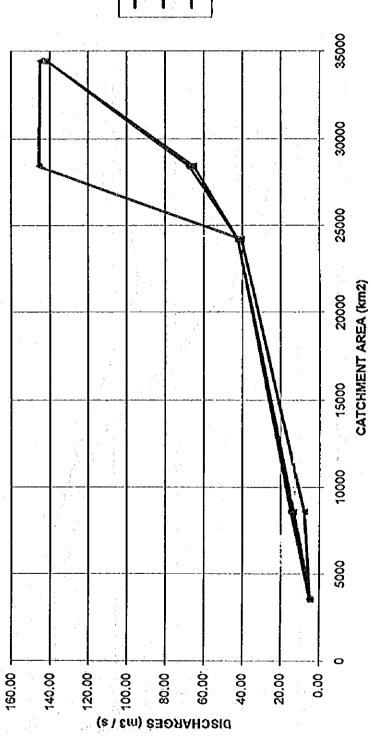
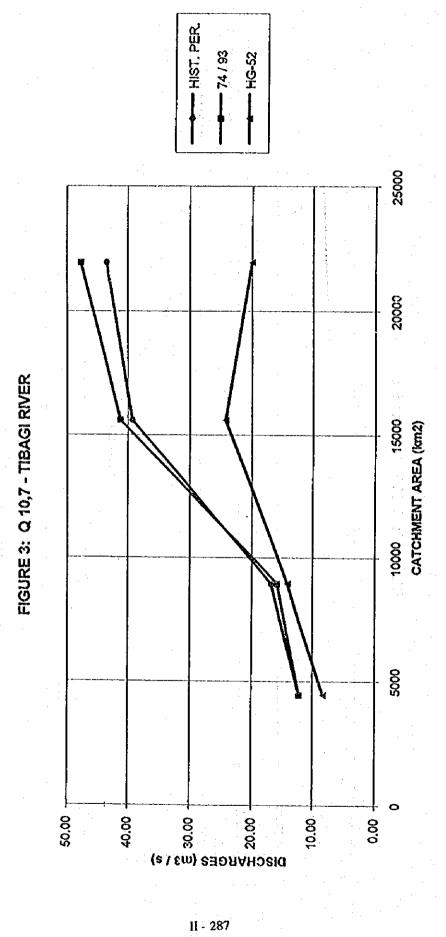


FIGURE 2: Q 10,7 - IVAÍ RIVER



HIST. PER. 74 / 93

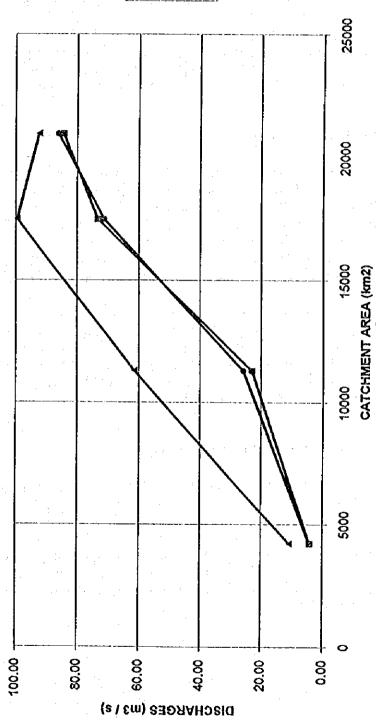


FIGURE 4: Q 10,7 - PIQUIRI RIVER

A VAZÃO MÍNIMA DE SETE DIAS DE DURAÇÃO E DEZ ANOS DE RECORRÊNCIA NO ESTADO DO PARANÁ

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INTRODUÇÃO

O valor da vazão mínima de sete dias de duração e dez anos de recorrência (Q_{10,7}) tem grande importância pois serve, para o Estado do Paraná, como avaliação das condições de captação do potencial de águas superficiais em uma dada bacia hidrográfica. Este trabalho surgiu da necessidade de subsidiar a JICA - JAPAN INTERNATIONAL COOPERATION AGENCY, em seu Plano Diretor de Recursos Hídricos do Paraná, na parte referente ao potencial hídrico do Estado (JICA, 1995).

São analisadas estações em bacias hidrográficas representativas do Estado, e, para cada estação, o valor de $Q_{10,7}$ é calculado por duas distribuições, dois métodos de obtenção da série de mínimas e dois períodos diferentes. Finalmente, são apresentadas equações empíricas relacionando o valor de $Q_{10,7}$ com a área de drenagem, para quatro bacias diferentes e para todo o Estado.

MÉTODOS DE CÁLCULO DE Q_{10,7}

Para cada estação estudada, duas distribuições foram ajustadas pelo método dos momentos: a distribuição de Weibull, escolhida pelo projeto IIG-52 (Sant'ana et al, 1989) como a mais apropriada para representar séries de vazões mínimas em todo o estado do Paraná, e a distribuição de Galton, ou lognormal a três parâmetros, considerada por Roche (1963, apud Gomide, 1970) a mais apropriada para estudos de mínimas em regiões tropicais. As equações de distribuição utilizadas estão mostradas em Kite (1977).

Para cada uma das duas distribuições acima, foi calculado o valor de $Q_{10.7}$ por duas séries de vazões mínimas diferentes:

- série não-extendida: é, simplesmente, a série de vazões mínimas anuais de sete dias de duração;
- série extendida: utiliza uma série composta com vazões adimensionalizadas mínimas anuais com 7, 15, 21, 30, 45, 60, 90, 120, 150 e 180 dias de duração, segundo a proposta de Gomide (1970). Esta série adimensionalizada é tomada como um única série e para a mesma são aplicadas as distribuições de Weibull e de Galton para a obtenção do fator de recorrência de dez anos. Para a obtenção do valor final de Q_{10,7}, multiplica-se este fator pela média de vazões mínimas anuais de sete dias de duração.

Finalmente, para os quatro casos descritos acima (duas distribuições e duas séries) são empregados dois períodos diferentes: o histórico, contendo todos os anos da estação, e o período disponível do ano de 1974 em diante, que é o período básico utilizado pela JICA em seu Plano Diretor.

As estações estudadas foram em número de 30, as mesmas escolhidas pela JICA como representativas do Estado, com exceção da estação 65175000 - Divisa, situada na Bacia do Iguaçu. A relação das estações, com seus códigos, bacias e rios onde estão situadas, áreas de drenagem e período de dados está mostrada na tabela 1. Esta tabela também mostra os oito valores de Q_{10.7} em m³/s calculados para cada estação, considerando diferentes distribuições, séries e períodos estudados. No topo de cada coluna com vazões está escrita uma letra, que corresponde a um tipo de estudo diferente, explicado na parte de baixo da tabela. Por exemplo, para a letra A: "Galton - extendida - histórico", a coluna correspondente dá os valores de Q_{10.7} calculados pela distribuição de Galton por séries extendidas com o período histórico disponível. Em algumas células da tabela há traços: são casos de períodos históricos que se iniciam depois de 1974, ou casos em que a distribuição de Weibull não pôde ser aplicada porque o valor do coeficiente de assimetria resultou fora dos limites da fórmula (11-13), pag. 135, do livro de Kite(1977), utilizada no programa computacional que calcula as vazões mínimas.

ANÁLISE DOS RESULTADOS

Foram comparadas as estimativas dos valores de Q_{10,7} de acordo com sua distribuição, série e período. Assim, foram calculadas estatísticas relacionando a diferença entre Weibull e Galton, entre a série extendida e a não extendida, e entre os dois períodos empregados. Para cada uma destas três comparações foram elaborados dois vetores, de modo que para cada valor constante em um vetor corresponde um único valor no outro, que é o valor, para a mesma estação, de Q_{10,7} levando em conta um método diferente - aquele a ser comparado -, mas com os outros dois iguais. Por exemplo, na comparação Weibull-Galton, para um valor, em uma dada estação, calculada por Weibull com série extendida e período histórico, corresponderá, para o outro vetor, o valor calculado por Galton, mas também com série extendida e período histórico. Quando, em uma estação, não foi possível calcular o valor de Q_{10,7} por uma combinação de métodos, não há valores, correspondentes a este caso específico, no outro vetor.

Deste modo, foram elaborados três grupos de dois vetores. Estes três grupos são:

- Weibull-Galton;
- Série extendida não extendida;
- Período histórico 74 em diante.

Foram calculadas duas estatísticas que calculam a distância entre cada um destes três grupos de dois vetores:

 valor absoluto médio das distâncias percentuais (A): sejam os valores de um vetor notados como x(i), e os do outro y(i). O valor de A é dado por:

$$A = \frac{1}{N} \sum_{i=1}^{N} \left| \frac{x(i) - y(i)}{x(i)} \right|.100$$
 (1)

onde N é o tamanho dos dois vetores.

 raiz do valor quadrático médio das distâncias percentuais (B): com x(i), y(i) e N conforme mostrado acima, B é dado por:

Tabela 1 - Valores de Q_{10,7} (m³/s) nas estações estudadas

CODICO	ESTAÇÃO	BACIA	STO STO	PER	AREA	٧Æ	ZAO 0 10.7	(m3/s) CA	LCULAD,	VAZÃO O 10,7 (m3/s) CALCULADA CONFORME (ver legenda abaixo)	ME (ver lo	cade abaca	6
		•			(km 2)	٧	Æ	Ö	Ω		u.	O	ľ
64242000	TAMANDUA	Starare.	Unguariativa	77/93	7791	7.86	7.26	Parameter .		7,93	l		
64360000	TOMAZINA	Cinzes	Cuzas	27/93	50.5	Ç.,	3.1	27.0	8	7.4.	30.5		8
64370000	ANDIKÁ	Cuzzas	Ciazas	32/93	22%	6,70	7,21	10.34	:0,46	6.84	. !	10 14	10,29
6:41:000	かない。	Tibegi	Tibagi	75/93	4450	11,29	11.7			₹ ::	12.11		ľ
000.94	TEAGI			32/93	2762	13.09	16.7	19.68	1647	19,07	2	19.1	
000161-0	B. DO R.B. DAS ANTAS			42/93	15600	43.85	38,76	56.52	41.42		39,26		·
6.150701	PATAIZINHO (EXT.)			32/93	21955	41.86	42.36	\$4.28	48.85	41.7	43,46	52,46	47,76
0000551-9	NEA SEVA JARDEM	Power	Pumpo	£6/69	4627	20.9	19.13	19.65	19.43	29.62	19,13		
00052919	TEREZA CRISTINA	N. I	N.	57/91	33.72	Ş	16,4	7	4,26	4,73	3,		
0005 1 915	PORTO ESPANHOL	-ver-		883	2600	14,31	¥.	17,66	13.52	14,32	ĭ		
64675002	PORTO BANANEIRAS	-		75.93	24200	2,6	43,87			47.34	47.15	÷	
6468.5000	P. PARAISO DO N.	er-e-		\$493	23.427	8	68.23	78.41	67.31	70,52	67.53		
9.693000	N. PORTO TAQUARA			75/93	34432	141.25	141,24	7		144.07			
6+771500	PORTO GUARANI	Prque	Psquan	77/93	4223	*	<u> </u>	******	I	4,28	4.13		
21793300	PONTE DO PIQUIRA			71/93	11303	27,07	26.24	3	2.5	26.	3 7		
64820000	PORTO FORMOSA			6//3	17500	77.43	71,63	2,4	73,16	20,0%	73,38		
64830000	B. DO SANTA MARIA		-	70.93	20022	2,17	\$7,72	86,56	85,33	90.47	85.93		٠
65010000	FAZENDINHA	r.Sansig	advensite	\$6793	110	0,30	05,0	0.0	o	0	0,49	ŀ	l
65025000	GUAUVIRA		~	77.93	23.02	7	423	1		4.81	4 29		
65035000	PORTO AMAZONAS			36/93	3662	7.45	803	6.21	8	7.43	5,31		
6500000	SAO NATEUS DO SUL			31/93	8909	13,91	15,52	7	14.57	14.47	15.99		
6:310000	CNIAO DA VITORIA			31/93	24211	8,66	66.42	62.63	2	61,19	68.33		
65895002	SALTO OSORIO			41/93	45824	137,07	135,51	138,65	133,8	131,56	170.04		
65993000	SALTOCATARATAS		-Cree	43/93	67317	182,03	11.00	240.36	210,43	186.43	174.41	•	
65260000	FOZ DO CACHOETRA		Timbo	\$ \$ \$	809	2.41	۲. ت	T	T	2,38	2.15	Ċ	
000523590	SANTA CLARA		Jonetio	66	3913	13 05	13,52	12,43	11.84	12,98	3		11.55
65960000	AGUAS DO VERE		Chopim	57/93	9699	16.92	16.68	16.58	15,25	16.6	16.24		14,66
21200000		Riberra	Riberrs 1	37/93	7252	39.72	40,01	43.76	49,29	40,09	40,59		50.24
22170000	ND.)	Litorabee	Nhundaeq.	32/93	217	02.	1,67	1,20	1.0	1,77	1,62	1.15	1,01
82195002	MORRETES (MAR.)	Litorence	Menumbi	26/92	g.	0,47	F. 0	T		64.0	0,31	Ì	

Legenda:

A GALTON - EXTENDIDA - MISTORICO	E WEBULL - EXTENDIDA - HISTORICO
B GALTON - NÃO EXTENDIDA - HISTÓRICO	F WEIBULL - NAO EXTENDIDA - MISTORICO
C GALTON - EXTENDIDA - 74 EM DIANTE	G WEBULL - EXTENDIDA - 74 EM DIANTE
D GALTON - NAO EXTENDIDA - 74 EM DIANTE	H WEIBULL - NAO EXTRNDIDA - 74 EM DIANTE

$$B = \sqrt{\frac{1}{N} \sum_{i=1}^{N} \left[\frac{x(i) - y(i)}{x(i)} . 100 \right]^{2}}$$
 (2)

Os resultados dos dois testes, em porcentagem, está mostrado na tabela 2, para cada uma das três comparações. Quanto menores os valores de A e B, maior a proximidade entre os vetores x(i) e y(i), i=1,...,N

Tabela 2 - Resultados para os testes efetuados

COMPARAÇÕES	\(i))(i)	TESTE	S (%)
		<u> </u>	Λ	В
GALTON - WEIBULL	GALTON	WEIBULL	2.19	2,66
EXTENDIDA - NÃO EXTENDIDA	EXTENDIDA	NÃO EXTENDIDO	6,87	8,78
HISTÓRICO - 74 EM DIANTE	HISTÓRICO	74 EM DIANTE	16,50	26,47

Pela tabela 2 nota-se que praticamente não houve diferença em se aplicar a distribuição de Weibull ou de Galton, o que era de certa maneira esperado, tendo em vista que quase todas as estações estudadas tinham pelo menos 20 anos de dados, e este estudo se resume em 10 anos de recorrência. Também a diferença entre séries, extendida ou não, não altera sobremaneira o resultado de $Q_{10,7}$. O grande fator de alteração dos resultados foi o período utilizado: pela tabela 1, vê-se que para a grande maioria das estações o valor de $Q_{10,7}$ calculado é maior no período de 1974 em diante do que no período histórico como um todo

FÓRMULAS EMPÍRICAS RELACIONANDO $Q_{10,7}$ E ÁREAS DE DRENAGEM

Neste trabalho foram calculados, para quatro bacias selecionadas e para o total das estações estudadas, fórmulas relacionando Q_{10,7} com a área de drenagem. As equações são obtidas pelo método dos mínimos quadrados e são de segundo ou terceiro grau. A tabela 3 fornece, para cada caso, o grau da curva empregada, os parâmetros obtidos e

coeficientes de correlação entre os dados e a curva. As curvas são do tipo:

$$Q_{10,7} = a + b_1 (AREA) + b_2 (AREA)^2 + b_3 (AREA)^3$$
 (3)

Na tabela 3, os coeficientes b₃ não existem para as equações de segundo grau e o bacia "TODAS" se refere ao estudo envolvendo todos os valores da Tabela1.

Tabela 3 - Coeficientes da curva de regressão para as equações empíricas

BACIA	GRAU	COEFICI	ENIES DA	CURVA DE	REGRESSÃO	CORREL
		£		b,	b ₃	
IGUAÇU	3°	1,27	1,83 * 10 ⁻³	4,46 * 10.8	-4,07 * 10 ·13	0,9922
IVAÍ	3°	-9,61	5,10 * 10 ⁻³	-3,61 * 10 ⁻⁷	9,89 * 10 -12	0,9991
PIQUIRI	2°	-5,45	$1,35 * 10^{-3}$	1,54 * 10 ⁻⁷	·	0,9893
TIBAGI	20	-6,42	3,83 * 10 ⁻³	-6,15 * 10 ⁻⁸		0,9547
TODAS	3°	1,18	2,08 * 10 ⁻³	4,76 • 10-7	-5,07 * 10 ⁻¹³	0,9593

As figuras 1 a 3 mostram os valores de Q_{10,7} em m³/s plotados nas ordenadas contra a área de drenagem em km² nas abcissas para, respectivamente, a bacia do Iguaçu, a bacia do Ivaí e para todos os valores estudados. Nestas figuras, os pontos representam os valores constantes na Tabela I para cada caso; a curva representa a equação de regressão mostrada na Tabela 3.

As equações resultaram em altos valores do coeficiente de correlação, é preciso tomar cuidado, entretanto, quando da extrapolação para áreas de drenagem maiores ou menores que aquelas para as quais foram calculadas as equações (mostradas na Tabela 1). Estas fórmulas podem ser empregadas como uma primeira estimativa do valor de Q_{10,7} para uma dada área de drenagem.

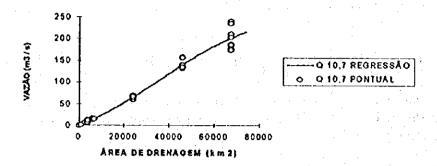


Figura 1 - Q_{10,7} na Bacia do Iguaçu: Vazão contra Área de Drenagem

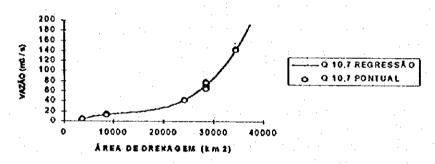


Figura 2 - Q_{10,7} na Bacia do Ivaí: Vazão contra Área de Drenagem

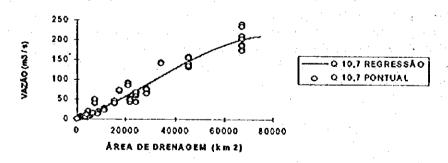


Figura 3 - Q_{10,7} na Estado do Paraná: Vazão contra Área de Drenagem

CONCLUSÕES E RECOMENDAÇÕES

Para os casos estudados, o período de dados utilizados mostrou-se a variável mais importante no estudo do valor de $Q_{10.7}$.

As equações empíricas relacionando Q_{10,7} e área de drenagem resultaram em altos valores para o coeficiente de correlação, mas devem ser empregadas apenas como uma primeira estimativa para o valor de Q_{10,7}

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REFERÊNCIAS BIBLIOGRÁFICAS

- GOMIDE, Francisco Luiz Sibut. Contribuição ao estudo de períodos de estiagem. <u>In</u>: CONGRESSO LATINOAMERICANO DE HIDRAULICA (4.: 1970: Oaxtpec Morelos) Anais. Oaxtpec Morelos: IAHR, 1970. v.2, p.25-36.
- JAPAN INTERNATIONAL COOPERATION AGENCY. The master plan study on the utilization of water resources in Paraná State in the Pederative Republic of Brazil: interim report. Tóquio, Jan. 1995, p. S-8.
- KITE, G. W. Frequency an risk analyses in hidrology. Fort Collins: Water Resources Publ., 1978. 224p.
- SANT'ANA, Ruy Fernando et al. Projeto HG-52. Aproveitamentos hidrelétricos de pequeno porte: volumes 1 a 4. Curitiba: CEHPAR, 1982.

A VAZÃO MÍNIMA DE SETE DIAS DE DURAÇÃO E DEZ ANOS DE RECORRÊNCIA NO ESTADO DO PARANÁ

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O valor vazão mínima de sete dias de duração e dez anos de recorrência (Q_{10,7}) tem grande importância pois serve, para o Estado do Paraná, como avaliação das condições de captação do potencial de águas superficiais em uma dada bacia hidrográfica.

São analisadas estações em bacias hidrográficas representativas do Estado, e, para cada estação, o valor de Q_{10,7} é calculado por duas distribuições, dois métodos de obtenção da série de mínimas e dois períodos diferentes. Finalmente, são apresentadas equações empíricas relacionando o valor de Q_{10,7} com a área de drenagem, para quatro bacias diferentes e para todo o Estado. O número de estações pesquisadas foi de 30.

Para cada estação estudada, duas distribuições foram ajustadas pelo método dos momentos: a distribuição de Weibull e a distribuição de Galton, ou lognormal a três parâmetros.

Para cada uma destas duas distribuições, foi calculado o valor de Q_{10.7} por duas séries de vazões mínimas diferentes:

• série não-extendida: é, simplesmente, a série de vazões mínimas anuais de sete dias de duração:

• série extendida: utiliza uma série composta com yazões adimensionalizadas mínimas anuais com 7, 15, 21, 30, 45, 60, 90, 120, 150 e 180 dias de duração, segundo a proposta de Gomide (1970).

Finalmente, para os quatro casos descritos acima (duas distribuições e duas séries) são empregados dois períodos diferentes: o histórico,

contendo todos os anos da estação, e o período disponível do ano de 1974 em diante.

Foram computadas estatísticas que calculam a distância abscluta e quadrática dos valores de $Q_{10,7}$ de acordo com três comparações: por distribuição, série e de período.

Os resultados mostraram que praticamente não houve diferença em se aplicar a distribuição de Weibull ou de Galton. Também a diferença entre séries de mínimas não alterou sobremaneira o resultado. O grande

fator de alteração para o valor de Q_{10.7} foi o período utilizado.

Foram ainda calculados, para quatro bacias selecionadas e para o total das estações estudadas, fórmulas relacionando $Q_{10,7}$ com a área de drenagem. As equações foram obtidas pelo método dos mínimos quadrados e foram de segundo ou terceiro grau. As equações resultaram em altos valores do coeficiente de correlação; é preciso tomar cuidado, entretanto, quando da extrapolação para áreas de drenagem maiores ou menores que aquelas para as quais foram calculadas as equações. Estas fórmulas podem ser empregadas como uma primeira estimativa do valor de $Q_{10,7}$ para uma dada área de drenagem.

As conclusões principais do estudo foram:

• no estudo do valor de Q_{10,7}, o maior fator de alteração dos resultados foi o período de dados;

• as equações empíricas relacionando $Q_{10,7}$ e área de drenagem, embora resultando em altos valores para o coeficiente de correlação devem ser empregadas apenas como uma primeira estimativa no valor de $Q_{10,7}$.

THE 10-YEAR-RETURN PERIOD 7-DAY-AVERAGE (Q_{10,7}) LOW FLOW IN PARANÁ STATE

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The value of 10-year-return period 7-day-average low flow $(Q_{10,7})$ is very important because it is worth using in Paraná State as estimation of surface water potential in some given hydrographic basin.

Stations of State representative hydrographic basins are analysed, and, for each station, the $Q_{10,7}$ is calculated according to two distributions, two methods of series obtention and two different periods. Moreover empirical equations are presented relating $Q_{10,7}$ with drainage area, for four different basins and for the whole State.

The most important alteration factor for the $Q_{10,7}$ value was data period. The empirical equations relating $Q_{10,7}$ and drainage area, although resulting high values for correlation coefficients, must be used only as a first estimate of the $Q_{10,7}$ value.